

Strokovno izobraževanje

SATELITI, RADARJI IN NAVIGACIJA

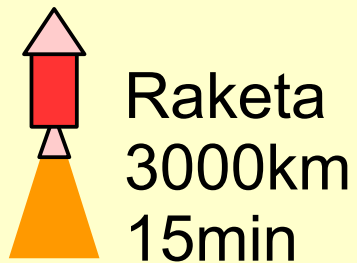
Matjaž Vidmar

AKOS, Ljubljana, 12.6.2015

Seznam prosojnic predavanja: SATELITI, RADARJI IN NAVIGACIJA

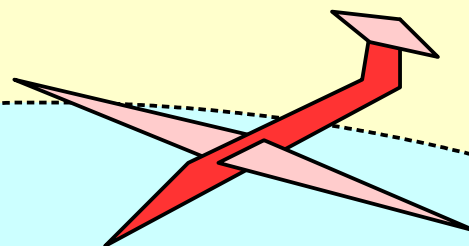
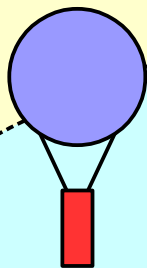
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Vesolje



Letalo
30km
12h

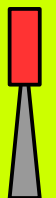
Balon
30km



Ozračje

Hrib
3000m

Stolp
100m



Kopno

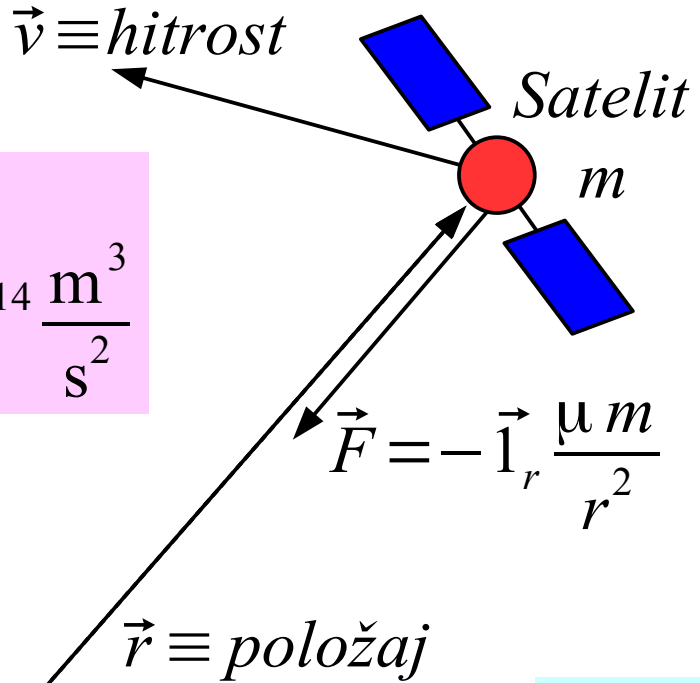
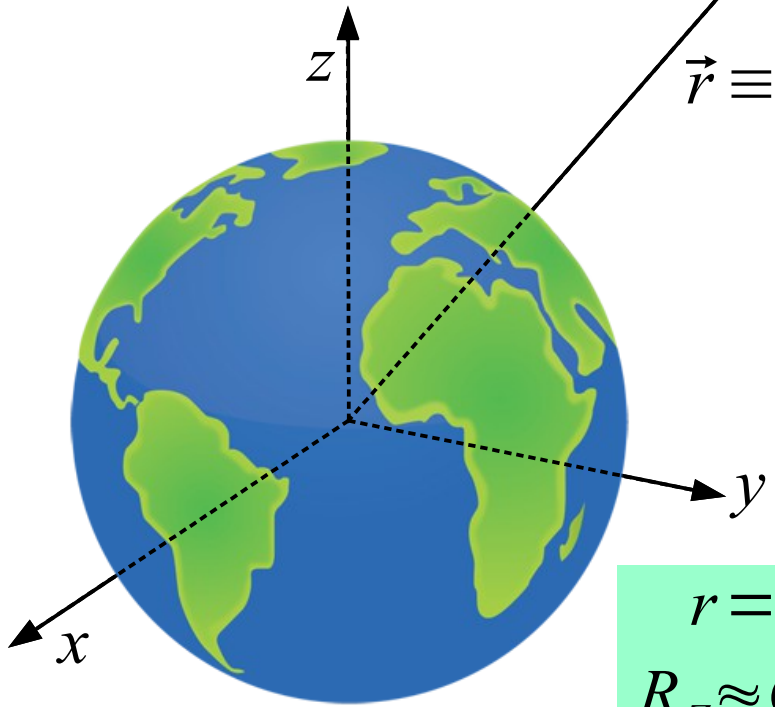
Morje

1 - Visoka radijska postaja

$$\vec{F} = -\vec{1}_r G \frac{M m}{r^2}$$

Zemlja

$$\mu = G M \approx 3.986 \cdot 10^{14} \frac{\text{m}^3}{\text{s}^2}$$



Energija

$$W = \frac{1}{2} m v^2 - \frac{\mu m}{r} = \text{konst.}$$

Vrtilna količina

$$\vec{l} = \vec{r} \times m \vec{v} = \text{konst.}$$

Enačba gibanja

$$\vec{a} = \frac{d^2 \vec{r}}{dt^2} = \frac{\vec{F}}{m} = -\vec{1}_r \frac{\mu m}{r^2}$$

Enačba stožnice $r = \frac{p}{1 + e \cos \varphi}$

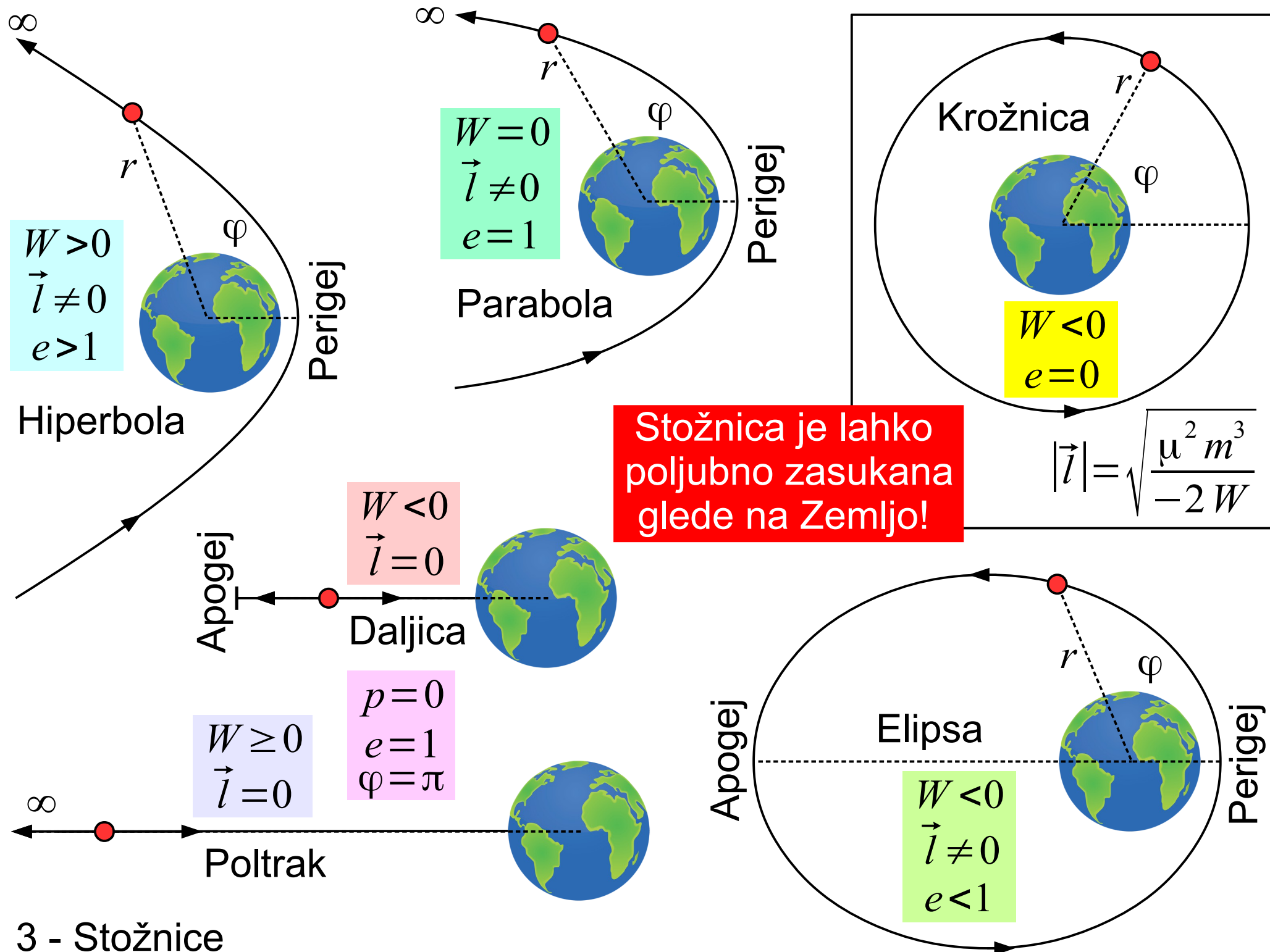
$$p = \frac{|\vec{l}|^2}{\mu m^2} \quad e = \sqrt{1 + \frac{2W |\vec{l}|^2}{\mu^2 m^3}}$$

