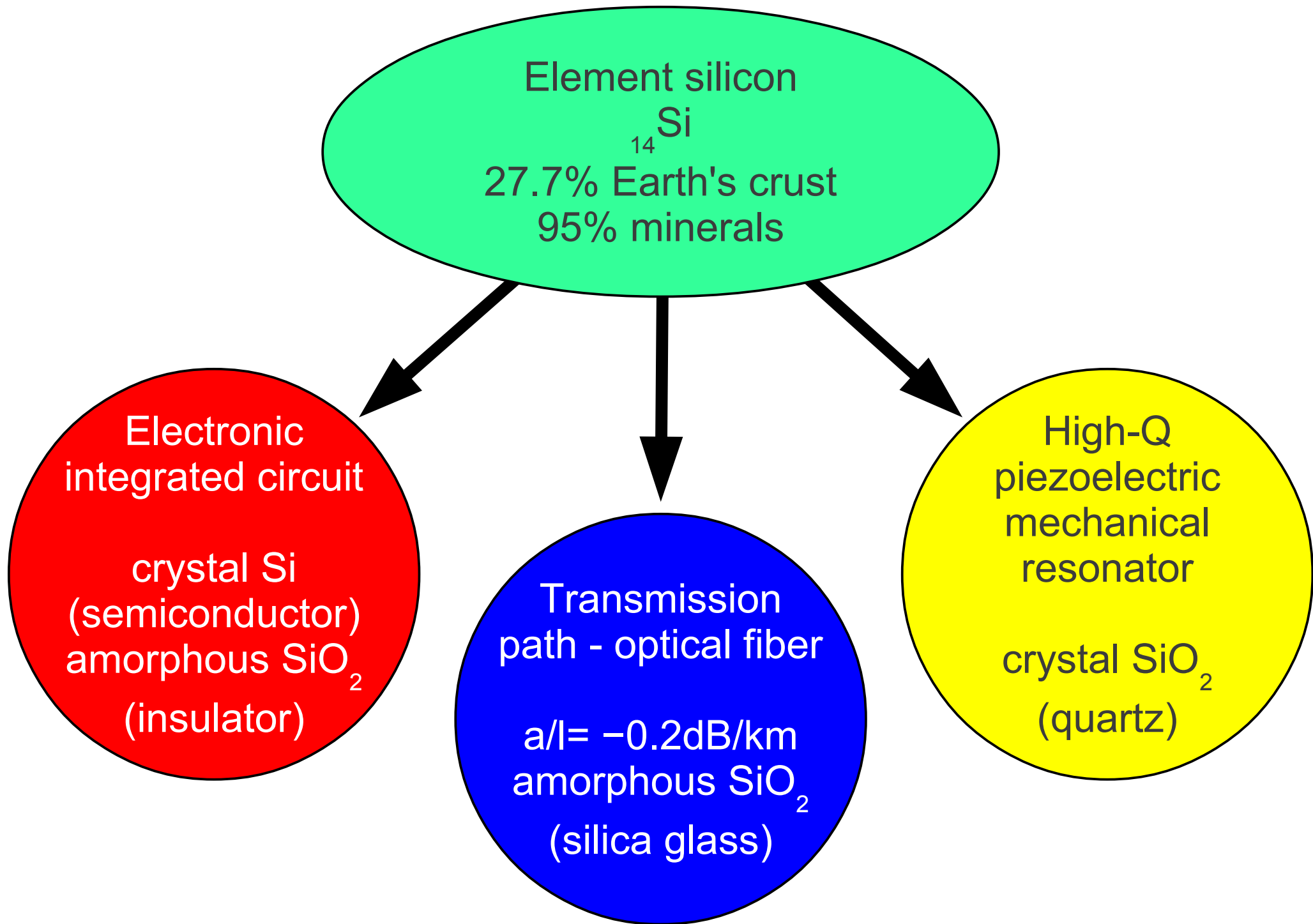


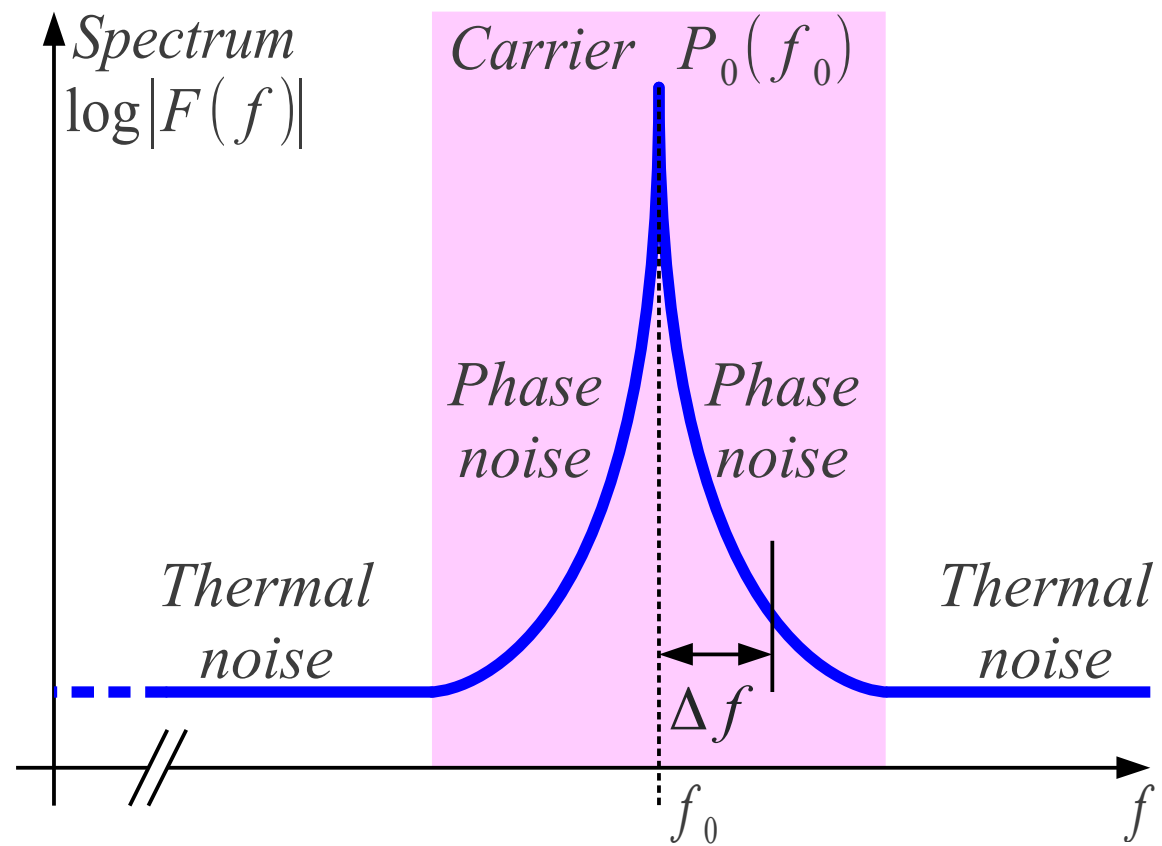
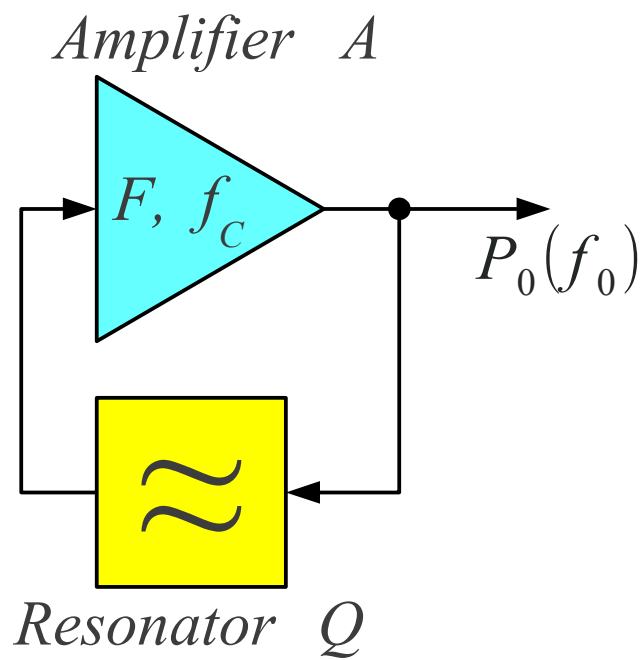
# Communication Electronics

## Lecture 9:

### Piezoelectric devices



*Communication – electronics roles of silicon*



Leeson's equation:  
phase – noise spectral density

$$L(\Delta f) = \frac{1}{P_0} \cdot \frac{dP_N}{df} = \frac{1}{2} \cdot \left[ 1 + \left( \frac{f_0}{2Q_L \Delta f} \right)^2 \right] \cdot \frac{k_B T_0 F}{P_0} \cdot \left( 1 + \frac{f_c}{|\Delta f|} \right)$$

$k_B \approx 1.38 \cdot 10^{-23} \text{ J/K} \equiv \text{Boltzmann constant}$

$T_0 \approx 290\text{K} \equiv \text{circuit temperature}$

$F \equiv \text{amplifier noise figure}$

$f_c \equiv \text{flicker noise corner frequency}$

$Q_L \equiv \text{loaded resonator } Q$

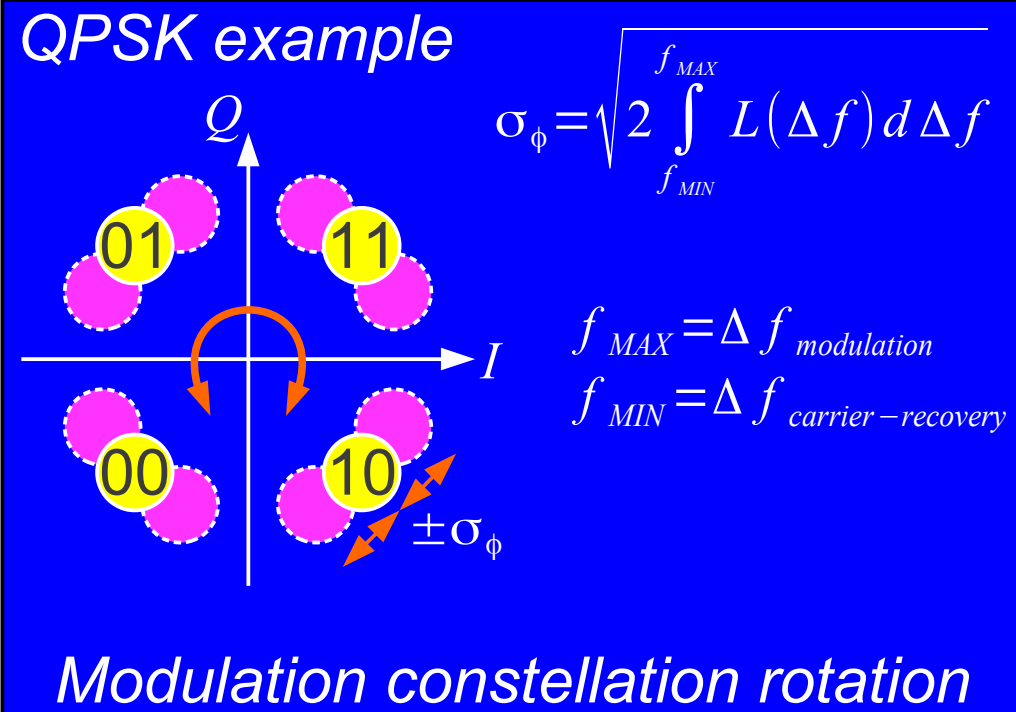
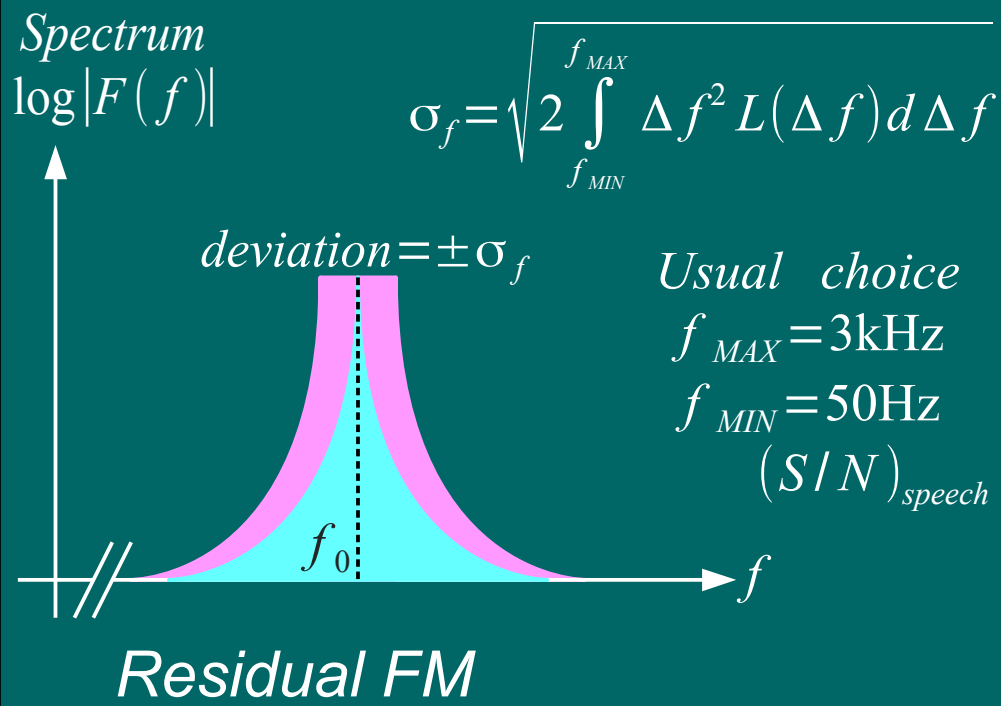
$Q_L \approx 30 \text{ (LC resonant circuit)}$

$Q_L \approx 1000 \text{ (electrical cavity)}$

$Q_L \approx 30000 \text{ (quartz crystal)}$

*Oscillator phase noise*

$$L(\Delta f)_{\text{dBc/Hz}} = 10 \log_{10} [L(\Delta f) \cdot 1\text{Hz}]$$



Analog radio link:

$$Q_L \approx 30 \dots 1000$$

SSB (A3j w/o carrier)  $\rightarrow f_0 < 30\text{MHz}$

FM (speech  $B=15\text{kHz}$ )  $\rightarrow f_0 < 1\text{GHz}$

FM (picture  $B=30\text{MHz}$ )  $\rightarrow f_0 < 30\text{GHz}$

*Phase – noise constraints*

Digital radio link:

$$Q_L \approx 1000 \dots 30000$$

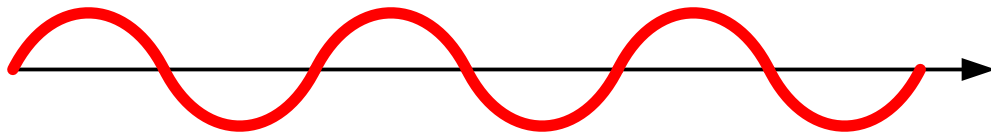
Dense OFDM ( $N > 1000$ )  $\rightarrow f_0 < 1\text{GHz}$

Coarse OFDM ( $N < 100$ )  $\rightarrow f_0 < 10\text{GHz}$

Single-carrier QPSK  $\rightarrow f_0 < 100\text{GHz}$

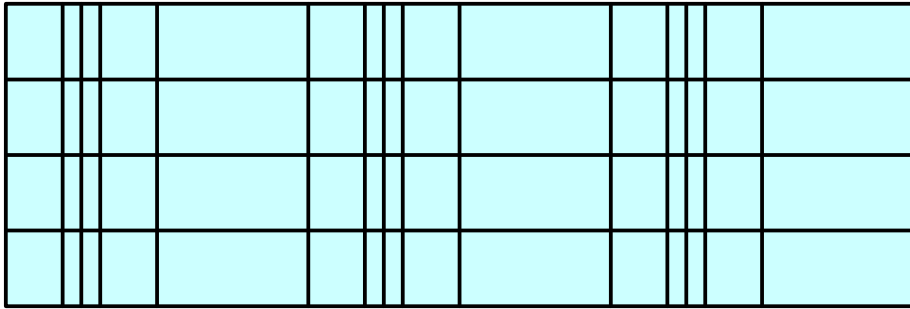
- 1880 – Jacques & Pierre Curie discover the piezoelectric effect
- 1905 – Giorgio Spezia hydrothermal growth of quartz crystals in lab
- 1917 – First use of the piezoelectric effect in sonar
- 1918 – First use of a quartz crystal in an oscillator
- 1926 – First broadcast transmitter with a quartz oscillator
- 1927 – Discovery of a thermally-compensated quartz cut
- 1927 – First clock with a quartz crystal
- 1934 – First practical thermally-compensated "AT" cut
- 1949 – High-Q, high-stability "AT" cut developed
- 1956 – First artificial synthetic quartz crystals available
- 1956 – Described first TCXO
- 1972 – Tuning-fork quartz crystal for wrist watches
- 1974 – Predicted "SC" cut and verified 1976

*History of quartz in electronics*

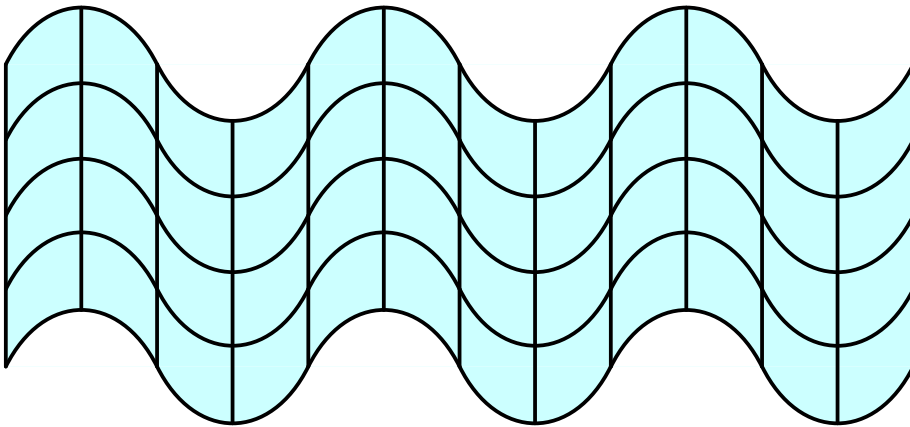


# *Mechanical waves*

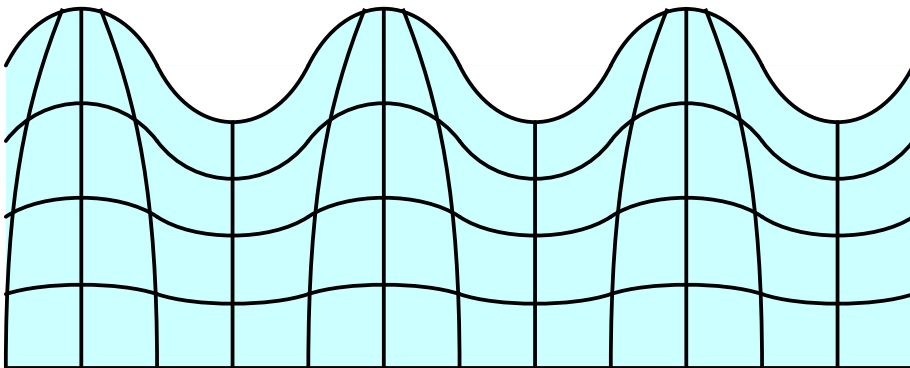
$v \approx 2\text{km/s} \dots 12\text{km/s}$  (*solids*)