$$r = R_Z + h$$

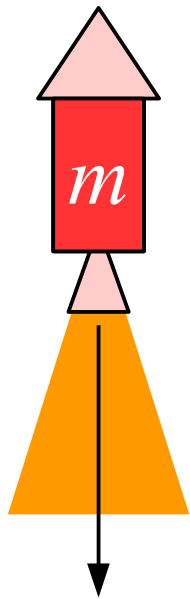
$$R_Z \approx 6378 \text{ km}$$

$h < 200 \text{ km} \rightarrow$ trenje z ozračjem!

$h > 50000 \text{ km} \rightarrow$ težnost Sonca, Lune!



Stožnica je lahko poljubno zasukana glede na Zemljo!



$$\sum \vec{F} = 0 = -\frac{d m}{d t} \vec{v}_i + \vec{a} m \rightarrow \vec{a} = \frac{\vec{v}_i}{m} \cdot \frac{d m}{d t}$$

$$\Delta \vec{v} = \int_{t_1}^{t_2} \vec{a} d t = \int_{m_1}^{m_2} \frac{\vec{v}_i}{m} d m = -\vec{v}_i \frac{m_1}{m_2} = -\vec{v}_i \ln \left(1 + \frac{m_g}{m_t} \right)$$

$m_g \equiv$ masa goriva $m_t \equiv$ masa tovora

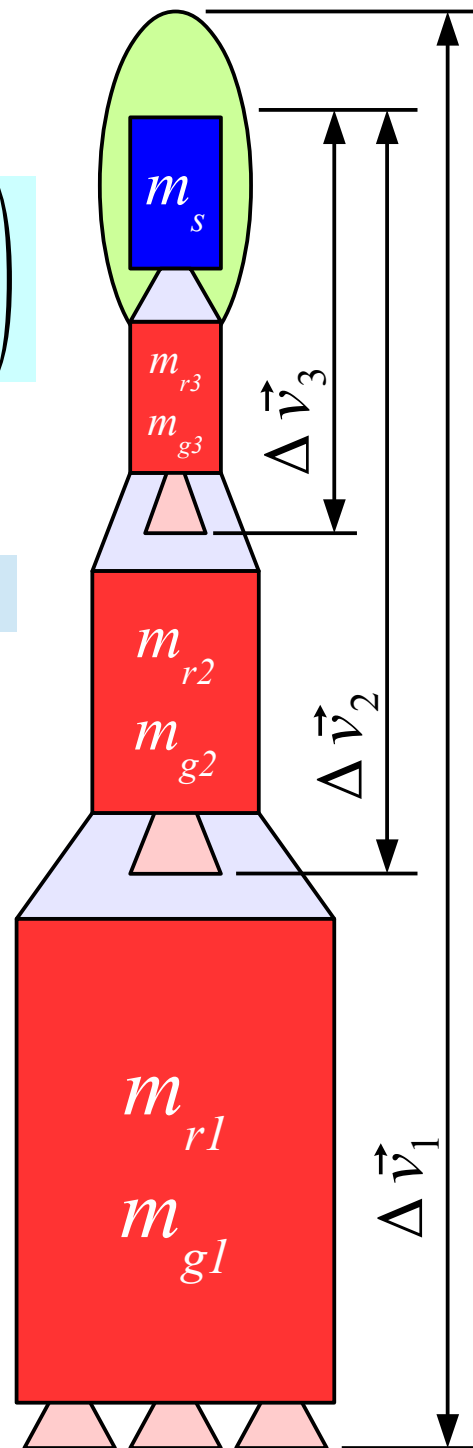
$\vec{v}_i \equiv$ hitrost izpuha

$\Delta \vec{v} \equiv$ sprememba hitrosti

Gorivo	v_i	Δv $m_g = 9m_t$
Hladen N_2	0.3km/s	0.7km/s
H_2O_2	1.5km/s	3.5km/s
N_2H_4	2.2km/s	5.1km/s
$Al + NH_4ClO_4$	2.7km/s	6.2km/s
$N_2H_2(CH_3)_2 + N_2O_4$	3.0km/s	6.9km/s
Tekoča $H_2 + O_2$	4.5km/s	10.4km/s

Potrebno:
 $\sum \Delta v = 8 \dots 12 \text{ km/s}$
 Večstopenjska raketa!

$$m_g = m_t \left(e^{\frac{\Delta v}{v_i}} - 1 \right)$$



4 - Enačba gibanja rakete

$$r_a = \frac{p}{1-e} = a(1+e)$$

$$h_a = r_a - R_Z$$

$$e = \frac{r_a - r_p}{r_a + r_p}$$

$e \equiv$ ekscentričnost

$$a = \frac{p}{1-e^2} \equiv \text{velika polos}$$

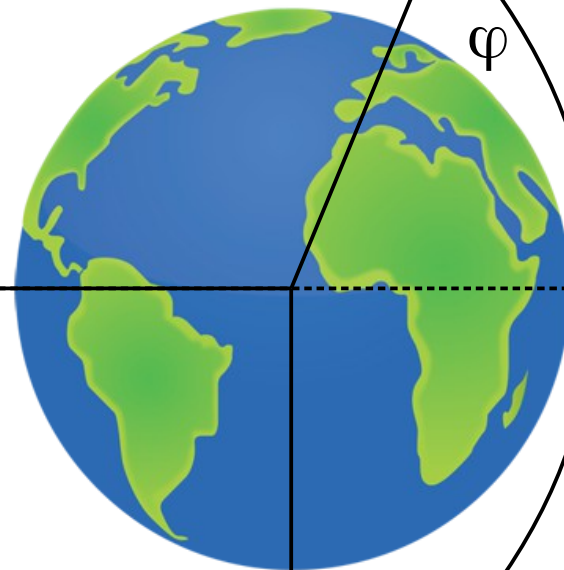
Apogej

h_a

$$f = a e \equiv \text{goriščnica}$$

$b \equiv$ mala polos

f



$$a = -\frac{\mu m}{2W}$$

Plovilo

\vec{r}

φ

Perigej

h_p

Elipsa

$$W < 0$$

$$\vec{l} \neq 0$$

$$0 \leq e < 1$$

$$b = \sqrt{a^2 - f^2}$$

$$p = a(1 - e^2)$$

$$h_p = r_p - R_Z$$

$$a = \sqrt[3]{\mu \left(\frac{T}{2\pi} \right)^2}$$

$$r_p = \frac{p}{1+e} = a(1-e)$$

$$\text{Perioda } T = 2\pi \sqrt{\frac{a^3}{\mu}}$$

Elipsa je lahko poljubno zasukana glede na Zemljo!

$$\text{Hitrost } v = \sqrt{\mu \left(\frac{2}{r} - \frac{1}{a} \right)}$$

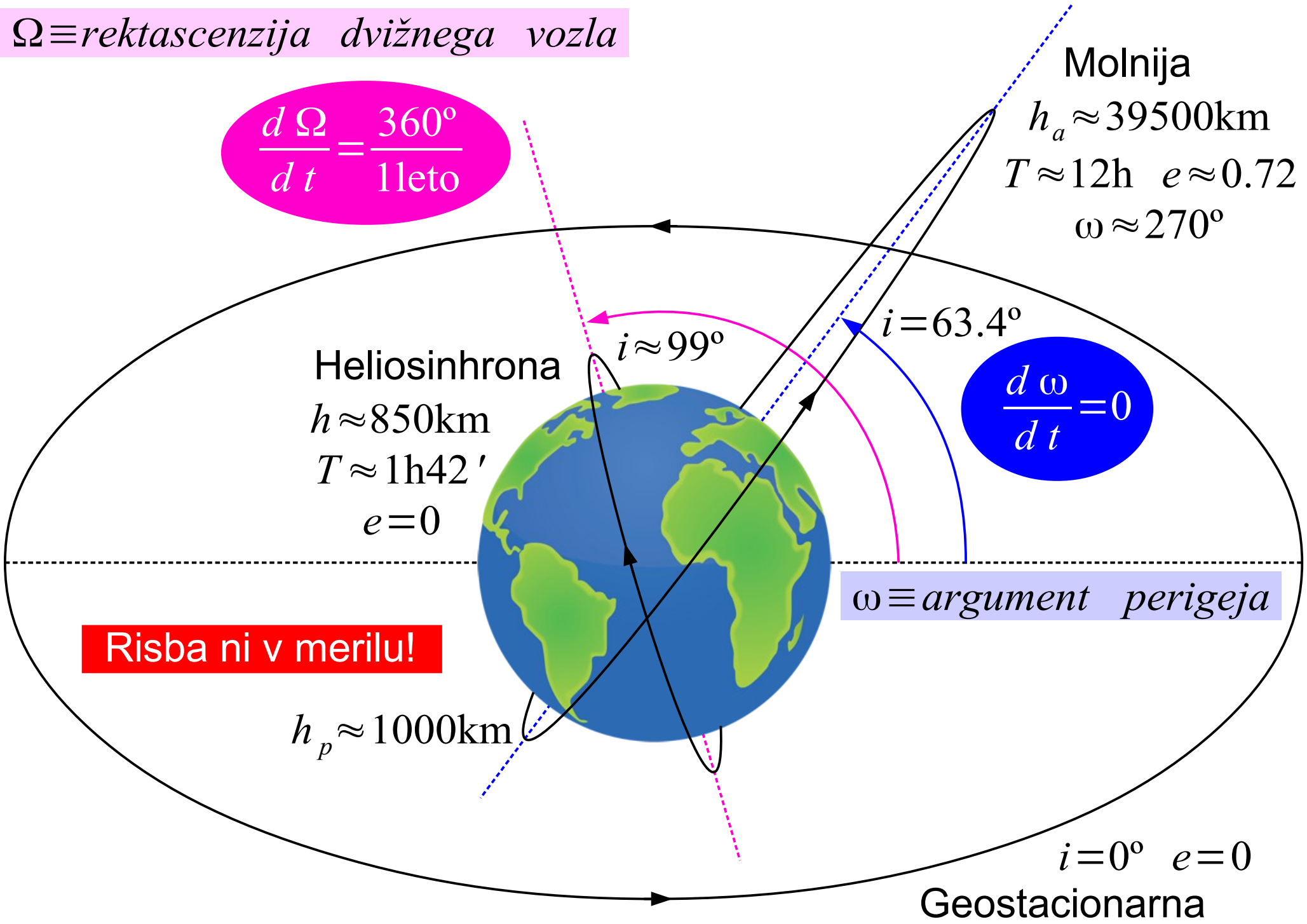
5 - Eliptična tirnica

$\Omega \equiv$ rektascenzija dvižnega vozla

$$\frac{d\Omega}{dt} = \frac{360^\circ}{1 \text{ leto}}$$

Molniya

$h_a \approx 39500 \text{ km}$
 $T \approx 12 \text{ h}$ $e \approx 0.72$
 $\omega \approx 270^\circ$