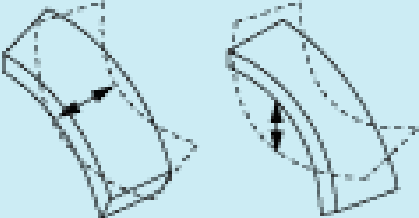


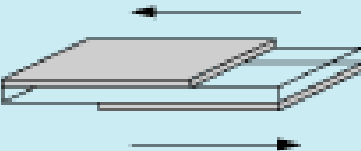
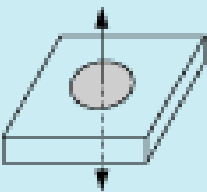

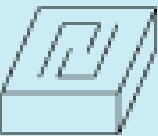
Pressure wave "P" (primary wave)  
gases, liquids, solids  
("BAW" bulk acoustic wave)



Shear wave "S" (secondary wave)  
solids only  
("BAW" bulk acoustic wave)



Surface acoustic wave "SAW"  
surface of solids

Vibrating mode	Frequency [Hz]							Application
	1k	10k	100k	1M	10M	100M	1G	
	Flextural mode							Piezoelectric buzzer
	Length mode							kHz Ceramic filter
	Area expansion mode							kHz Ceramic resonator
	Thickness shear mode							MHz Ceramic filter
	Thickness expansion mode							MHz Ceramic resonator
	Surface Acoustic Wave							SAW filter SAW resonator
	BGS Wave/SH Wave							HF trap HF Ceramic resonator HF Ceramic filter

←→ Vibration Modes

$v \approx 3\text{km/s} \dots 12\text{km/s}$

*Piezoelectric devices*

Melting point  
1670°C

$T < 573^\circ\text{C}$   
 $\alpha$ -quartz  
righthanded  
& lefthanded

$T > 573^\circ\text{C}$   
 $\beta$ -quartz

Mechanical  
 $Q > 10^6$

Piezoelectric



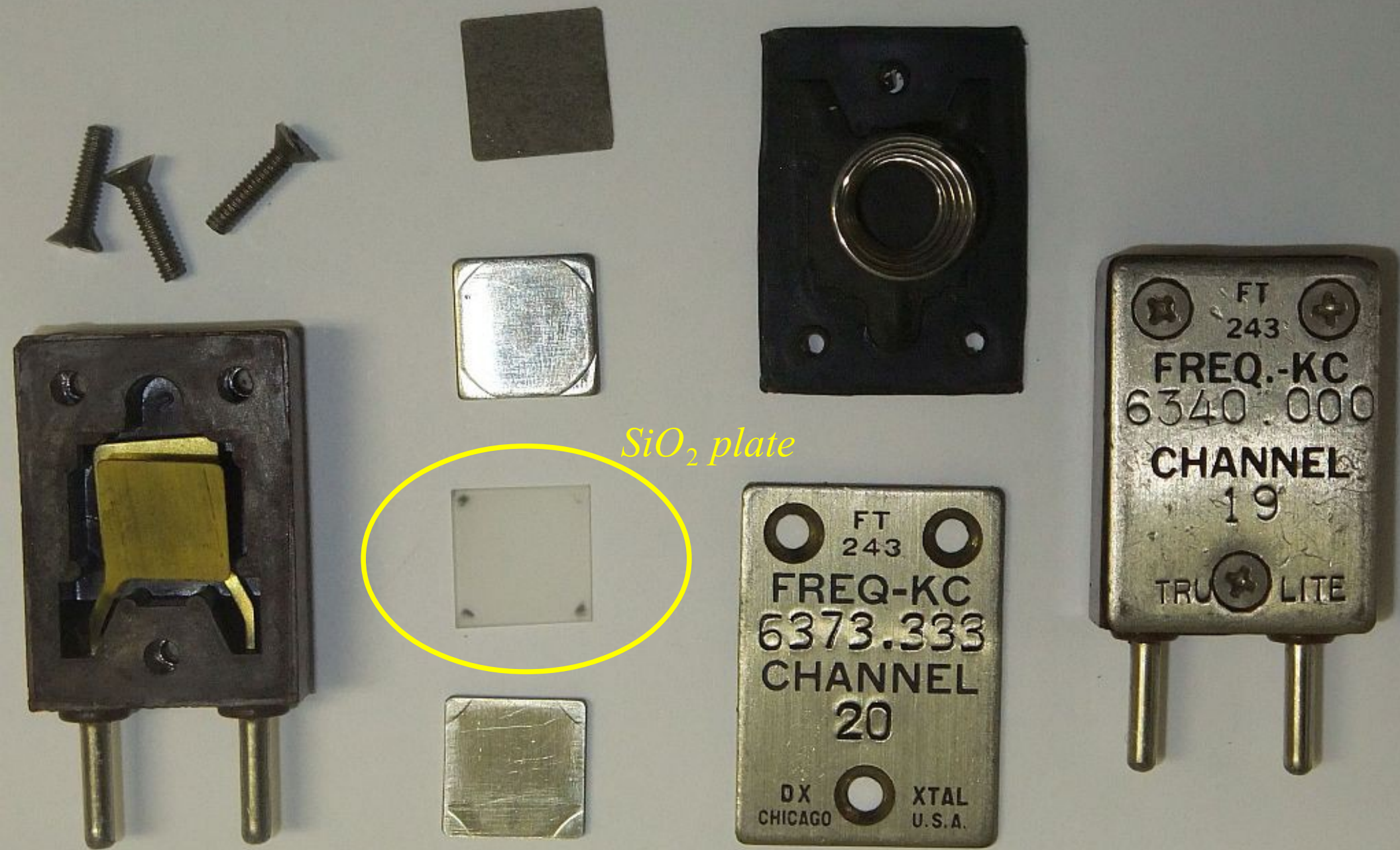
Hydrothermal growth in  $\text{H}_2\text{O} + \text{NaCl}$  (~1000 years)  $p \approx 1000\text{bar}$

Both  $\alpha$  forms present: righthanded & lefthanded (twinning)?

Impurities? Inclusions? Availability?

*Natural quartz crystal*





*Historical quartz resonator FT243*

# Hydrothermal growth

$$v_{\text{growth}}(z) \approx 3 \cdot v_{\text{growth}}(x)$$

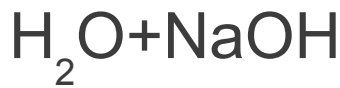
righthanded  $\alpha$ -quartz



$p \approx 700 \dots 1000 \text{ bar}$

$T \approx 345^\circ\text{C}$   $\Delta T \approx 10^\circ\text{C}$

$$v_{\text{growth}}(z) \approx 0.4 \text{ mm/day}$$

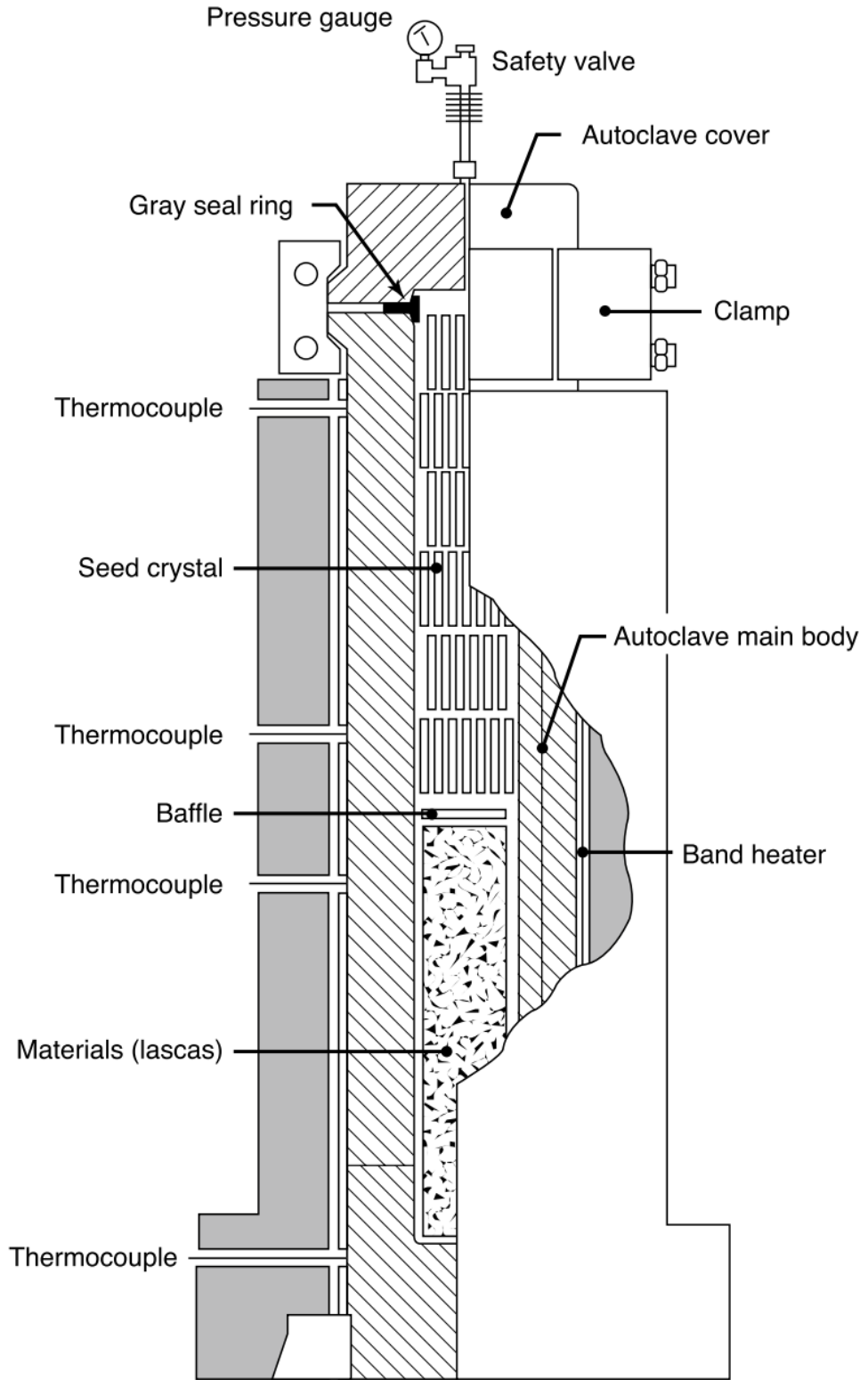


$p \approx 1000 \dots 1500 \text{ bar}$

$T \approx 380^\circ\text{C}$   $\Delta T \approx 25^\circ\text{C}$

$$v_{\text{growth}}(z) \approx 1 \text{ mm/day}$$

*Hydrothermal  
growth oven*





$\text{SiO}_2$   
 $m = 1.67\text{kg}$

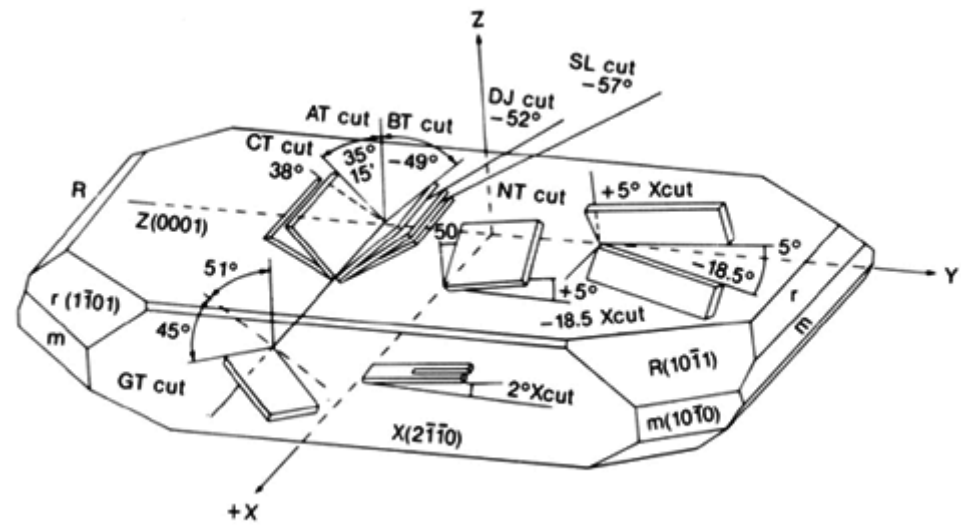
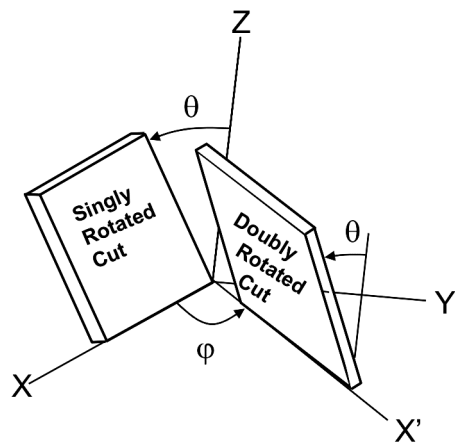
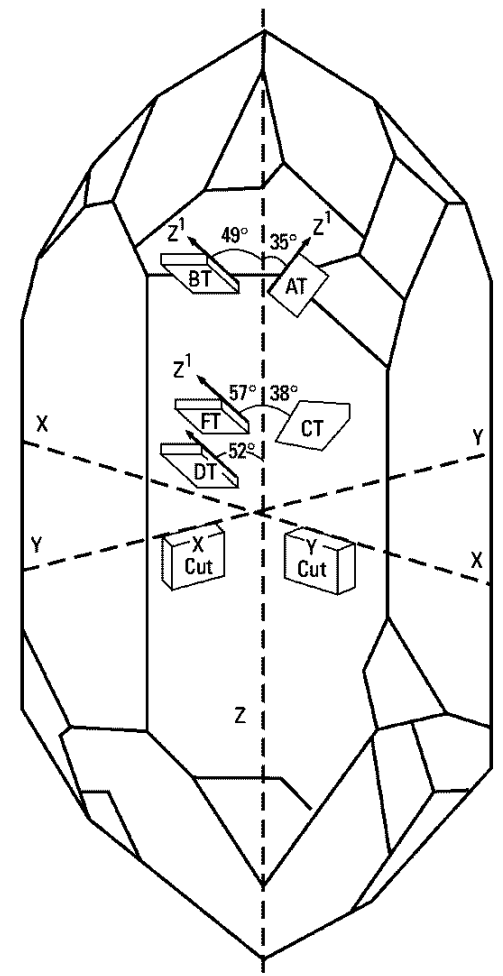
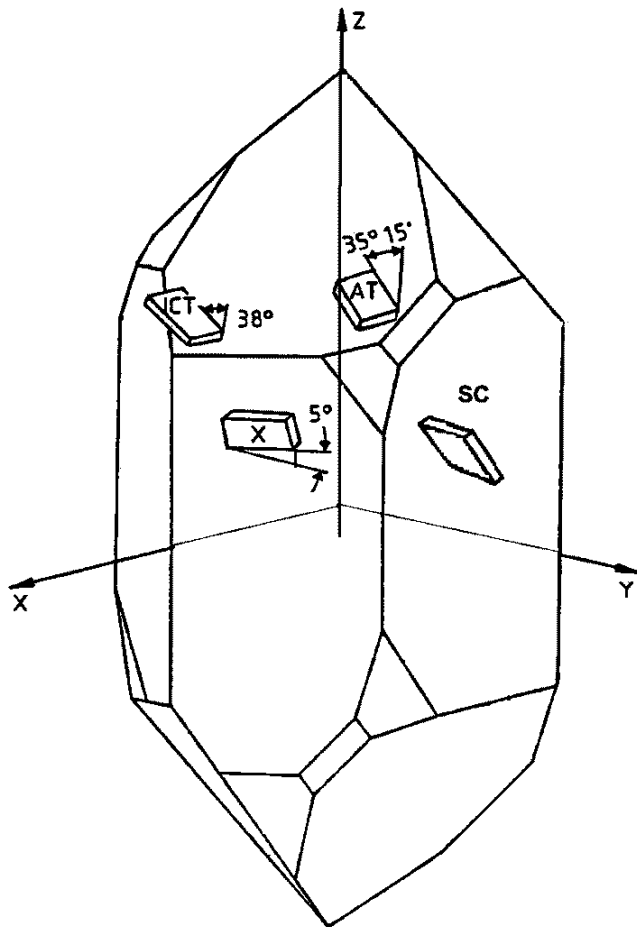
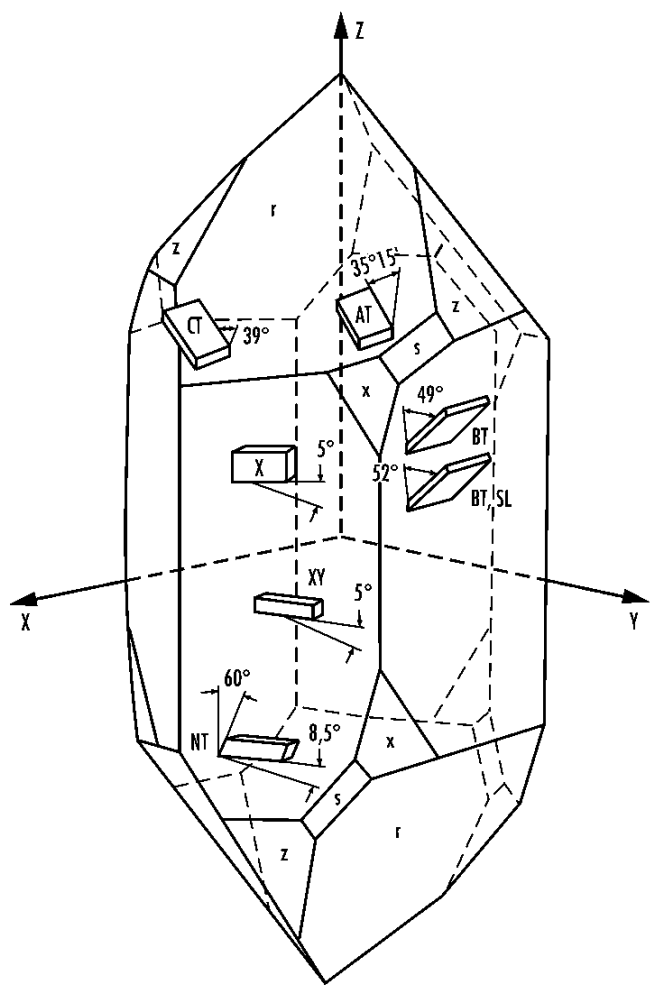


Seed  
attachment

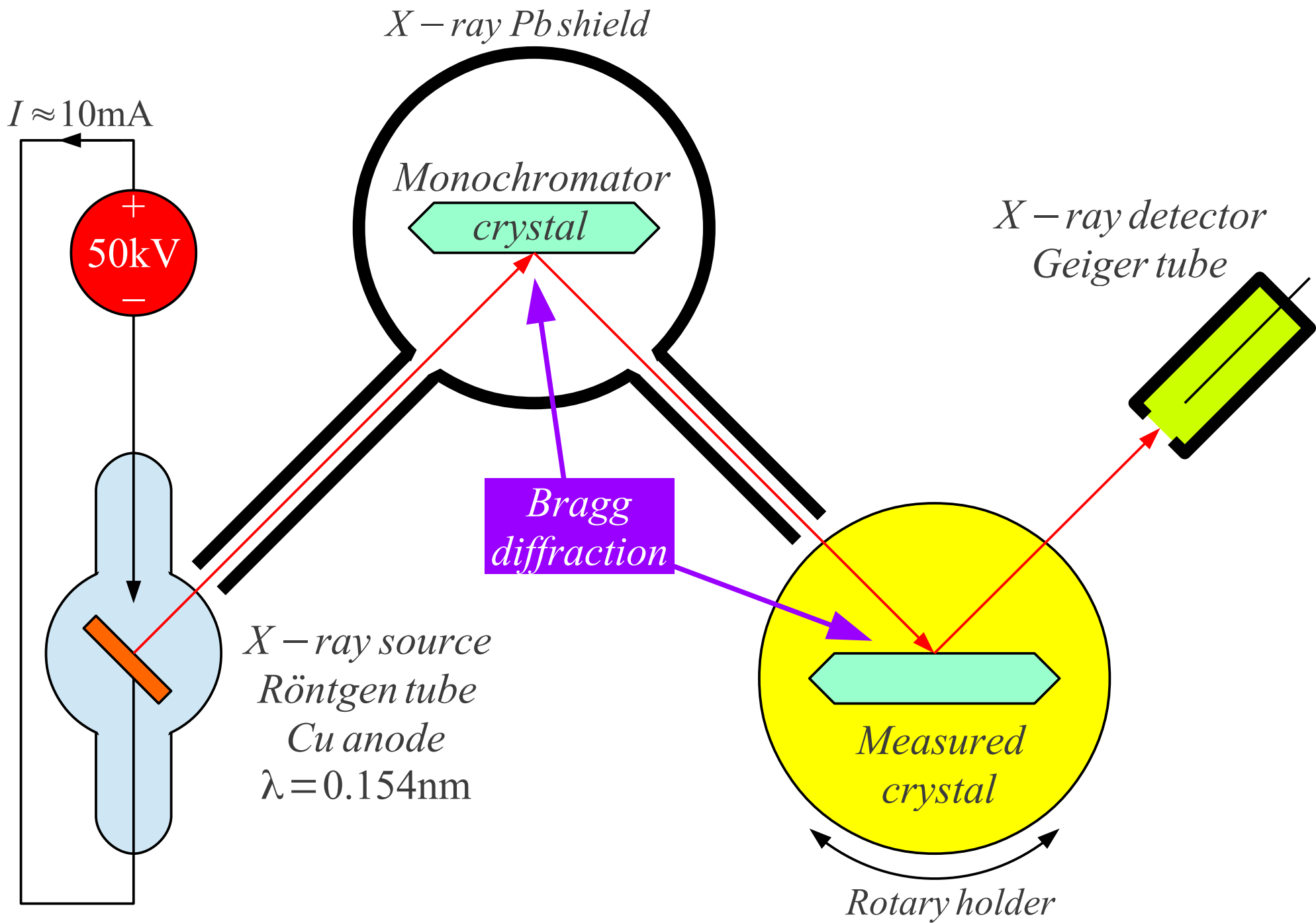


*Artificial quartz crystal*

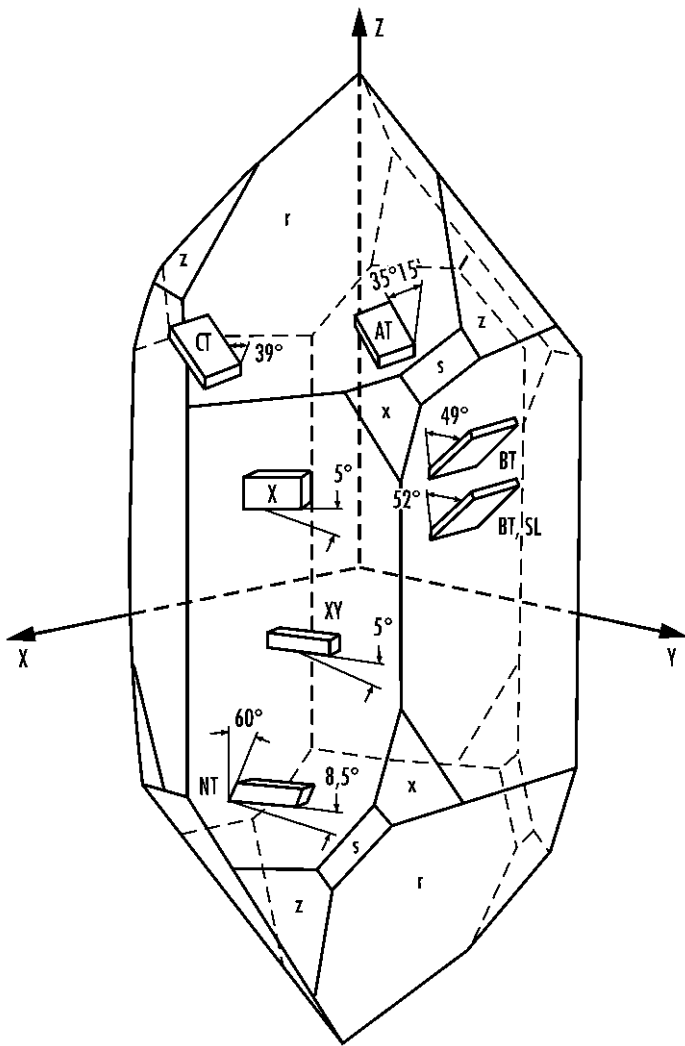


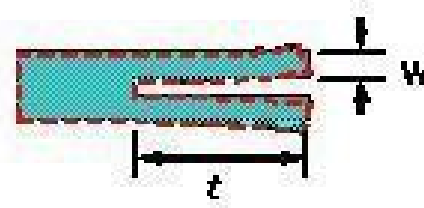
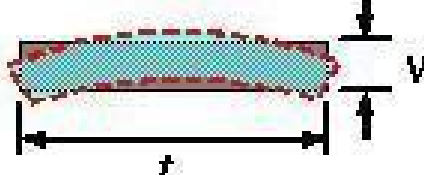
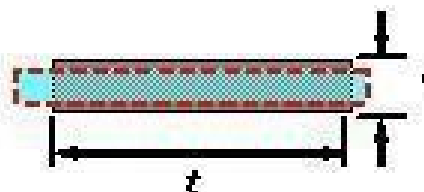
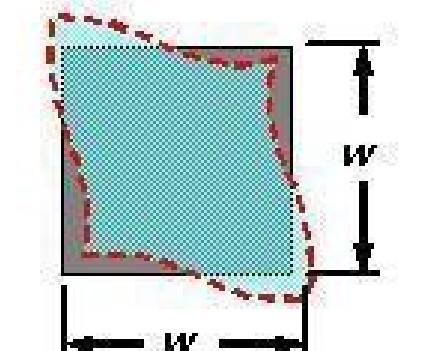
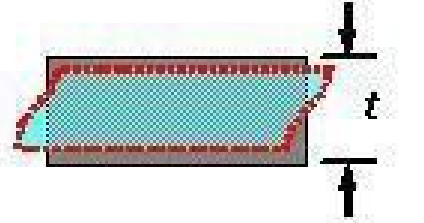


*Quartz – crystal cuts*



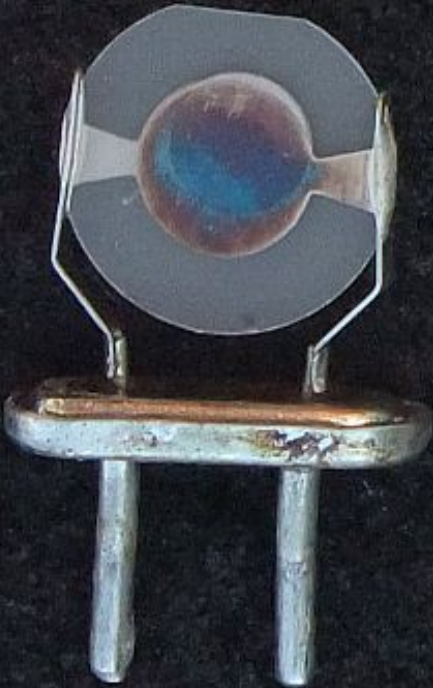
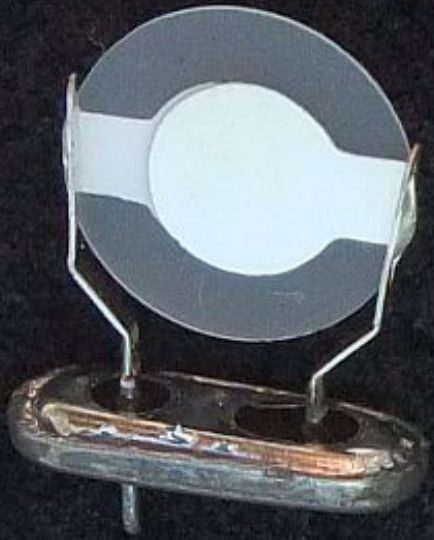
*Finding the crystal axes with X rays*



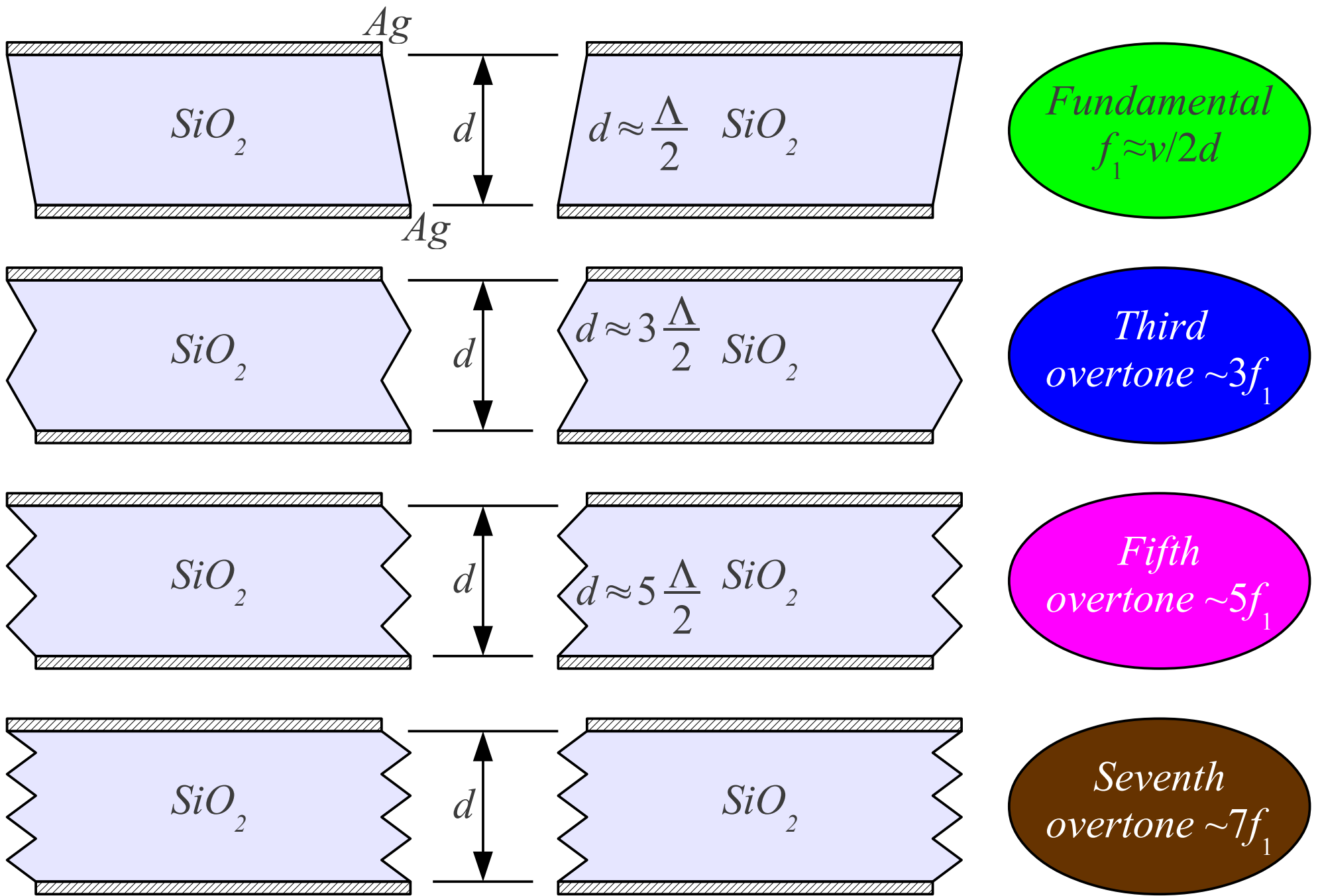
	Vibration Mode	Orientation Angle
Tuning Fork		+ 2° X
Flexure		XY NT
Extension		+ 5° X - 18.5° X
Face Shear		DT CT SL
Thickness Shear		AT Fundamental AT 3 <sup>rd</sup> Overtone AT 5 <sup>th</sup> Overtone BT Fundamental