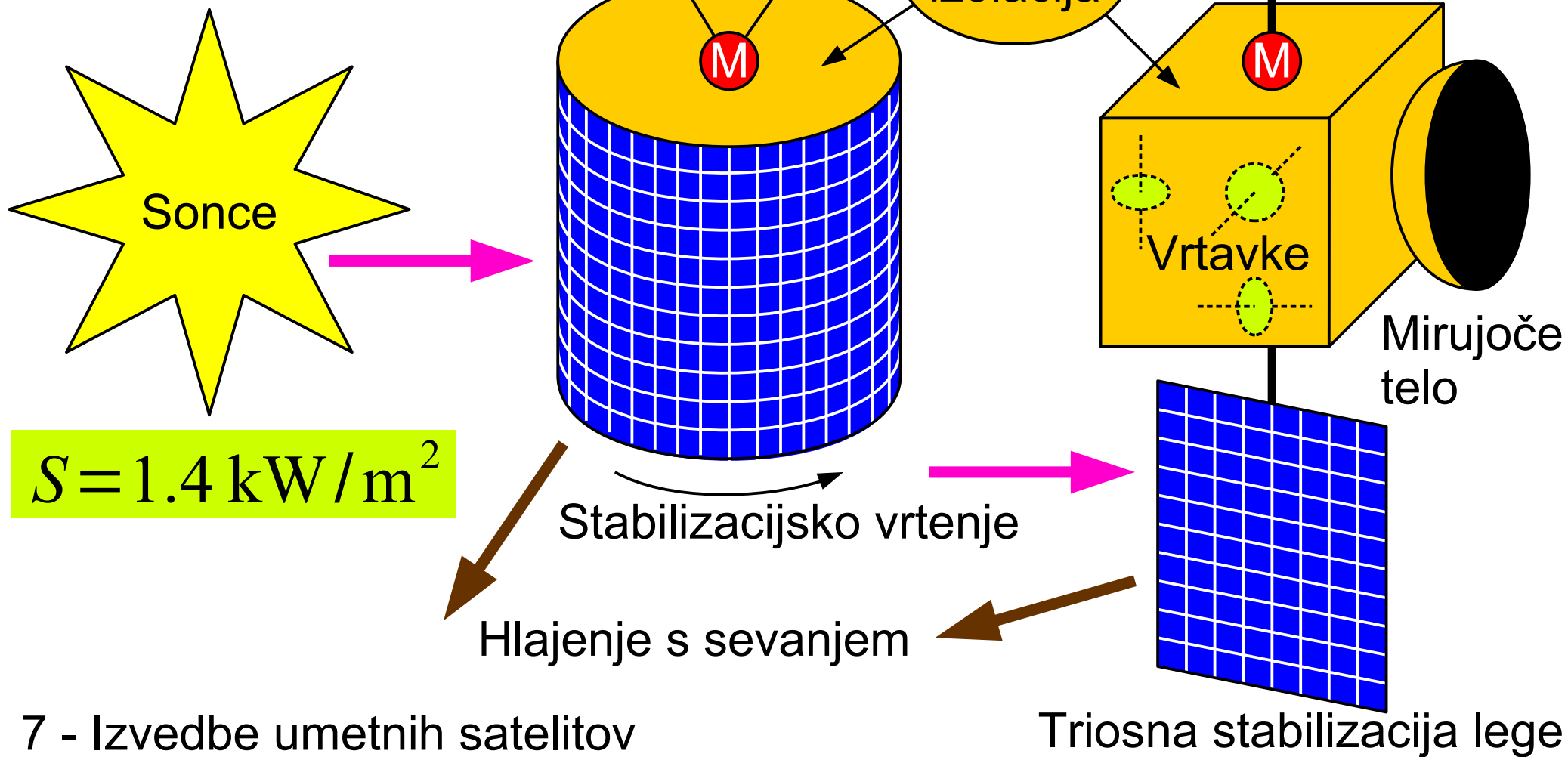


6 - Uporabne tirnice umetnih satelitov

$i = 0^\circ$ $e = 0$
Geostacionarna
 $h \approx 35800 \text{ km}$ $T \approx 23 \text{ h } 56'$

Načrtovanje satelita:

- (1) toplotno ravnovesje?
- (2) izvor energije?
- (3) stabilizacija lege?
- (4) ionizirajoče sevanje?



$$P_{\text{max}} \leq 10\text{kW}$$

Prepustnost ozračja
 $100\text{MHz} \leq f \leq 50\text{GHz}$

$$A \leq 10\text{m}^2$$

$$r \approx 38000\text{km}$$

Zakasnitev

$$\Delta t = \frac{2r}{c_0} \approx 0.25\text{s}$$

Omejena zmogljivost:

- (1) radiodifuzija
- (2) radionavigacija
- (3) opazovanje Zemlje

$$P_{RX} \approx \frac{P_{TX} G^2 \lambda^2}{(4\pi)^3 r^4} \sigma$$

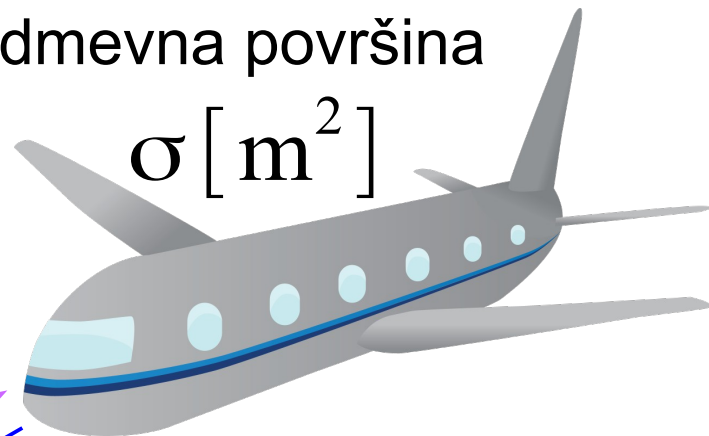
$$\lambda = 0.1 \text{ m}$$

Odmevna površina

$$\sigma [\text{m}^2]$$

$$t_p \approx 1 \mu\text{s}$$

$$T \approx 3 \text{ ms}$$



$$P_{TX} = +90 \text{ dBm} = 1 \text{ MW}$$

$$P_{RX} = -90 \text{ dBm} = 1 \text{ pW}$$

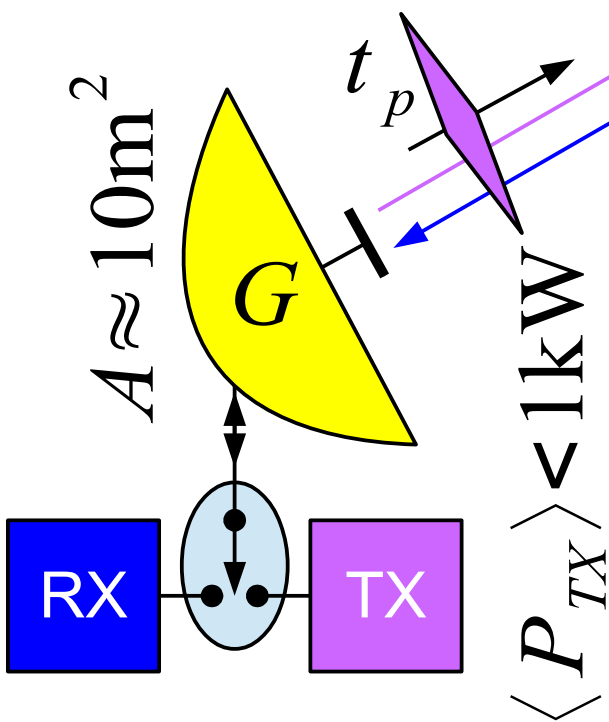
$$G = 40 \text{ dBi} = 10^4$$

$$r = \sqrt[4]{\frac{P_{TX} G^2 \lambda^2}{P_{RX} (4\pi)^3 \sigma}}$$

$$r = c_0 2 \Delta t$$

$$\sigma \approx 0.01 \text{ m}^2$$

$$\sigma \approx 30 \text{ m}^2$$



Letalo	σ	r
Cessna C172	$\sim 1 \text{ m}^2$	$\sim 150 \text{ km}$
Airbus A320	$\sim 10 \text{ m}^2$	$\sim 266 \text{ km}$
Lockheed F117	$\sim 0.01 \text{ m}^2$	$\sim 47 \text{ km}$

9 - Pulzni RADAR

$$f_{RX} = f_{TX} + \Delta f$$

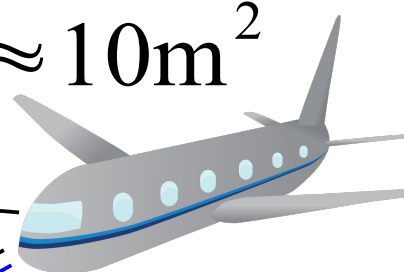
Zahtevna primerjava
faze zaporednih
impulzov!

$$\Delta f \ll 1/t_p$$

$$\vec{v} \neq 0$$

$$\sigma \approx 10\text{m}^2$$

$$\vec{l}_r$$



$$\vec{v} = 0$$

$$\sigma \approx 10^6\text{m}^2 = 1\text{km}^2$$

+50dB

$$\Delta f = 2 \frac{f_{TX}}{c_0} (\vec{v} \cdot \vec{l}_r) \equiv \text{Dopplerjev pomik}$$