*Oscillation modes*

*AT plates*

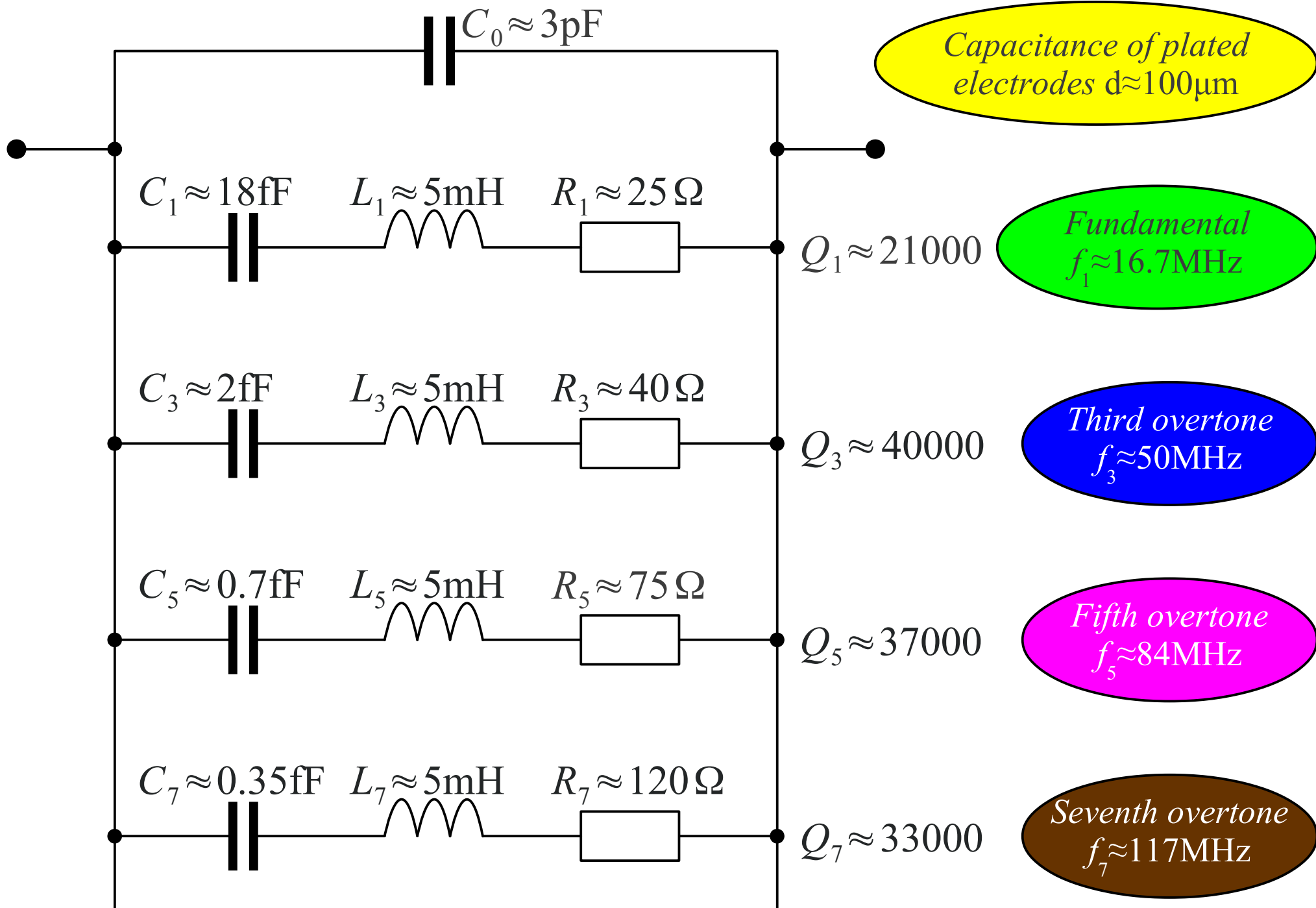






*AT – plate shear oscillation modes*





*AT – plate equivalent electric circuit*

$B = \text{Im}[Y]$

$Y(f) = G + jB$

$j\omega C_0$

Seventh  
overtone

$1/R_7$

$1/R_5$

$1/R_3$

$1/R_1$

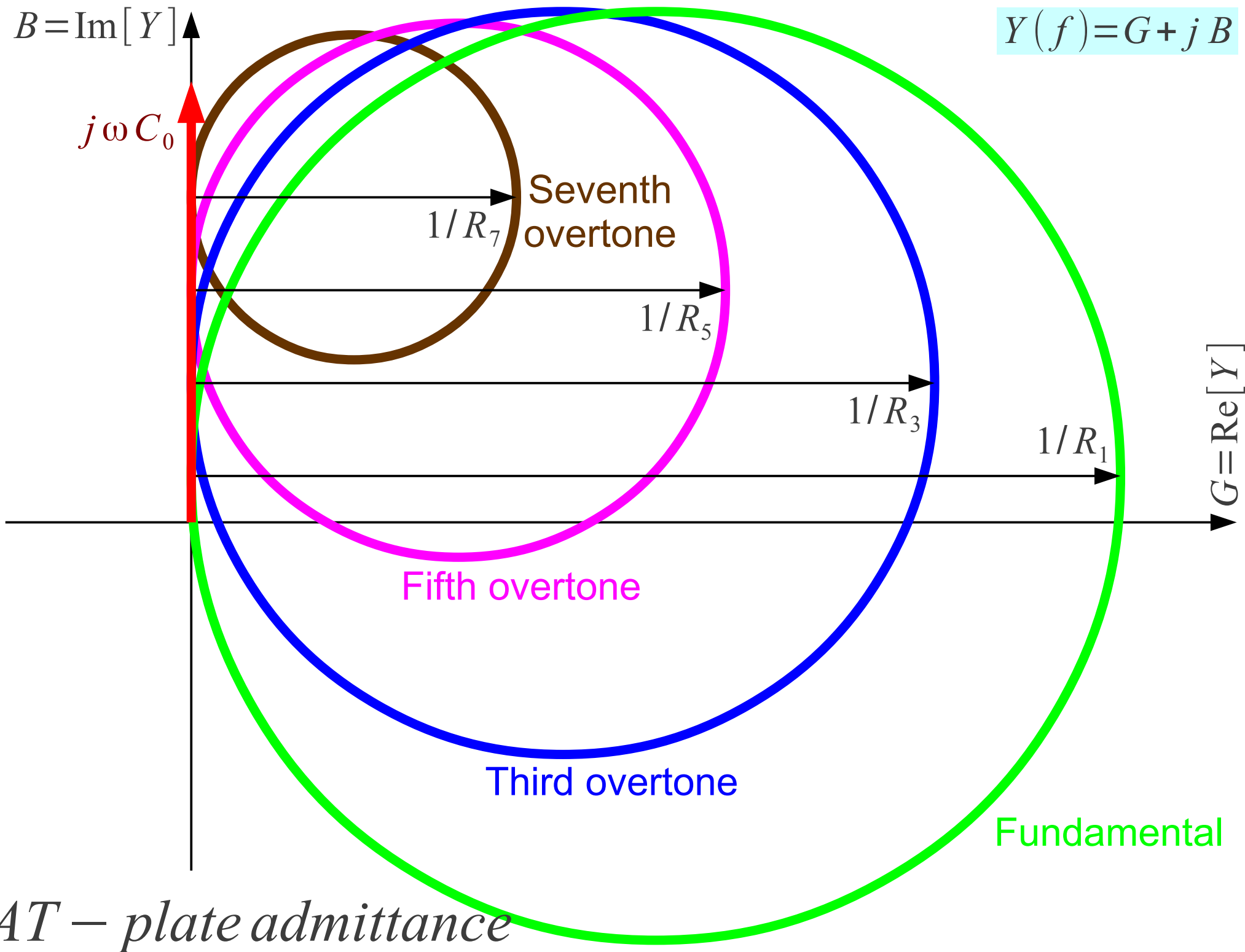
$G = \text{Re}[Y]$

Fifth overtone

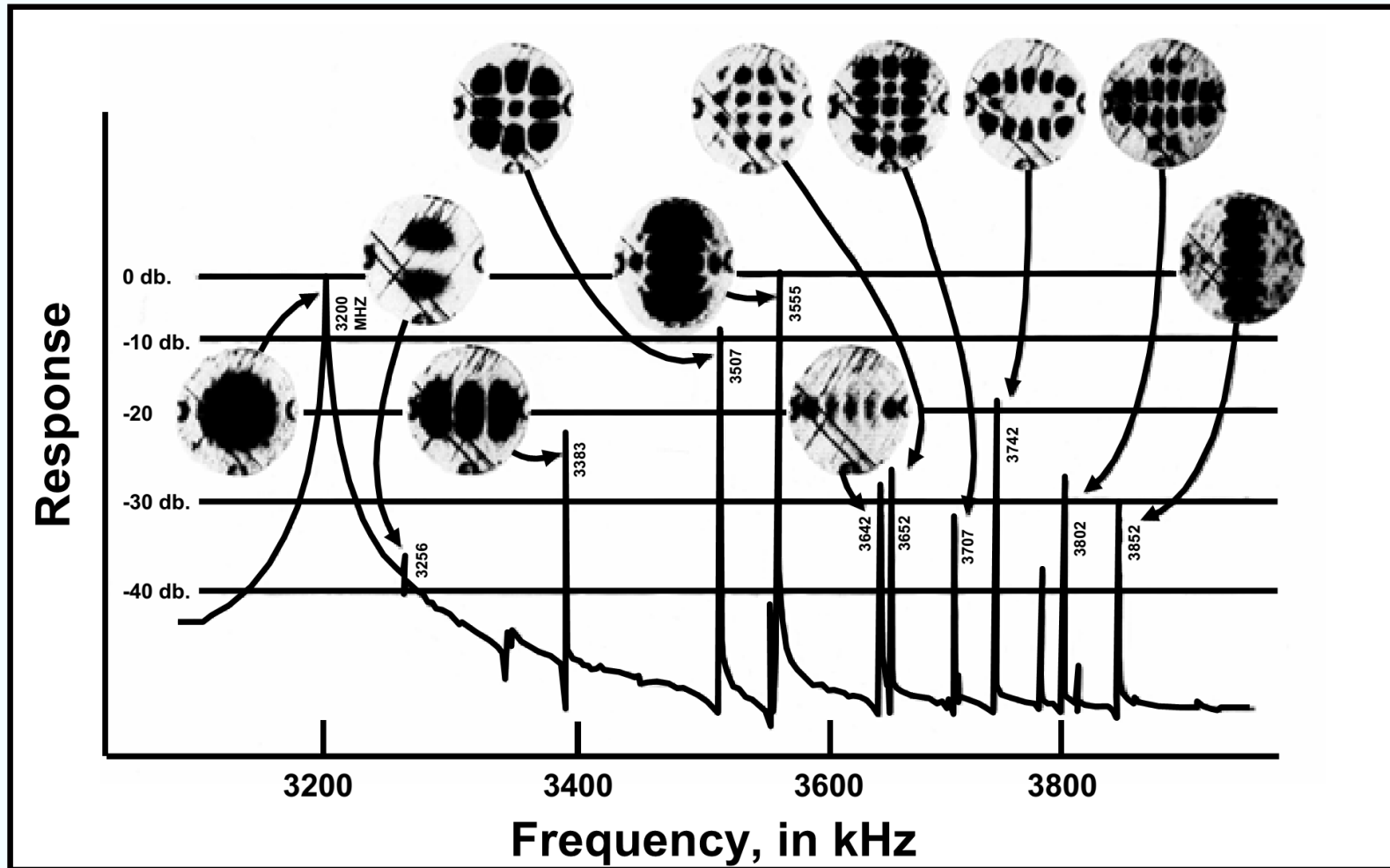
Third overtone

Fundamental

*AT* – plate admittance

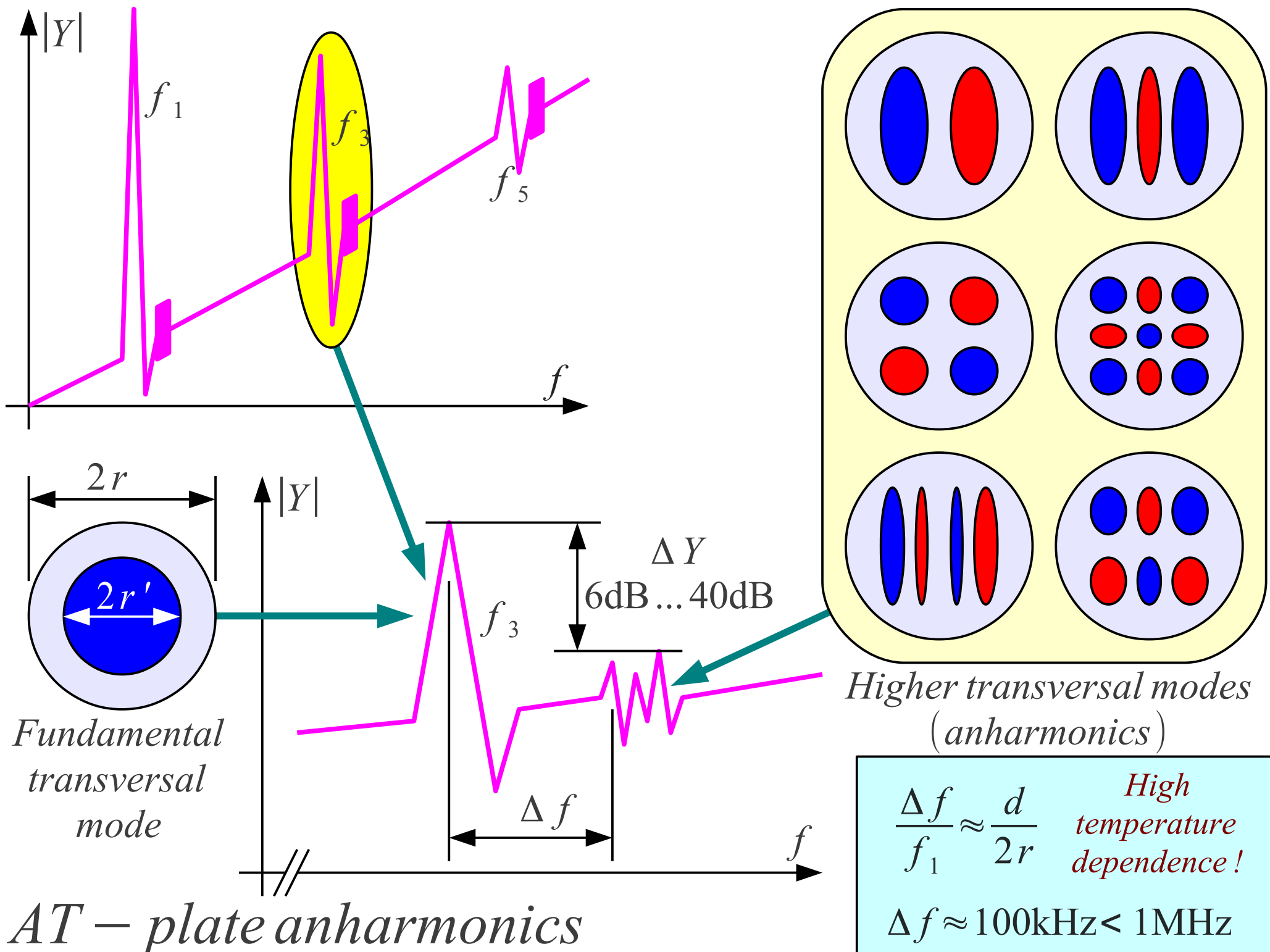


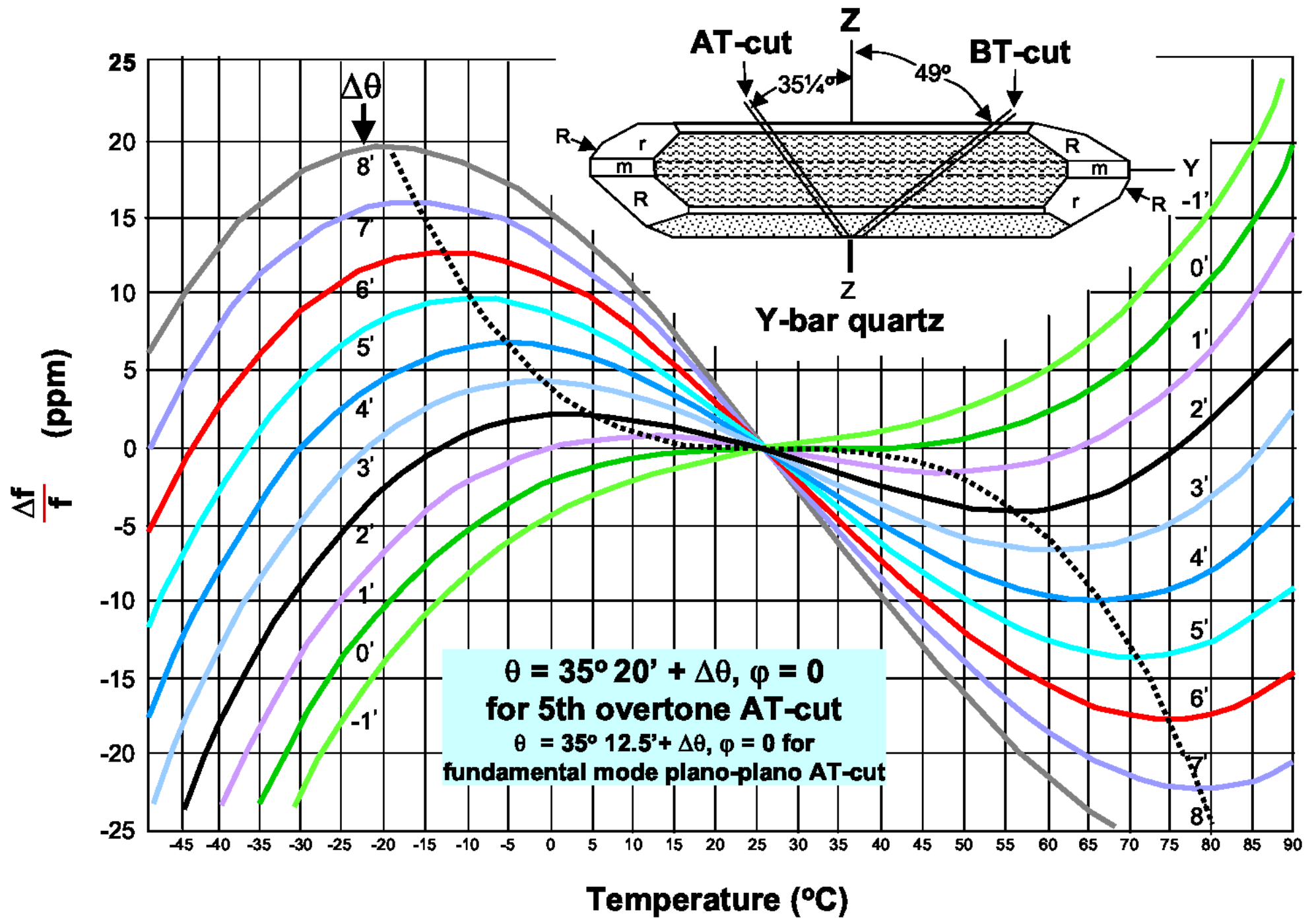
# Resonant Vibrations of a Quartz Plate



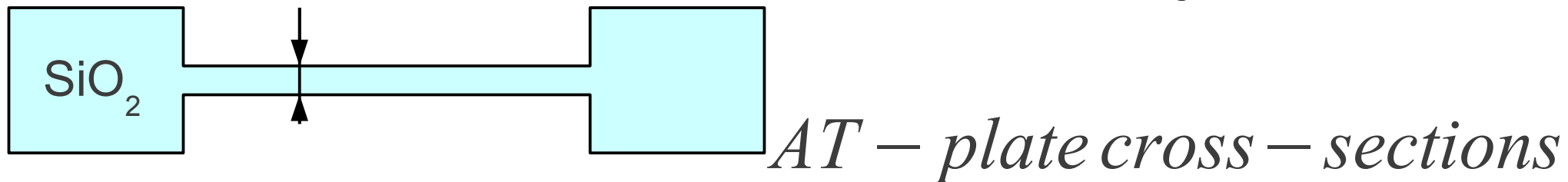
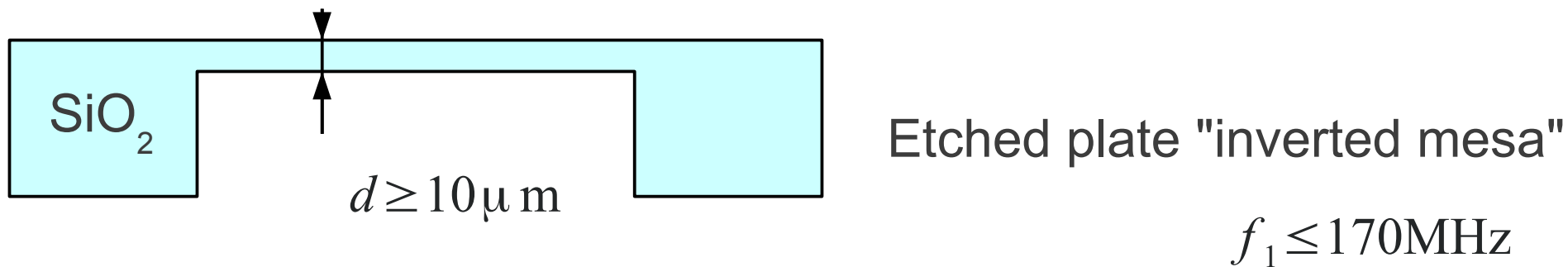
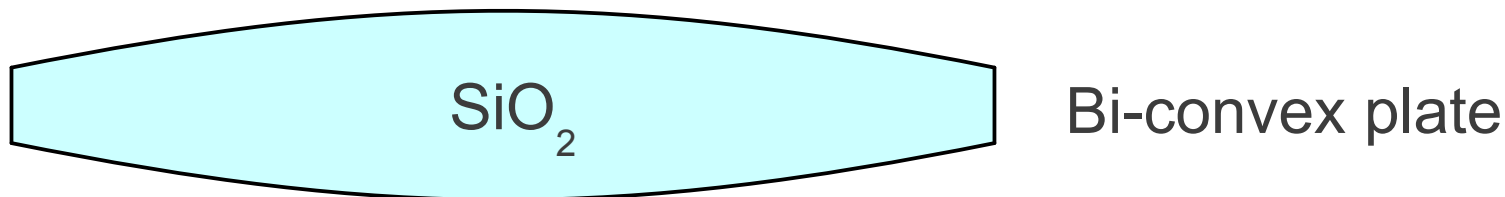
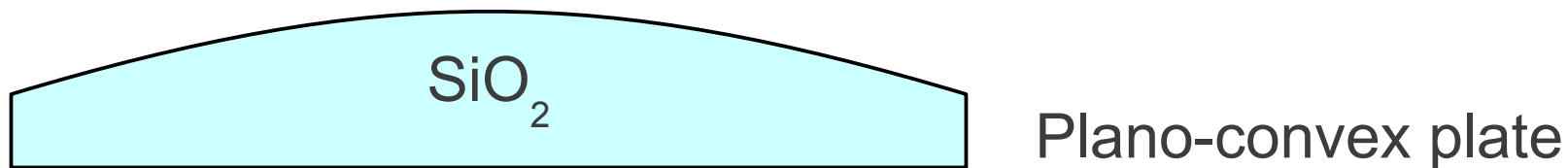
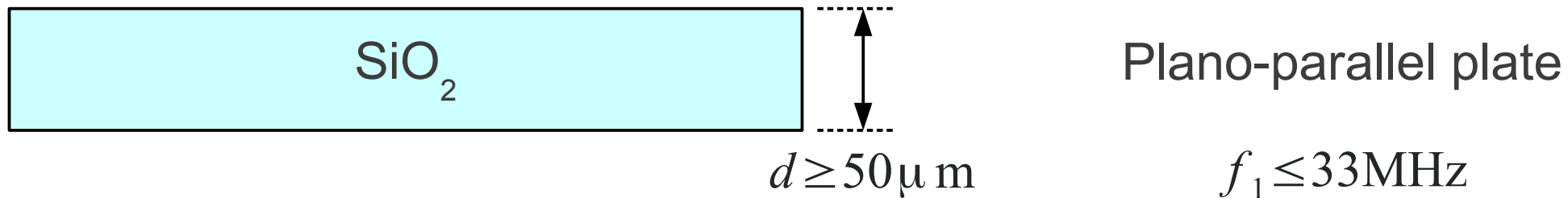
X-ray topographs ( $21\cdot\bar{0}$  plane) of various modes excited during a frequency scan of a fundamental mode, circular, AT-cut resonator. The first peak, at 3.2 MHz, is the main mode; all others are unwanted modes. Dark areas correspond to high amplitudes of displacement.

*AT – plate oscillation modes (anharmonics)*



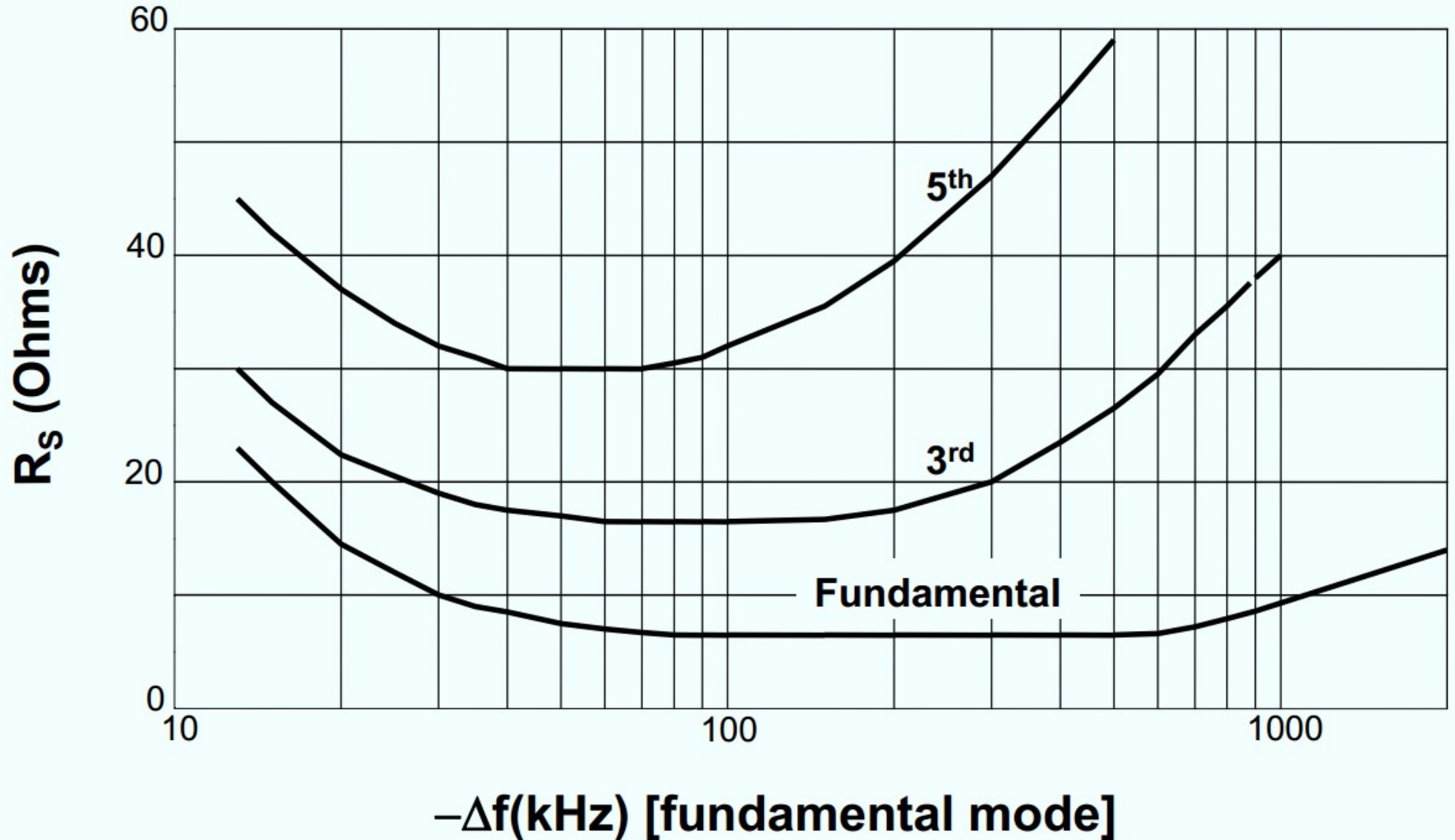


*AT – plate temperature dependence*



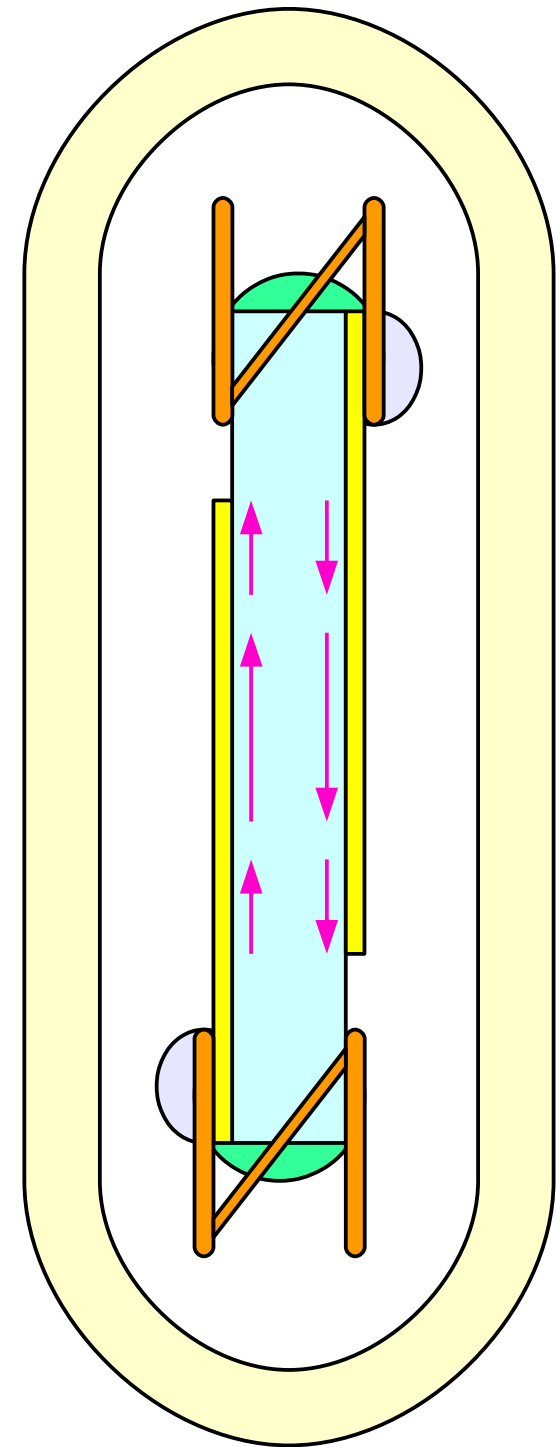
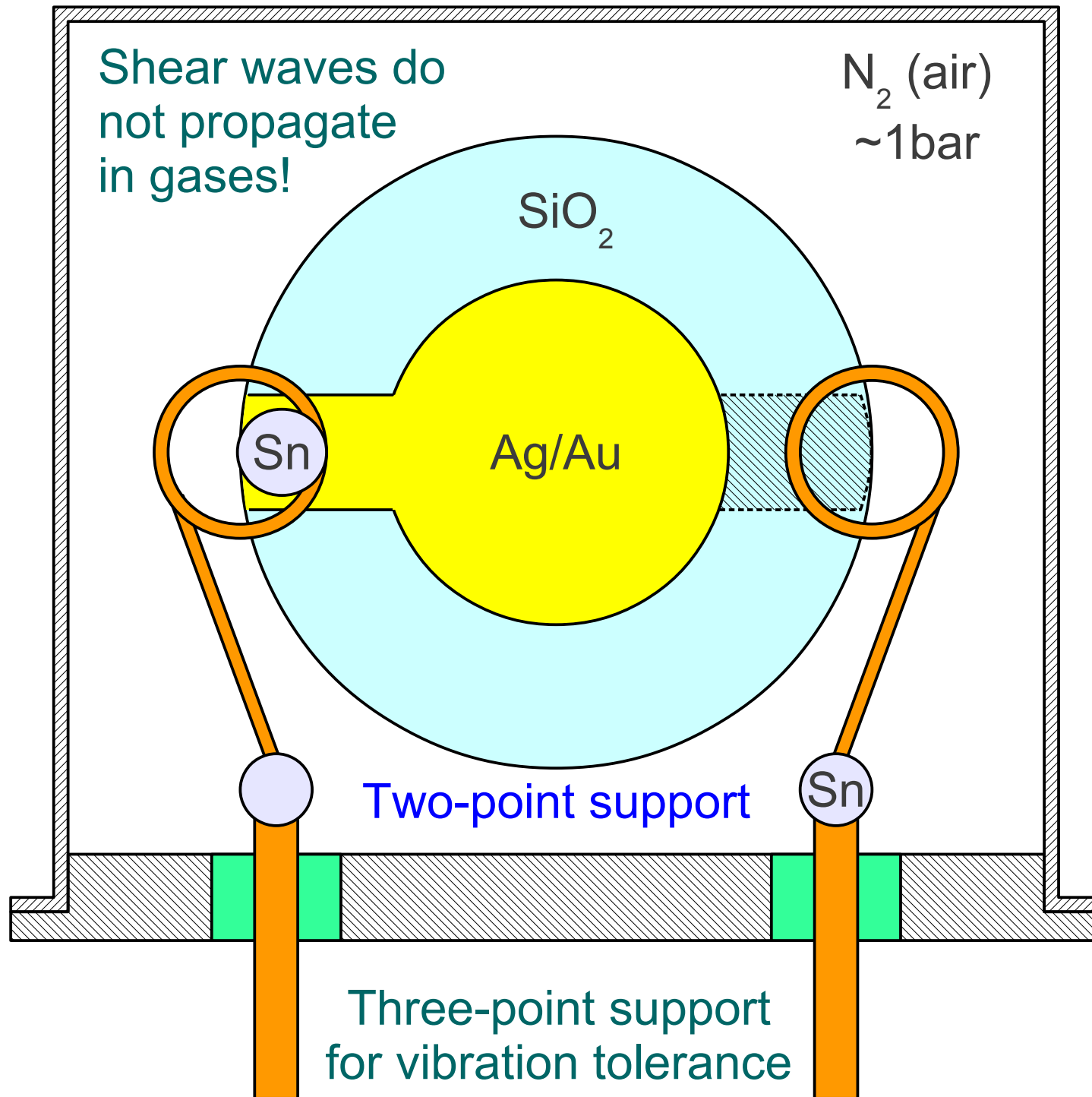
# Resistance vs. Electrode Thickness

AT-cut;  $f_1=12$  MHz; polished surfaces; evaporated 1.2 cm (0.490") diameter silver electrodes

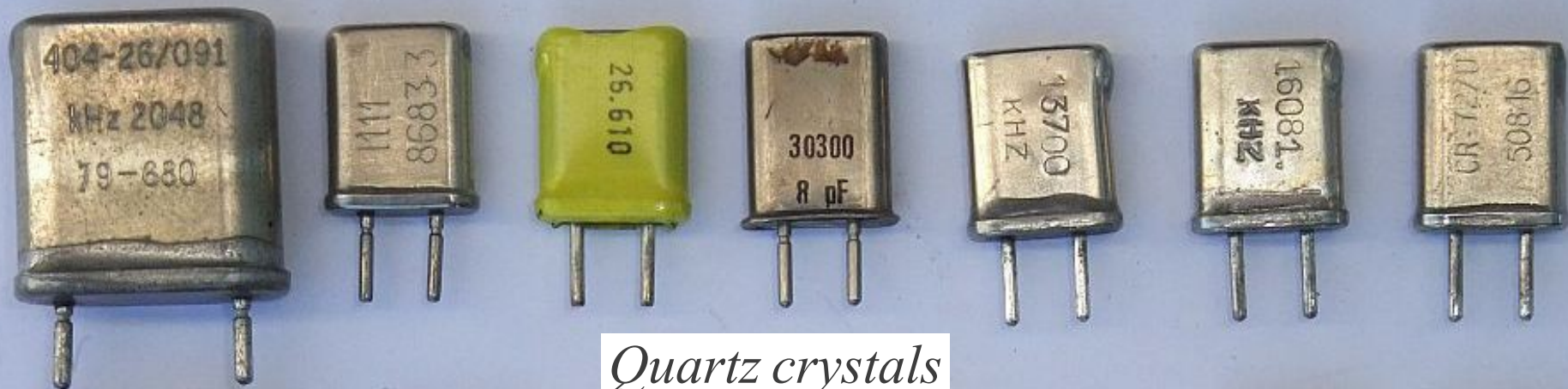


*Effects of plated electrodes*

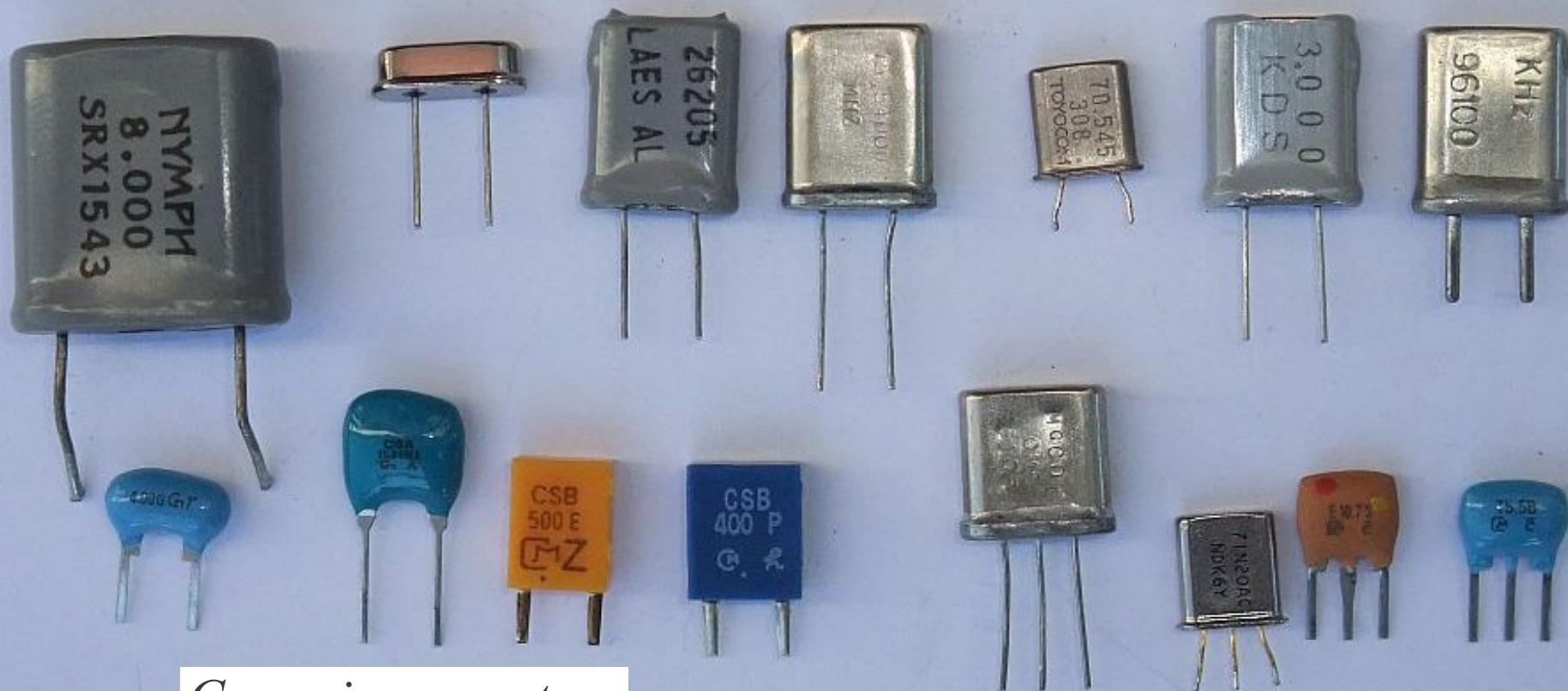
# AT – plate housing







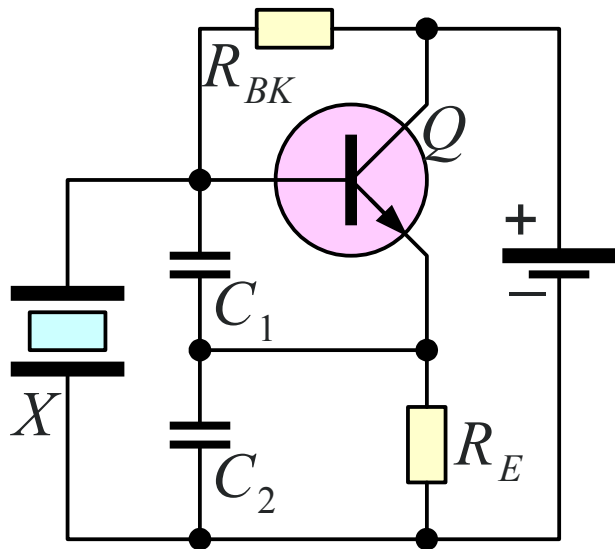
*Quartz crystals*



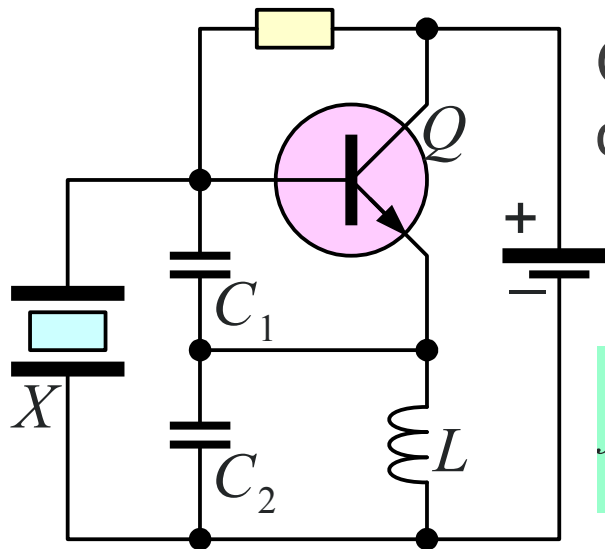
*Ceramic resonators*

*Multiple resonators*

*Piezoelectric – resonator housings*

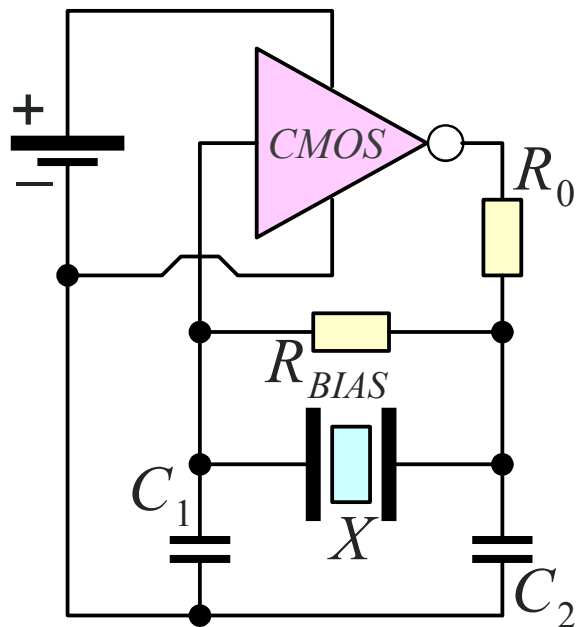


Fundamental  $f_1$   
Pierce (Colpitts)