Letalo $v \approx 800\text{ km/h}$

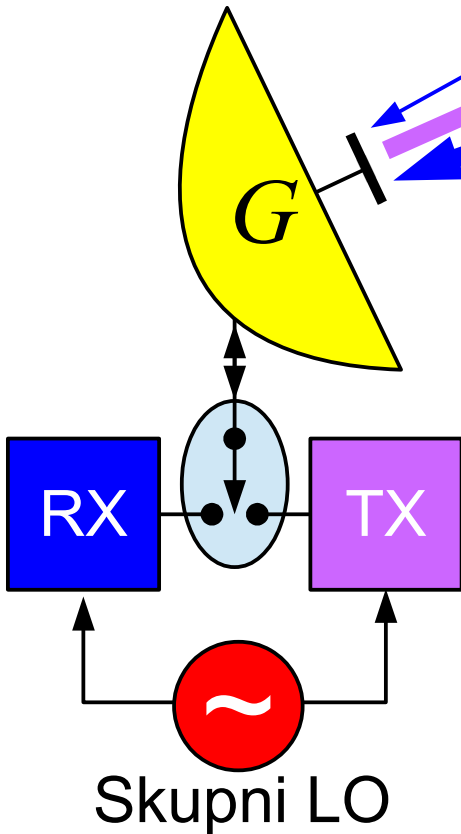
Hrib $v \approx 0\text{ km/h}$

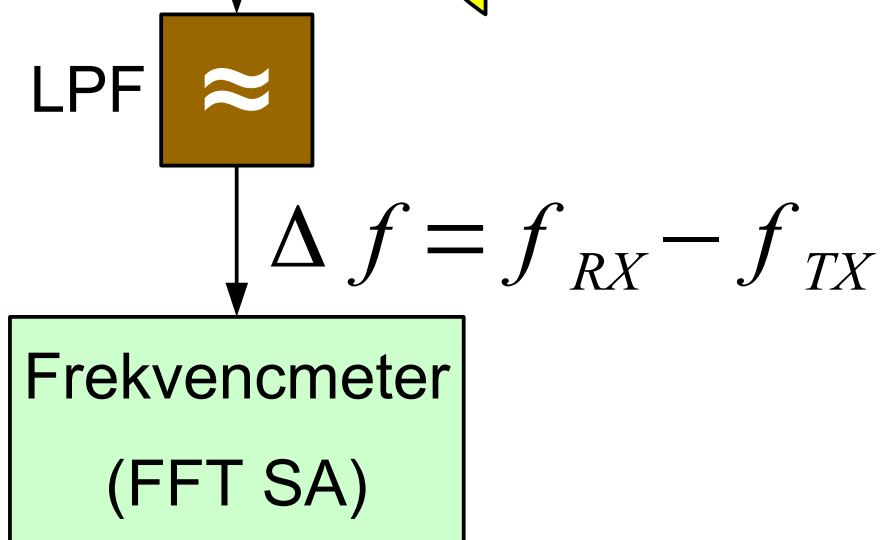
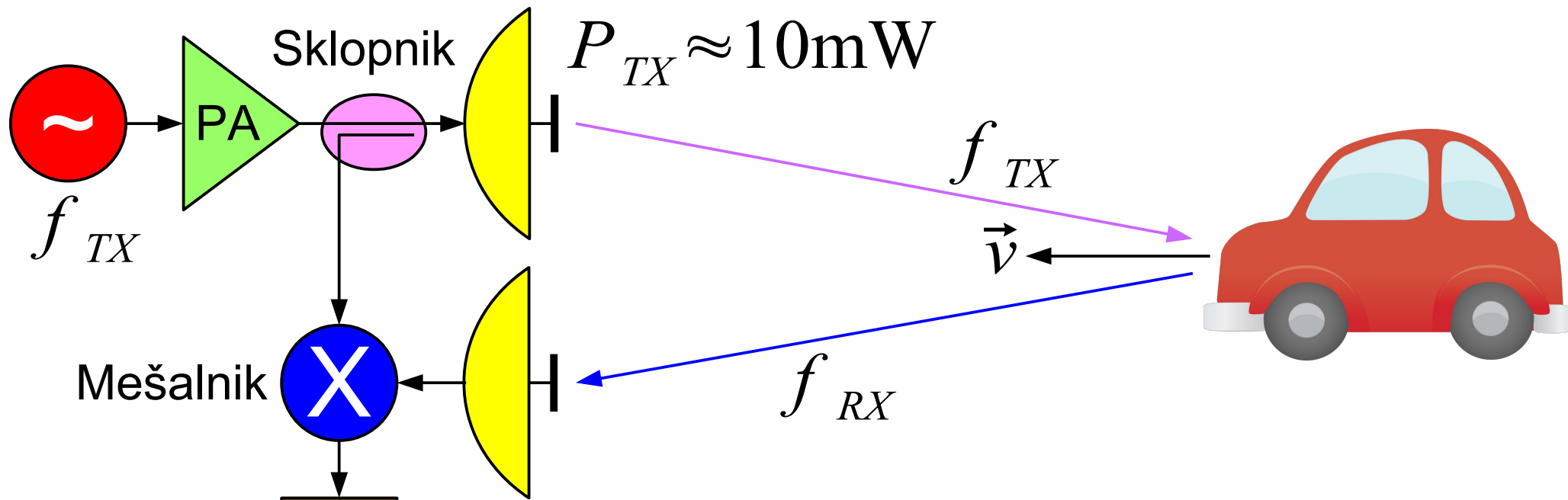
Razločevanje
premičnih
ciljev:

RADAR ne vidi:

počasnih ciljev: baloni, jadralci...

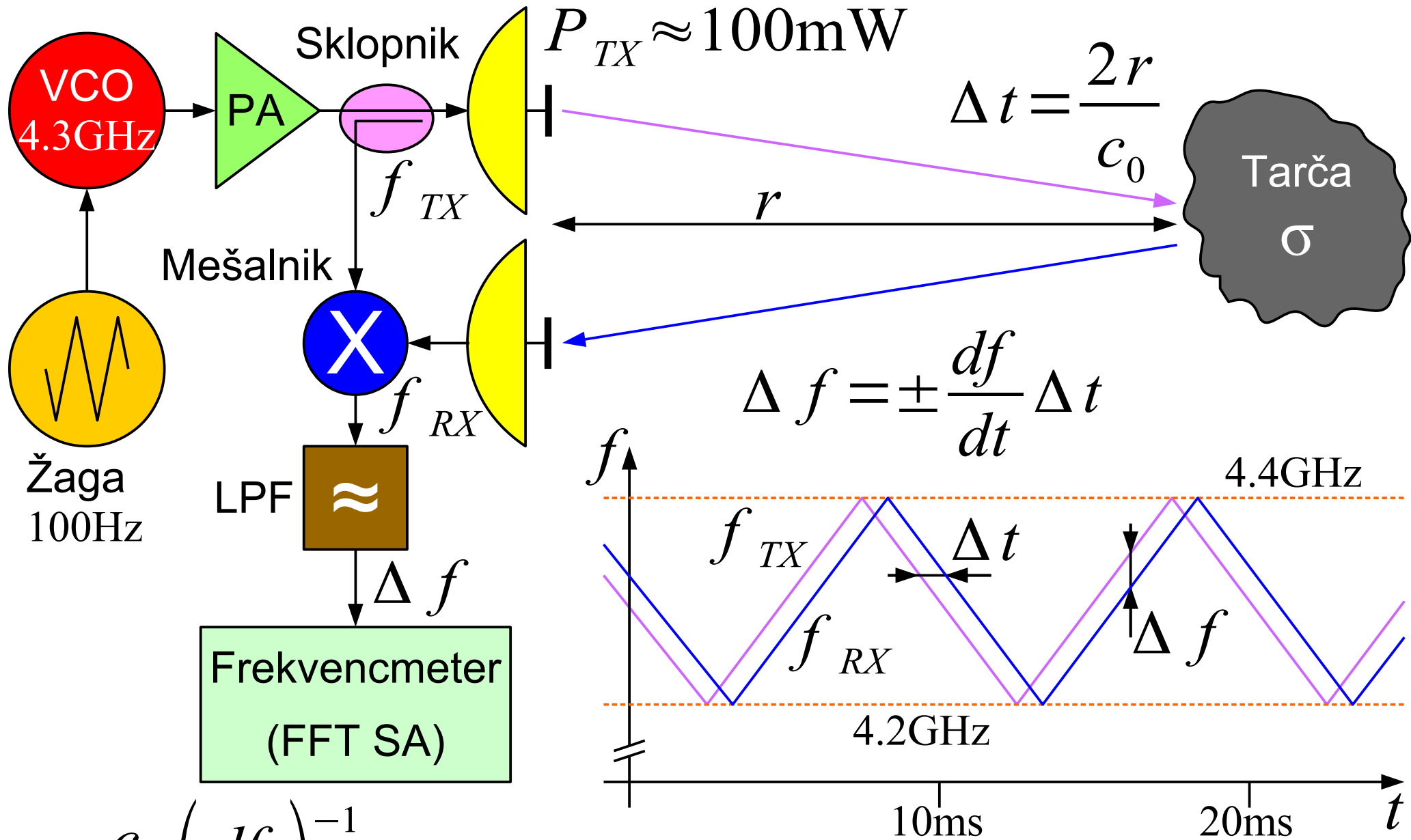
tangencialnih ciljev: $\vec{v} \perp \vec{l}_r$





$$v = \frac{c_0}{2 f_{TX}} \Delta f$$

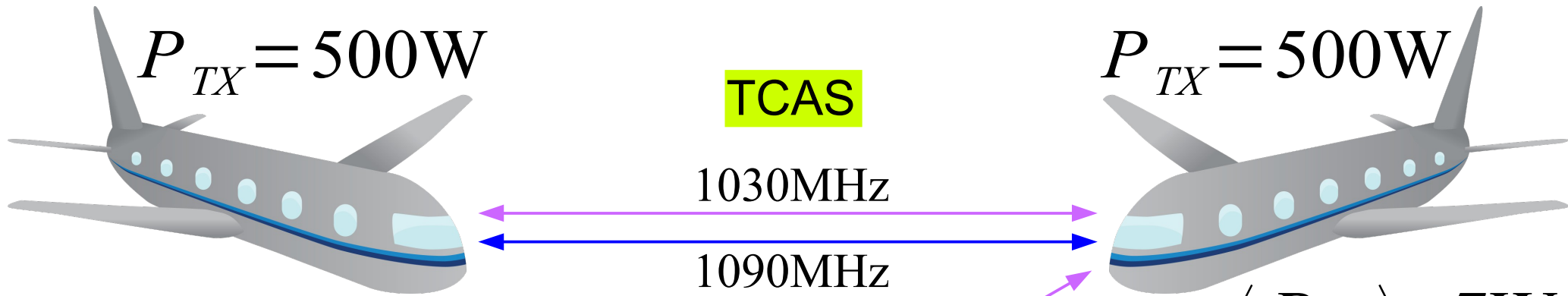
Frekvenčni pasovi	
9.375GHz	Ni več v uporabi
10.525GHz	Region 2
24GHz	ISM
34GHz	Licenciran



$$r = \frac{c_0}{2} \left(\frac{df}{dt} \right)^{-1} \Delta f$$

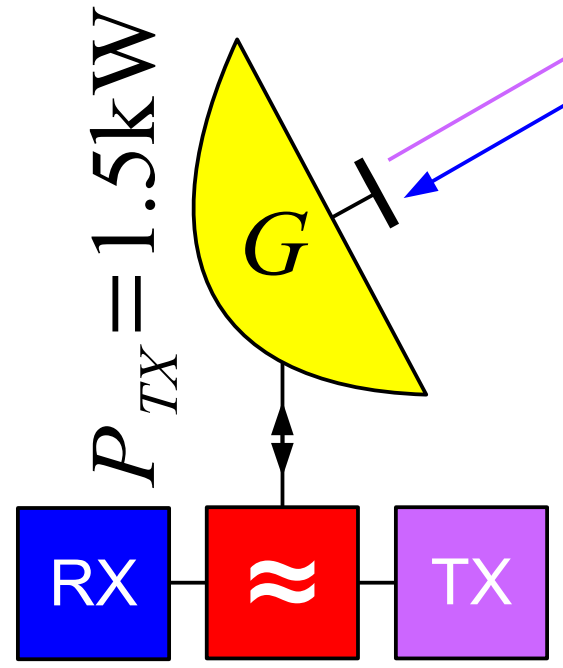
12 - FMCW RADAR

Letalski višinomer	4.3GHz±100MHz
Avtomobilski RADAR	77GHz±1GHz



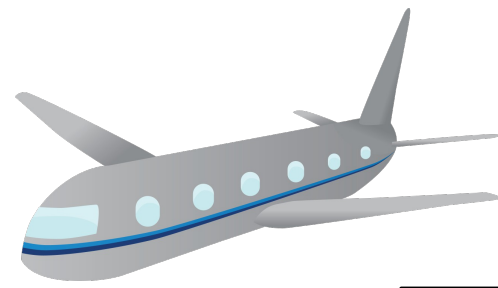
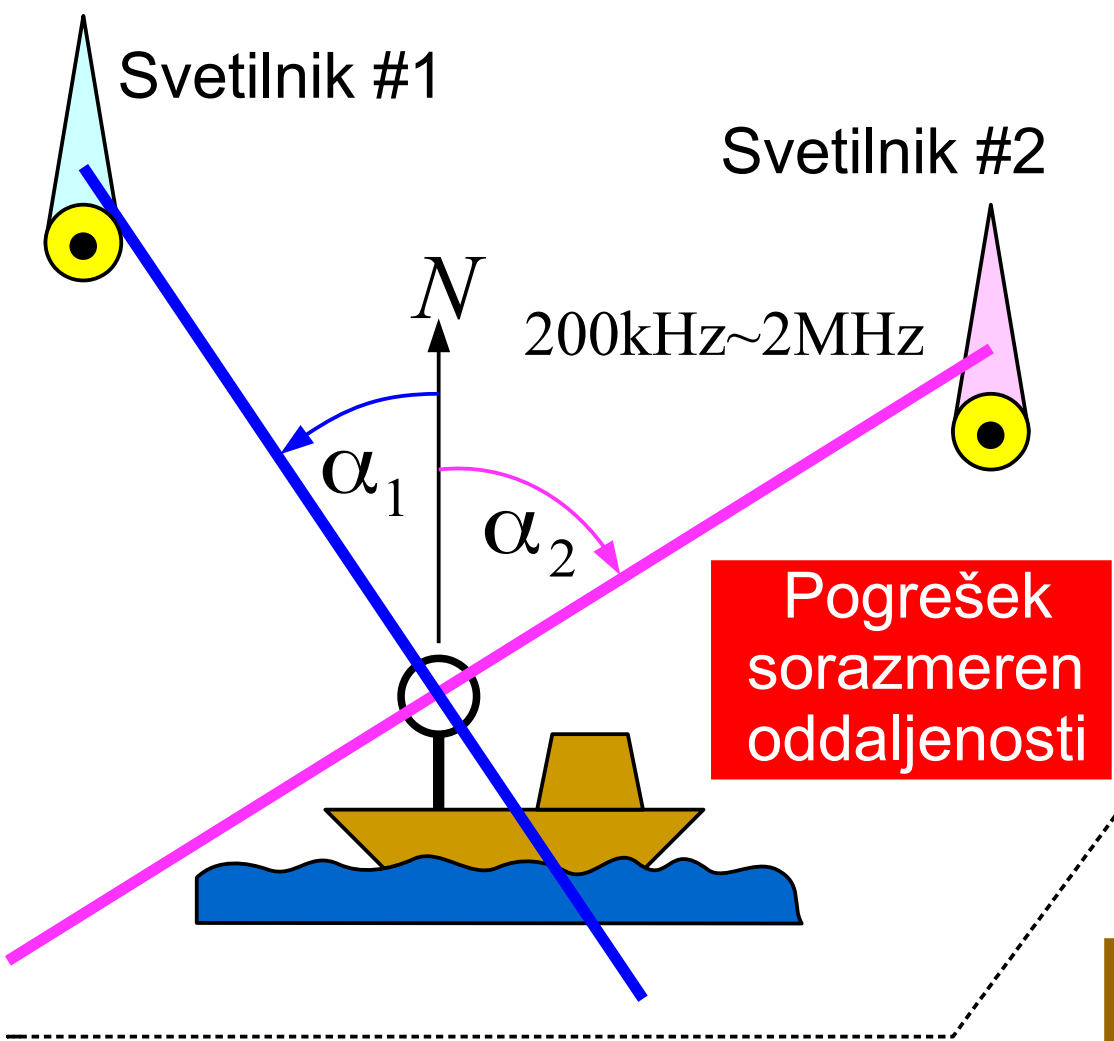
Vprašanja 1030MHz:
 Mode „A“ 2 pulza 8μs
 Mode „C“ 2 pulza 21μs
 Mode „S“ 56bit/112bit
 4Mbps BPSK