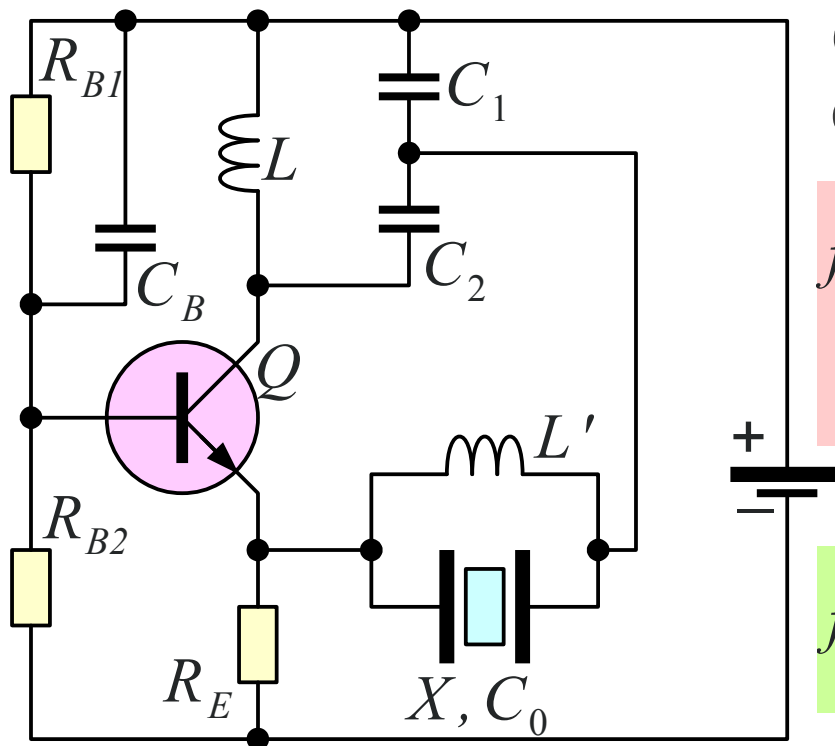


Overtone  
oscillator  $f_3$

$$f_1 < \frac{1}{2\pi\sqrt{LC_2}} < f_3$$



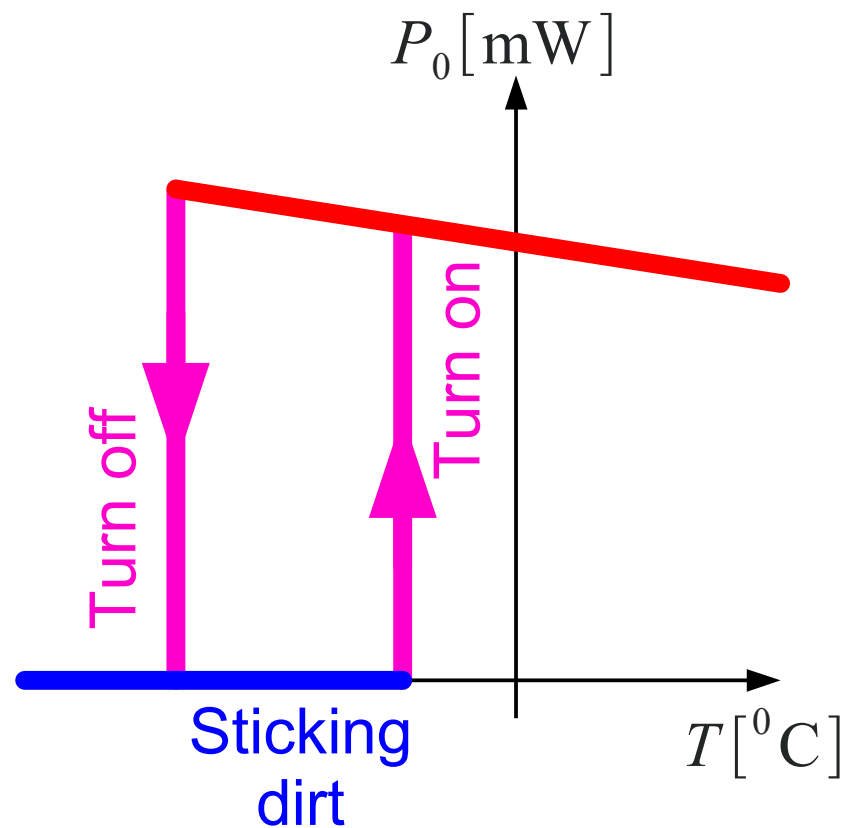
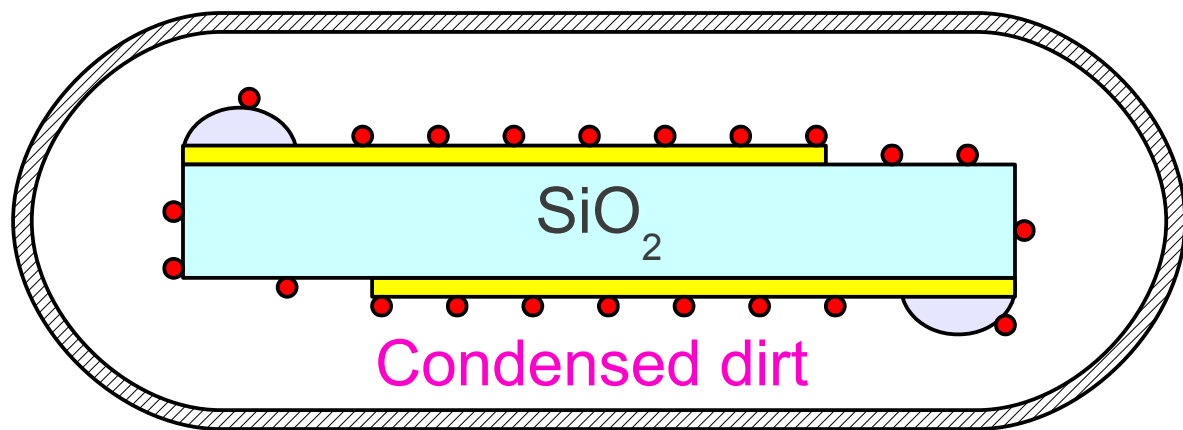
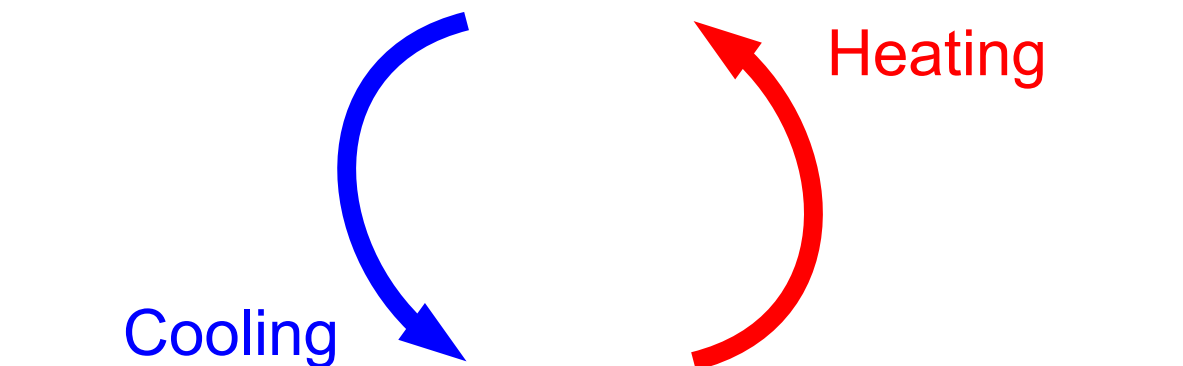
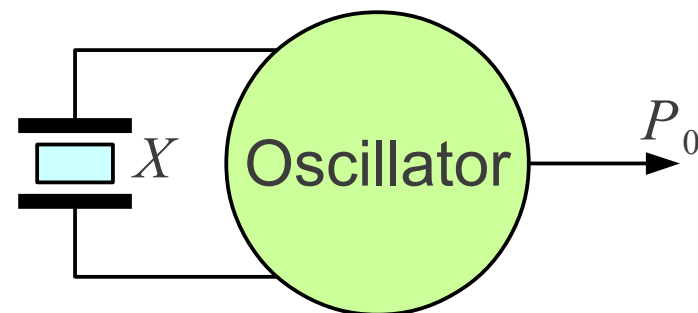
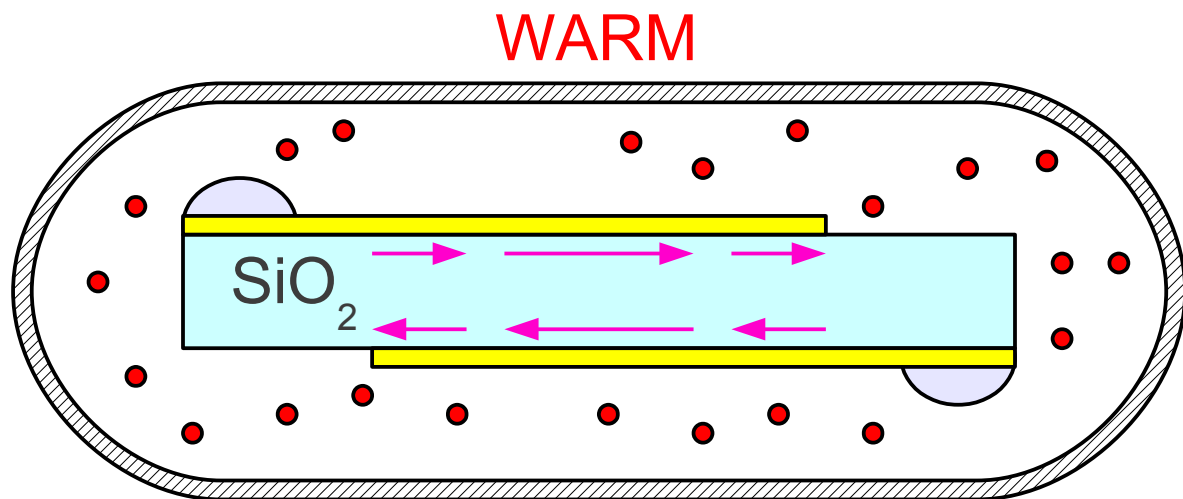
*Crystal oscillators*



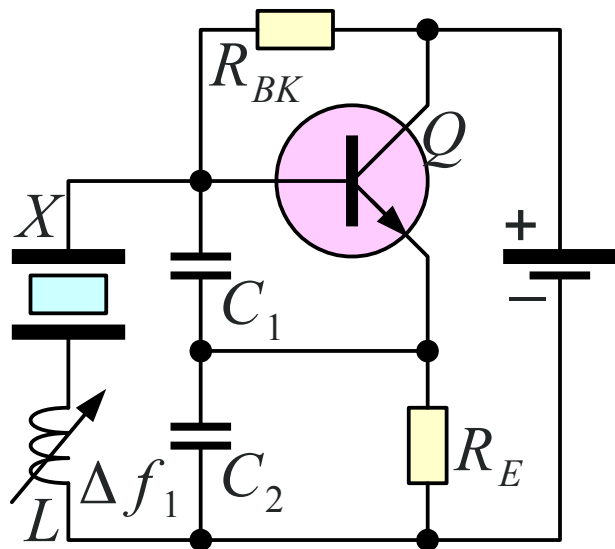
Overtone  
oscillator  $f_5$

$$f_5 = \frac{1}{2\pi\sqrt{L\frac{C_1C_2}{C_1+C_2}}}$$

$$f_5 = \frac{1}{2\pi\sqrt{L'C_0}}$$

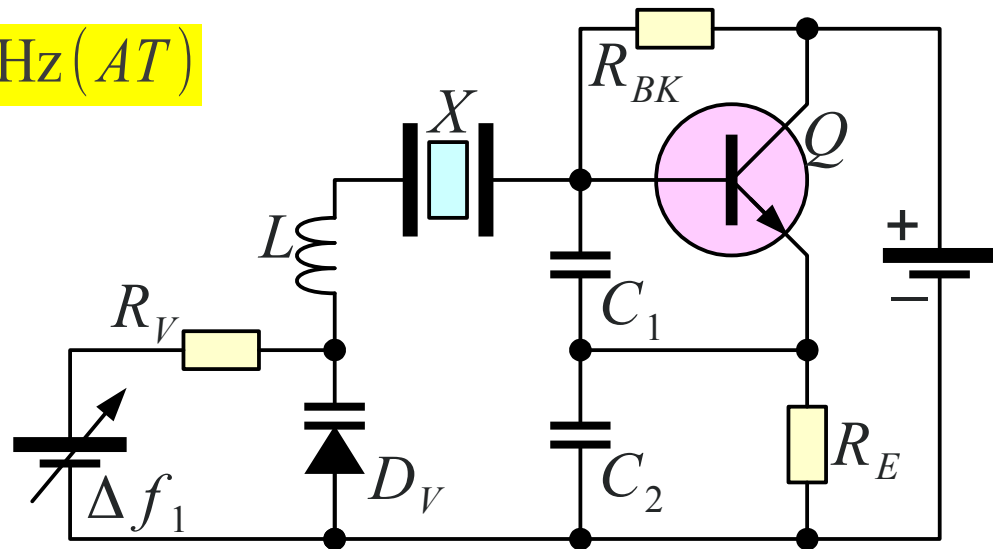


*Sticking – dirt hysteresis*

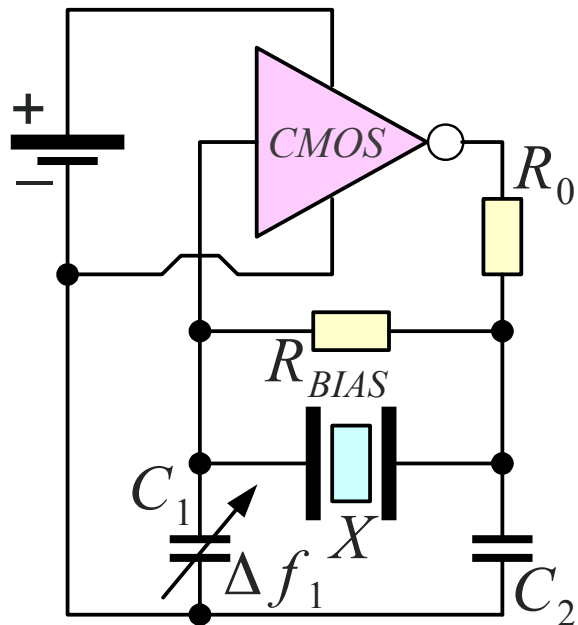


Adjustable crystal oscillator VXO

$f_1 \approx 10 \dots 20 \text{ MHz (AT)}$

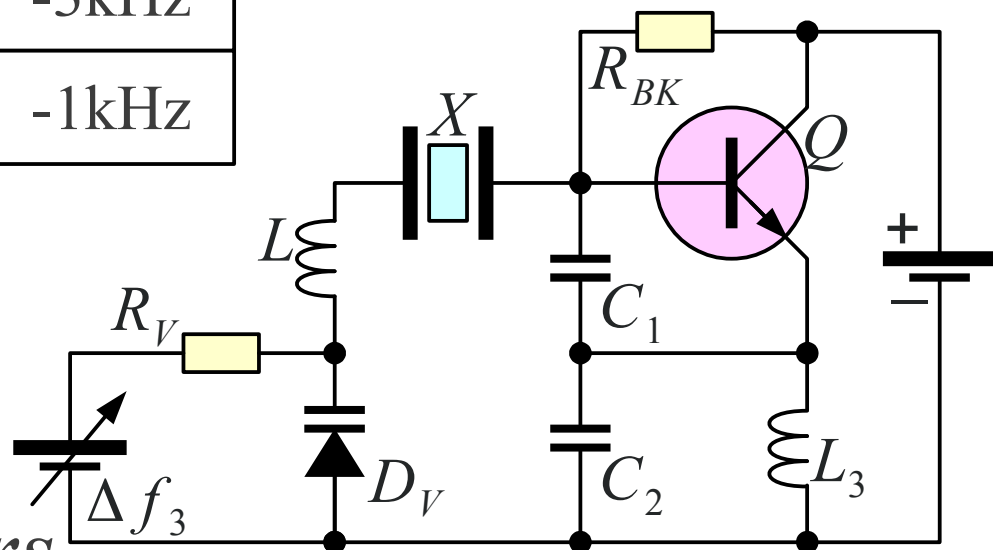


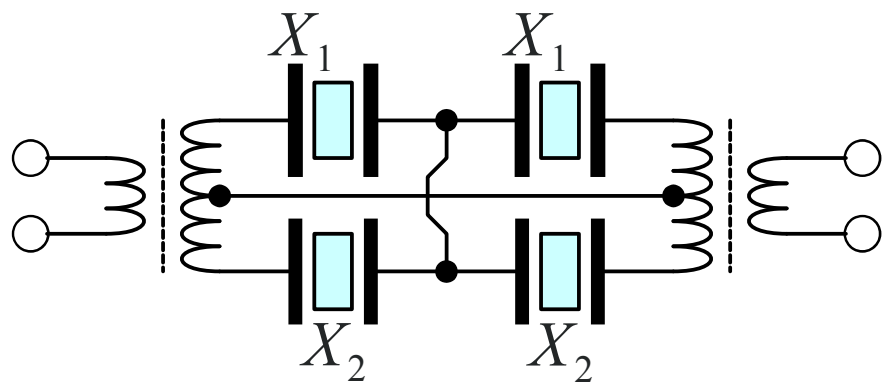
Voltage-adjustable crystal oscillator VCXO (temp. comp. TCXO)



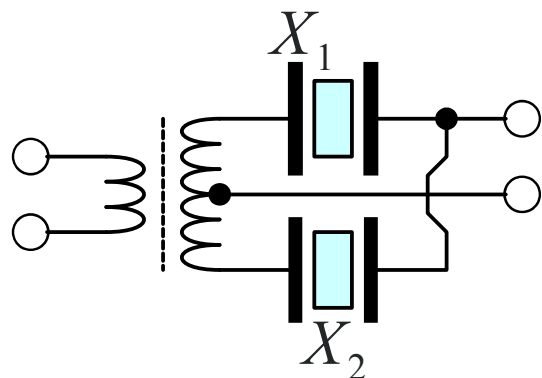
Adjustable crystal oscillators

	$C$	$L$
$\Delta f_1$	+10kHz	-30kHz
$\Delta f_3$	+1kHz	-3kHz
$\Delta f_5$	+300Hz	-1kHz