TCAS ≡ Traffic-alert Collision Avoidance System
 TCAS-1: Traffic Advisory C/S
 TCAS-2: Resolution Advisory S



Odgovori 1090MHz:
 Mode „A“ koda letala 15bit
 Mode „C“ višina letala 13bit
 Mode „S“ 56bit/112bit
 1Mbps Manchester/ASK

TCAS nima avtentikacije
 TCAS nima kriptazaščite
 Protokol TCAS je javno dosegljiv



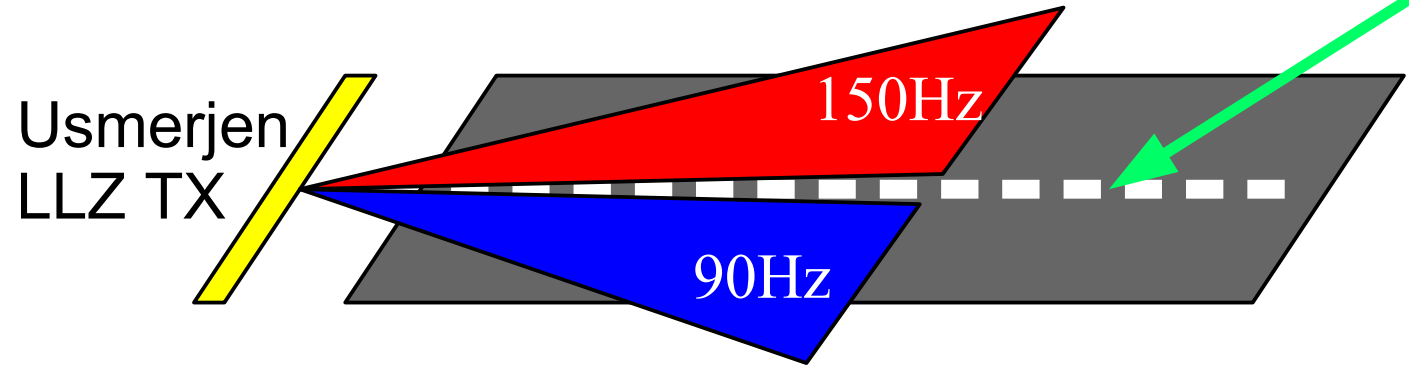
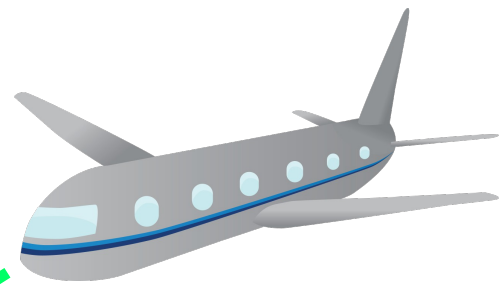
Zelo groba navigacija



Usmerjen marker TX

Marker 75MHz	
OM	400Hz
MM	1300Hz
IM	3000Hz

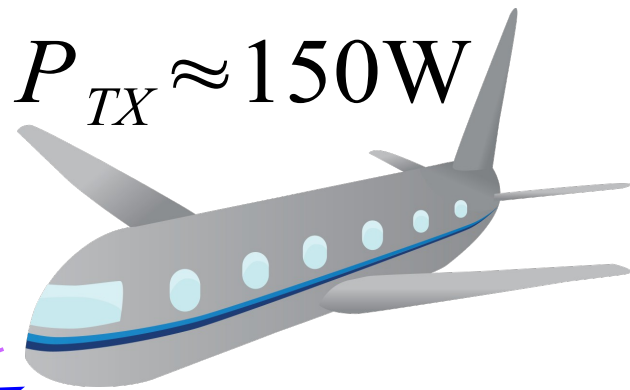
Navigacija na točko



Frekvence ILS	
LLZ	108.1MHz ~ ~111.95MHz
GS	328.6MHz ~ ~335.4MHz

DME/P uporablja 2 pulza 18 μ s ali 24 μ s

$$P_{TX} \approx 150W$$



DME vprašanja:

126 kanalov „X“ 2 pulza 12 μ s

126 kanalov „Y“ 2 pulza 30 μ s

$f=1025\text{MHz}\sim 1150\text{MHz}$

Omejeno število aktivnih uporabnikov $N < 100$ / en odzivnik

Odzivnik
DME

DME odgovori:

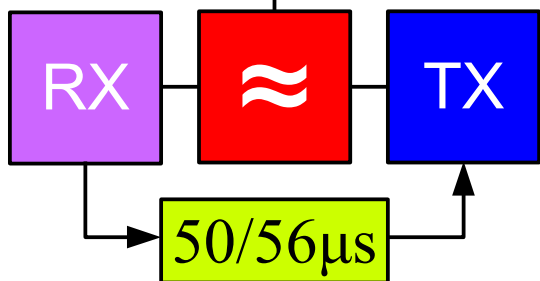
126 kanalov „X“ 2 pulza 12 μ s

$f_x = 962\text{MHz}\sim 1024\text{MHz}$ in $1151\text{MHz}\sim 1213\text{MHz}$

126 kanalov „Y“ 2 pulza 36 μ s

$f_y = 1025\text{MHz}\sim 1150\text{MHz}$

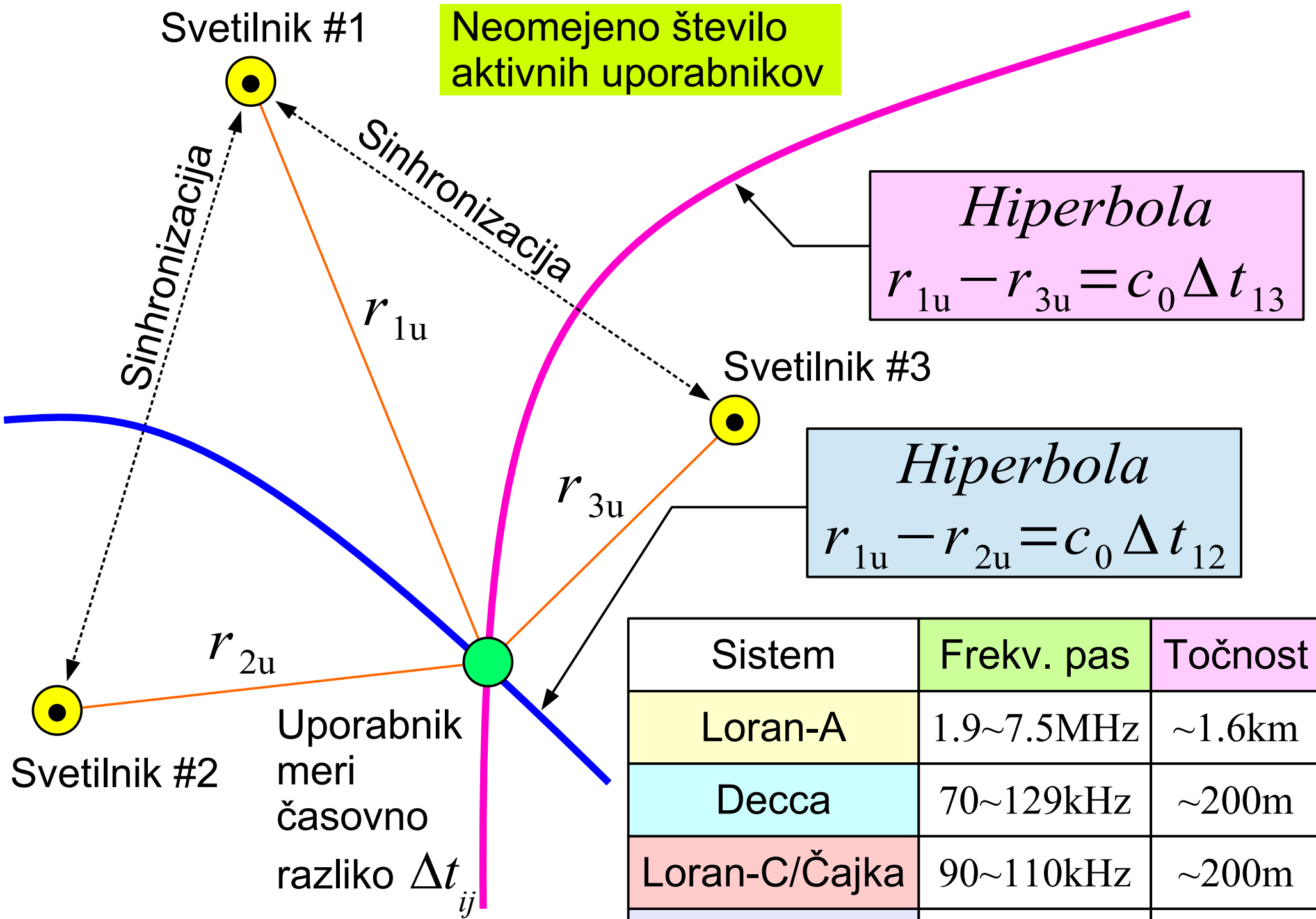
$$f_{odgovor} = f_{vprašanje} \pm 63\text{MHz}$$



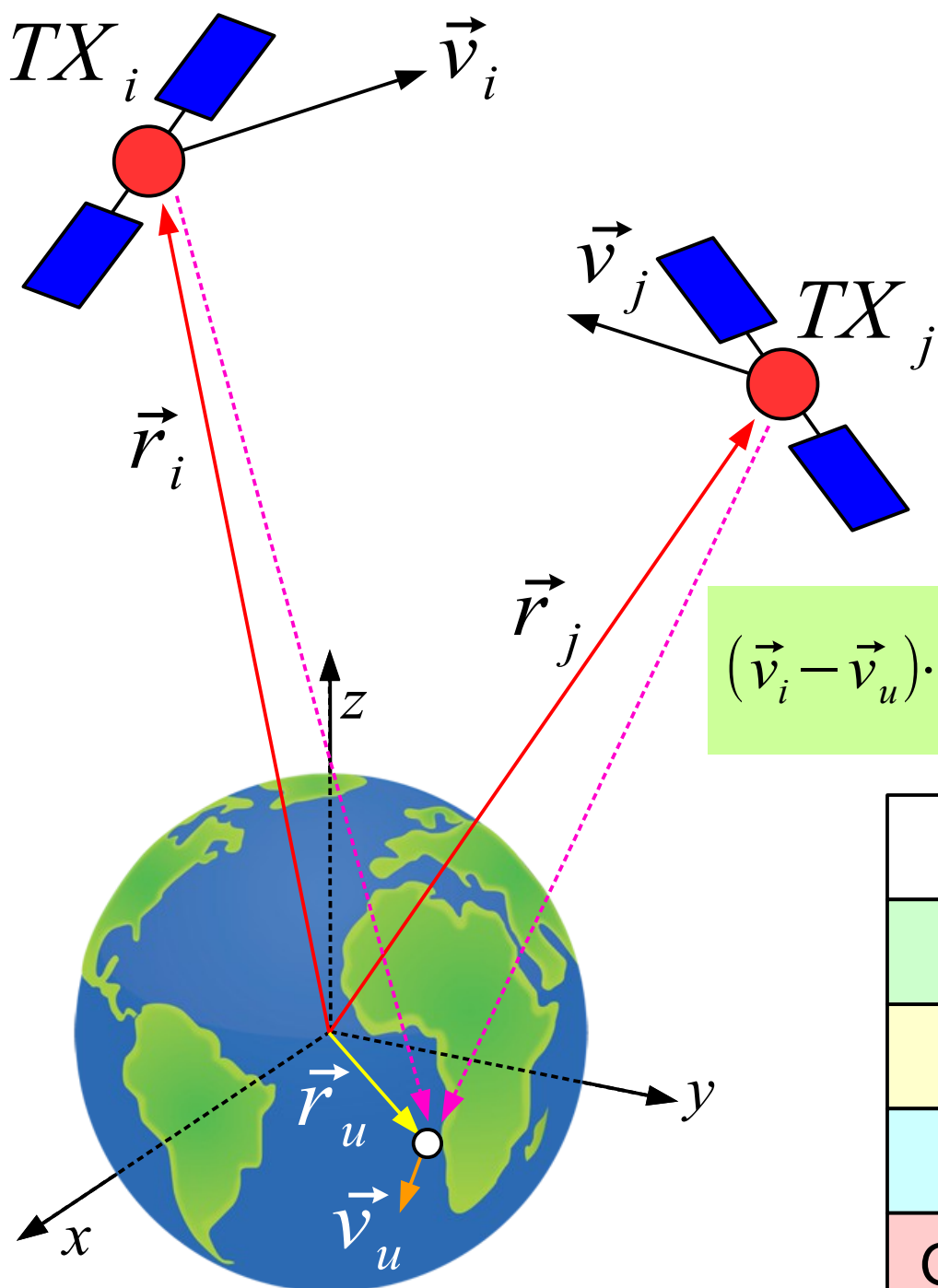
$$P_{TX} \approx 1.5\text{kW}$$

Točnost $\sim 0.1\text{nm} = 185\text{m}$ neodvisna od razdalje
2/3 odzivniki omogočajo 2D/3D navigacijo

15 - Časovna radionavigacija DME



Sistem	Frekv. pas	Točnost
Loran-A	1.9~7.5MHz	~1.6km
Decca	70~129kHz	~200m
Loran-C/Čajka	90~110kHz	~200m
Omega/Alpha	9~14KHz	~2.2km



Zakasnitev modulacije:

$$|\vec{r}_i - \vec{r}_u| - |\vec{r}_j - \vec{r}_u| = c_0 \Delta t_{ij}$$

Neznanke: $\vec{r}_u, \vec{v}_u, t_u, f_u$
 Potreben nabor enačb?

Doppler nosilca:

$$(\vec{v}_i - \vec{v}_u) \cdot \frac{(\vec{r}_i - \vec{r}_u)}{|\vec{r}_i - \vec{r}_u|} - (\vec{v}_j - \vec{v}_u) \cdot \frac{(\vec{r}_j - \vec{r}_u)}{|\vec{r}_j - \vec{r}_u|} = \frac{c_0}{f_0} \Delta f_{ij}$$

Sistem	Tirnica	Frekvence
Transit	1100km/90°	399.968MHz 149.988MHz
Cikada	970km/83°	~400MHz ~150MHz
GPS	20200km/55°	1575.42MHz 1227.6MHz
GLONASS	19100km/65°	~1600MHz ~1250MHz
BeiDou	21500km/55°	1561.098MHz 1207.140MHz