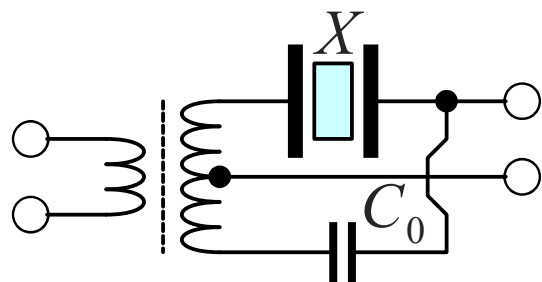




Double-bridge BPF

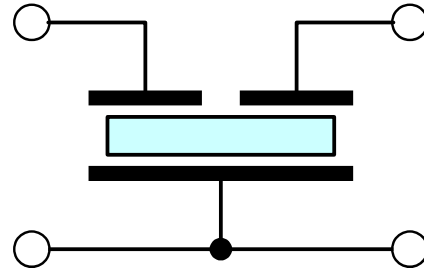


Bridge BPF

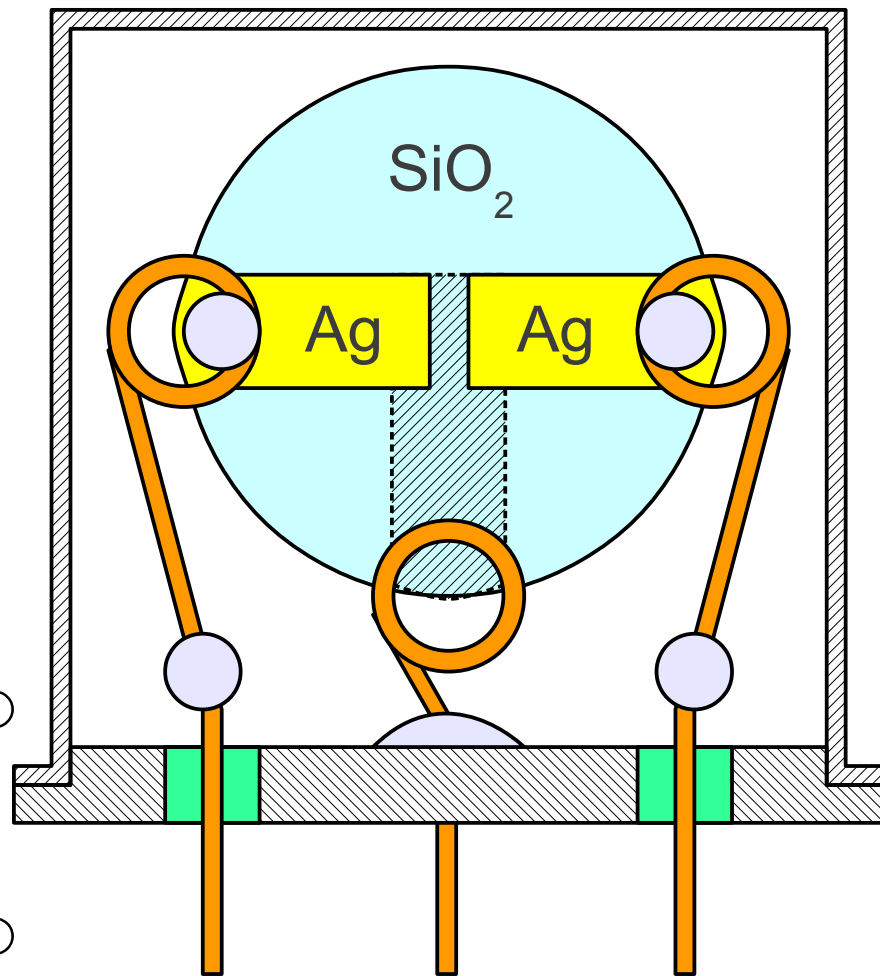


Simple BPF

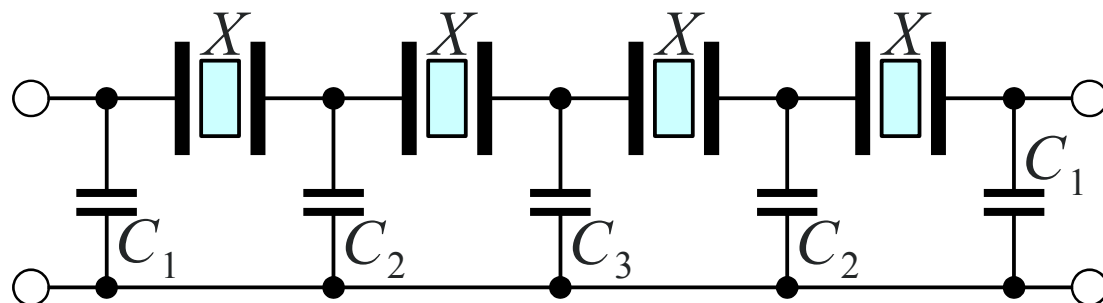
*Crystal bandpass filters*



Monolithic BPF

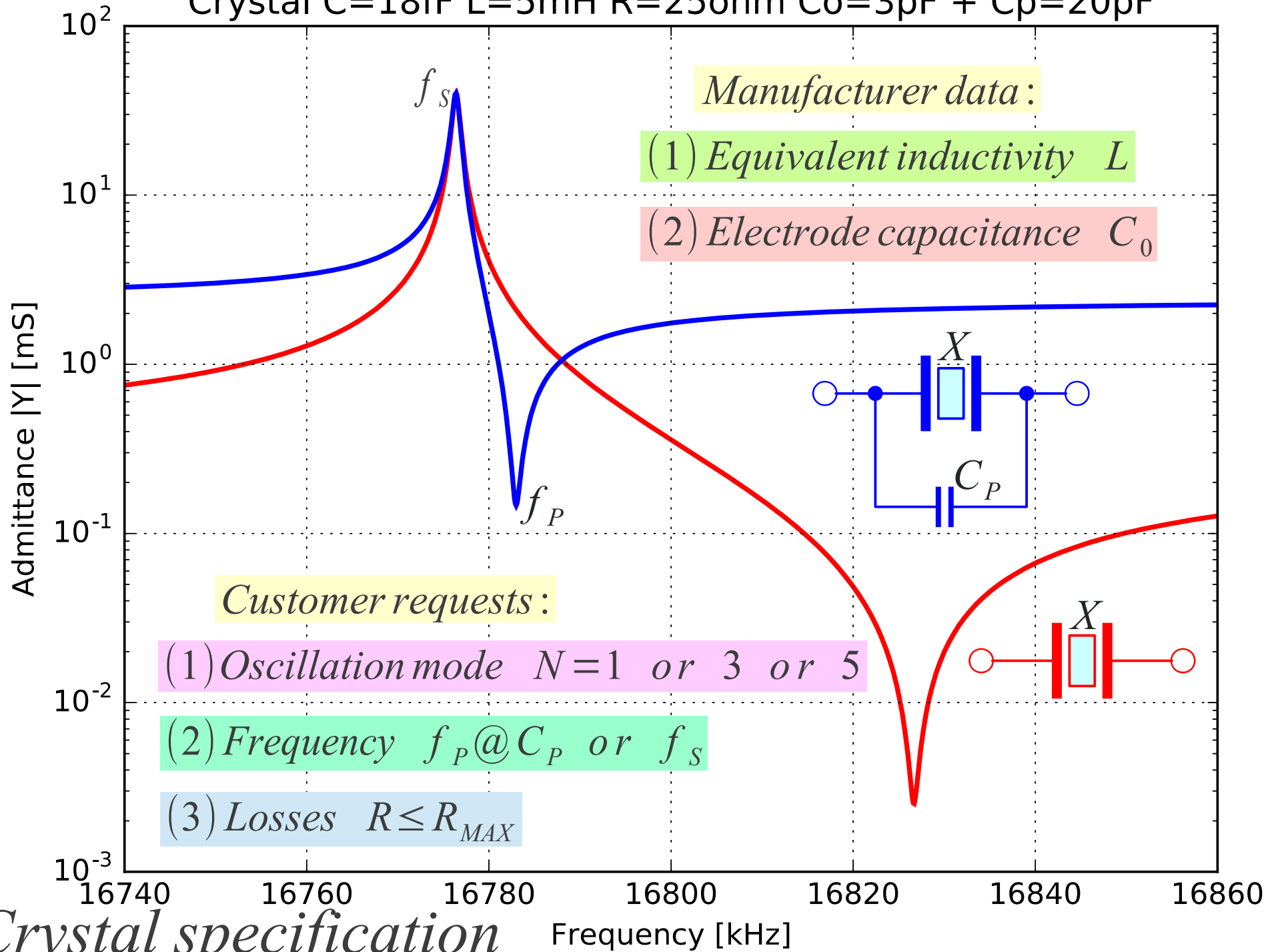


$$200\text{Hz} \leq B \leq 50\text{kHz}$$

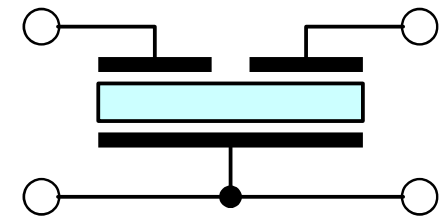
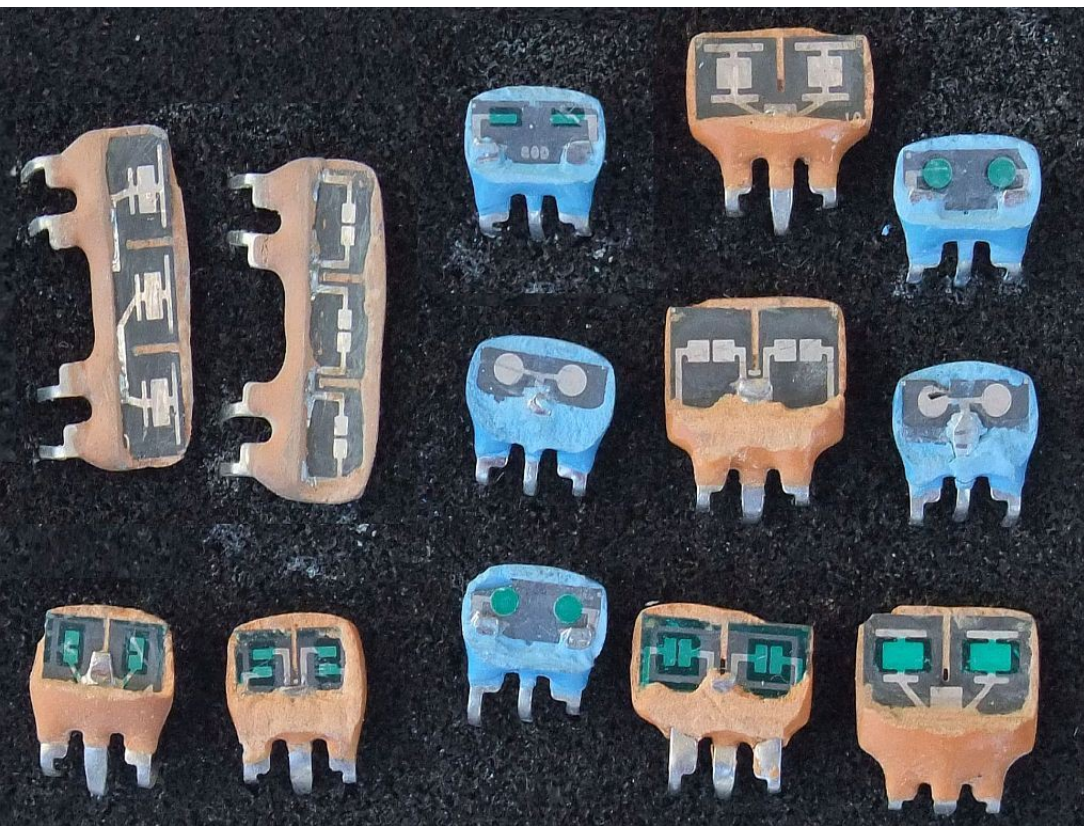
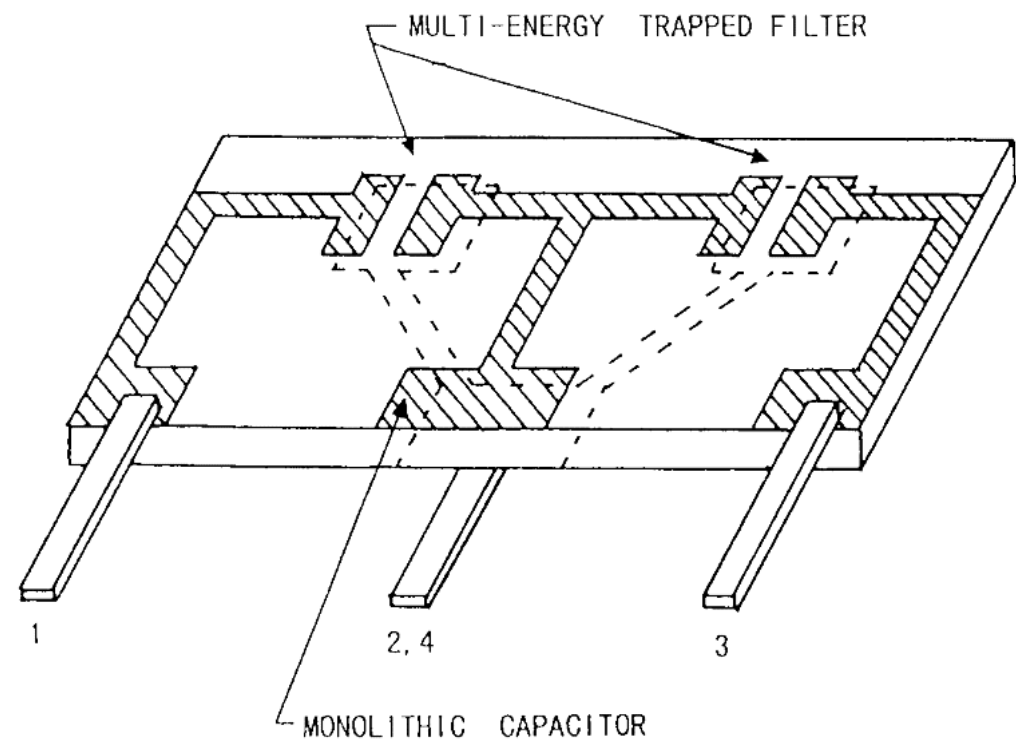
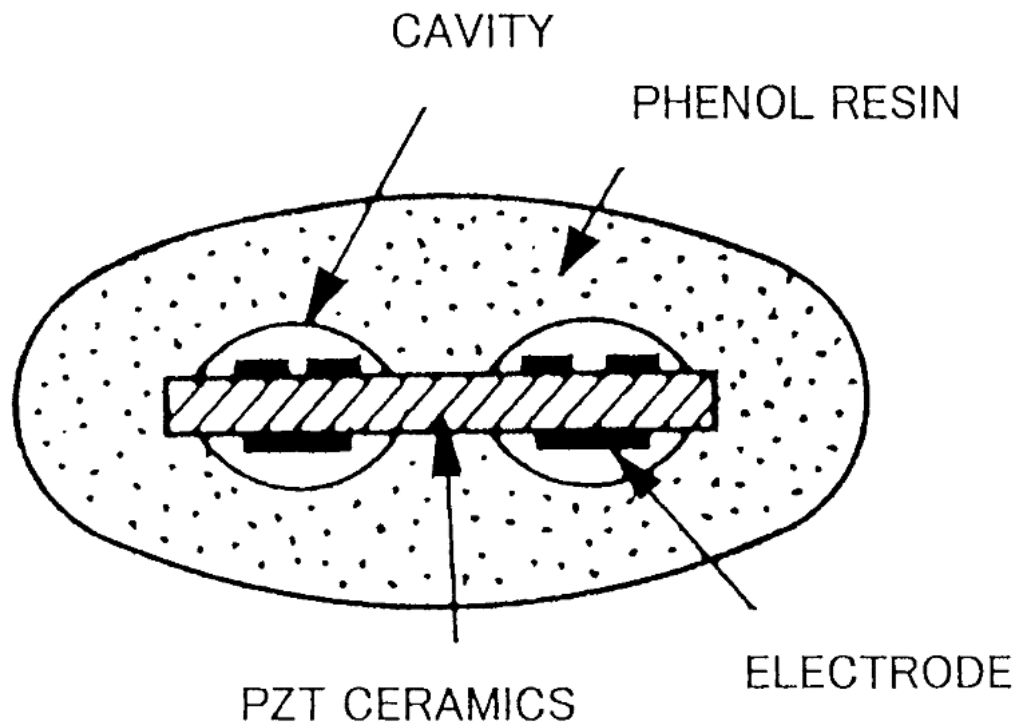


Ladder BPF

Crystal  $C=18\text{fF}$   $L=5\text{mH}$   $R=25\text{ohm}$   $C_0=3\text{pF}$  +  $C_p=20\text{pF}$







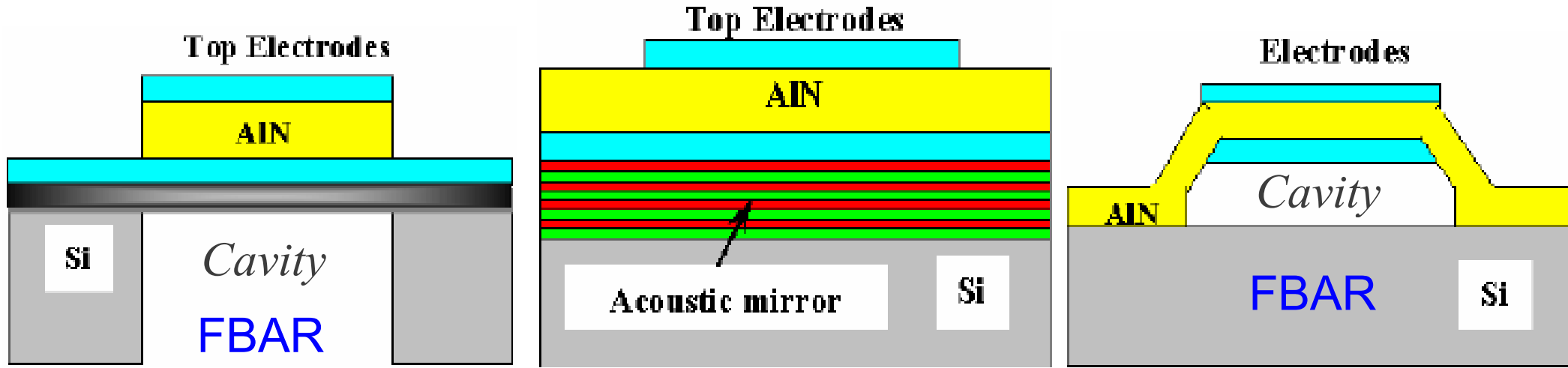
$$v \approx 3\text{km/s} \dots 4\text{km/s}$$

$$Q \approx 1000 \quad @f = 10\text{MHz}$$

*Piezoceramics*

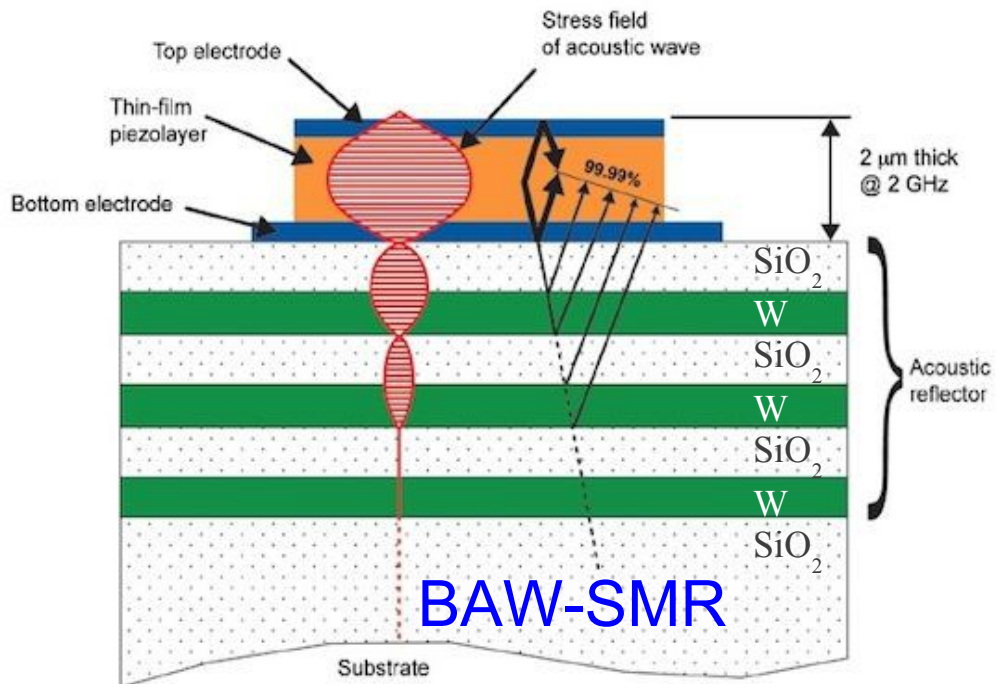
# Film Bulk Acoustic Resonator (FBAR)

$Q \approx 2000$  @  $f = 2\text{GHz}$



**BAW-SMR**

$v \approx 6\text{km/s} \dots 11\text{km/s}$  pressure wave  $P$

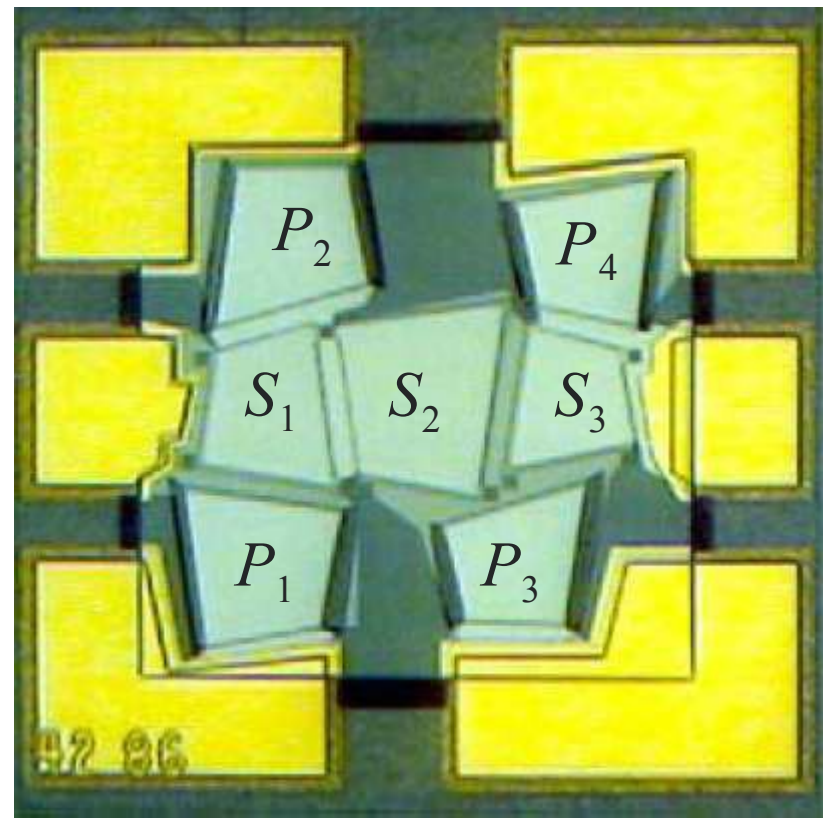
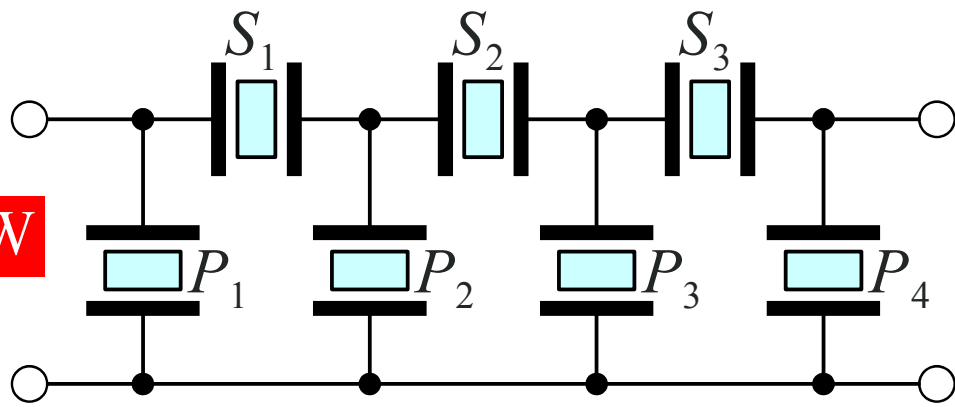


**BAW-SMR**

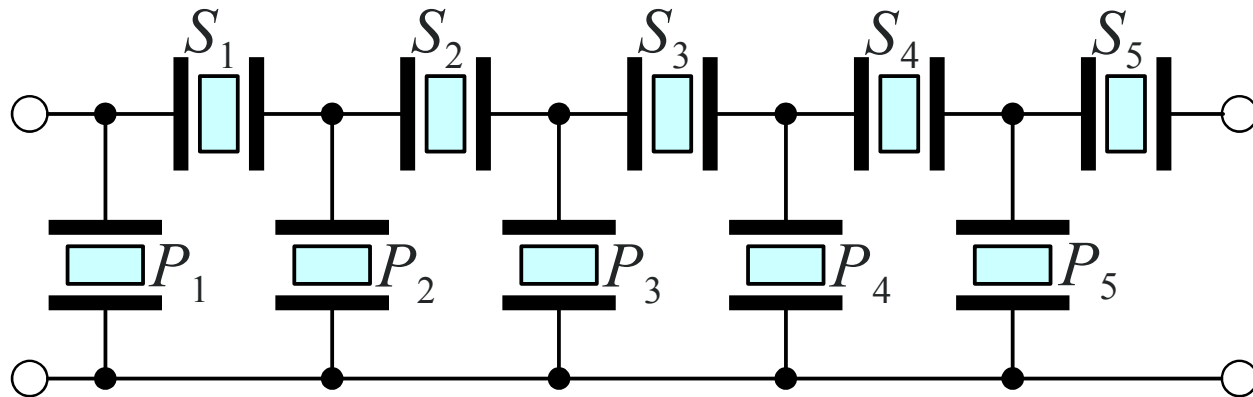
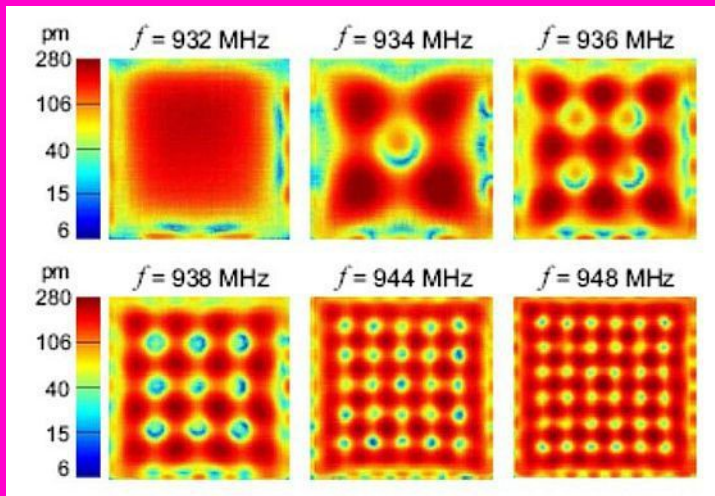
Material	Dielectric constant	Acoustic velocity (m/s)	Acoustic coupling	Acoustic loss dB/ $\mu\text{s}$ At 1 GHz
AlN ( <i>new</i> )	8.5	10,400	0.17	~5
ZnO ( <i>old</i> )	8.8	6,330	0.28	8.3

*FBAR technologies*

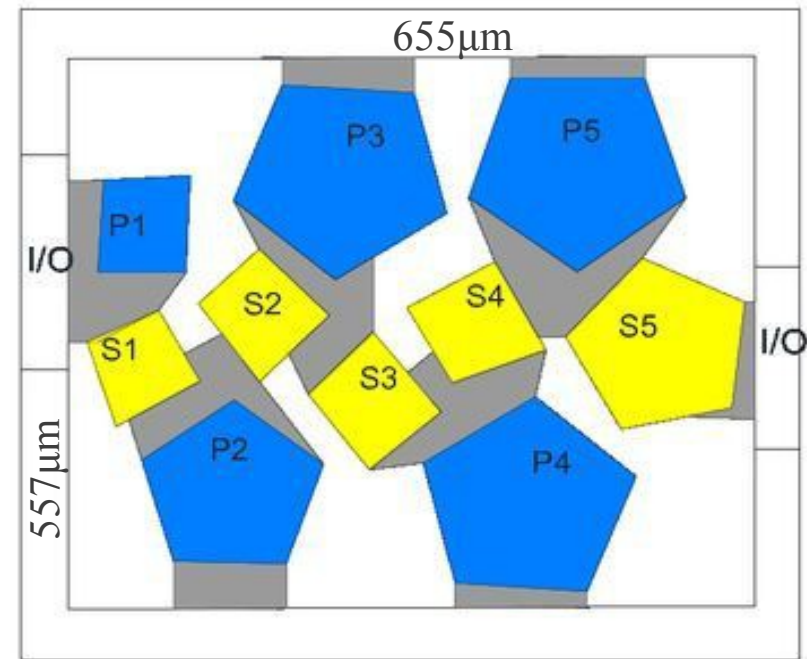




Anharmonics  
(transversal  
modes)  
of a square  
FBAR

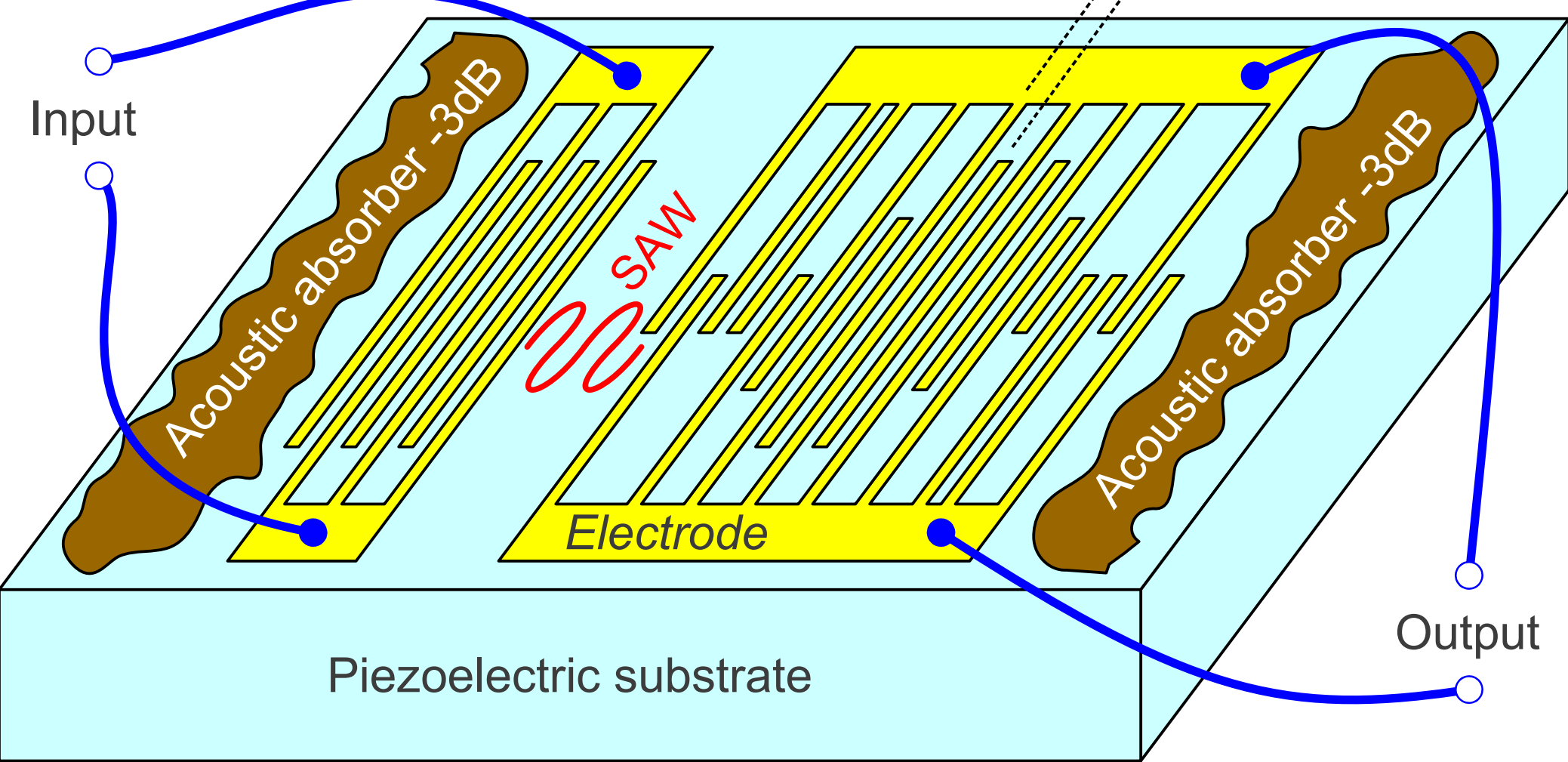


*FBAR bandpass filters (IIR)*

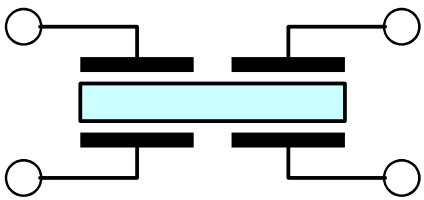


Travelling surface wave → finite impulse response (FIR)

$$\frac{\Lambda}{2} = \frac{v}{2f_0}$$



Crystal substrate:  $\text{SiO}_2$  (quartz) or  $\text{LiNbO}_3$  or  $\text{LiTaO}_3$  or  $\text{La}_3\text{Ga}_5\text{SiO}_{14}$  (langasite)  
 stability ↔ coupling



$v \approx 2\text{km/s} \dots 5\text{km/s}$

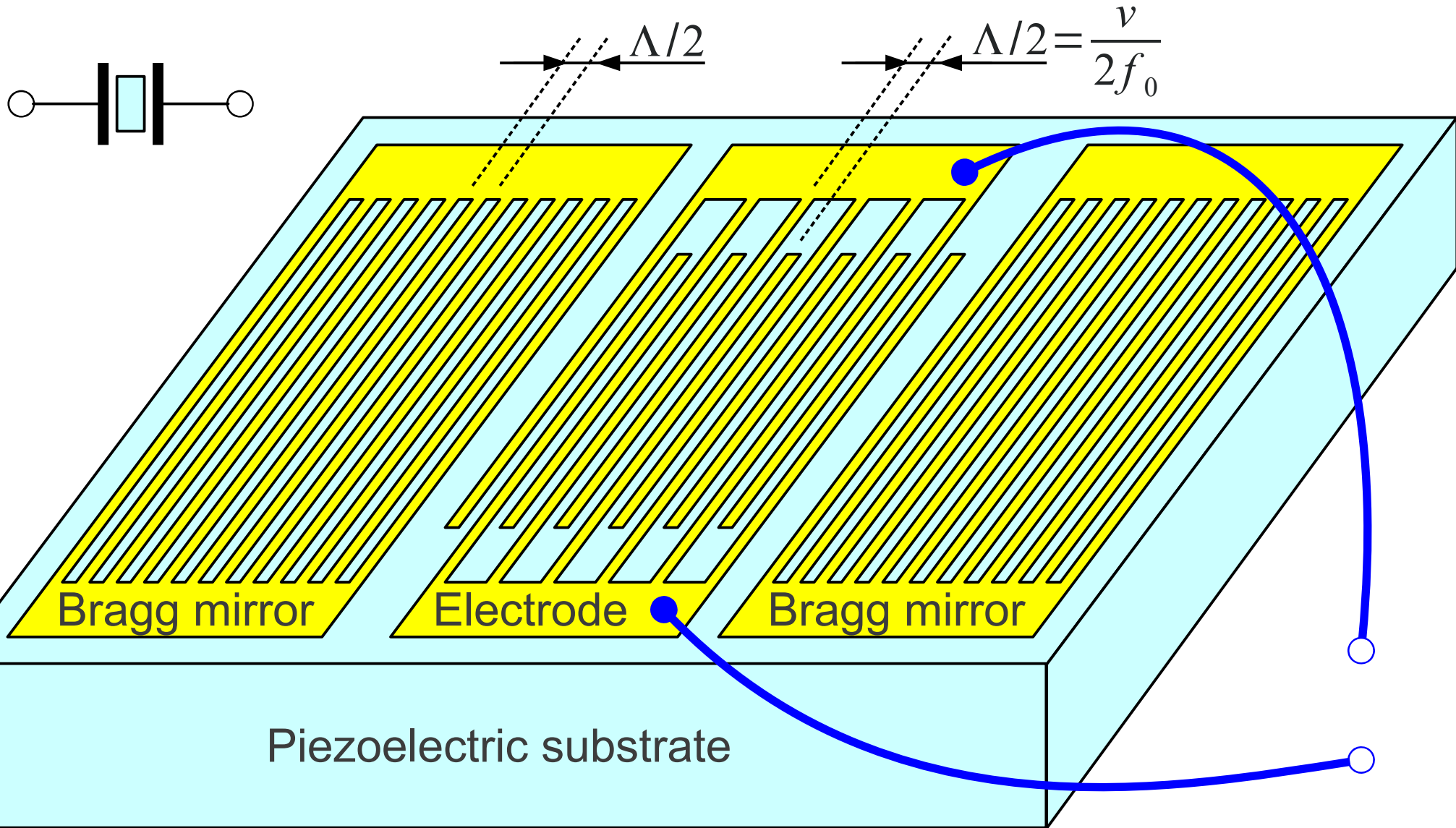
*SAW bandpass (FIR)*





36MHz SAW filter

Standing surface wave  $\rightarrow$  resonator  $\equiv$  infinite impulse response (IIR)



Crystal substrate:  $\text{SiO}_2$  (quartz) or  $\text{LiNbO}_3$  or  $\text{LiTaO}_3$  or  $\text{La}_3\text{Ga}_5\text{SiO}_{14}$  (langasite)  
stability  $\leftrightarrow$  coupling

*SAW resonator*

$v \approx 2\text{km/s} \dots 5\text{km/s}$