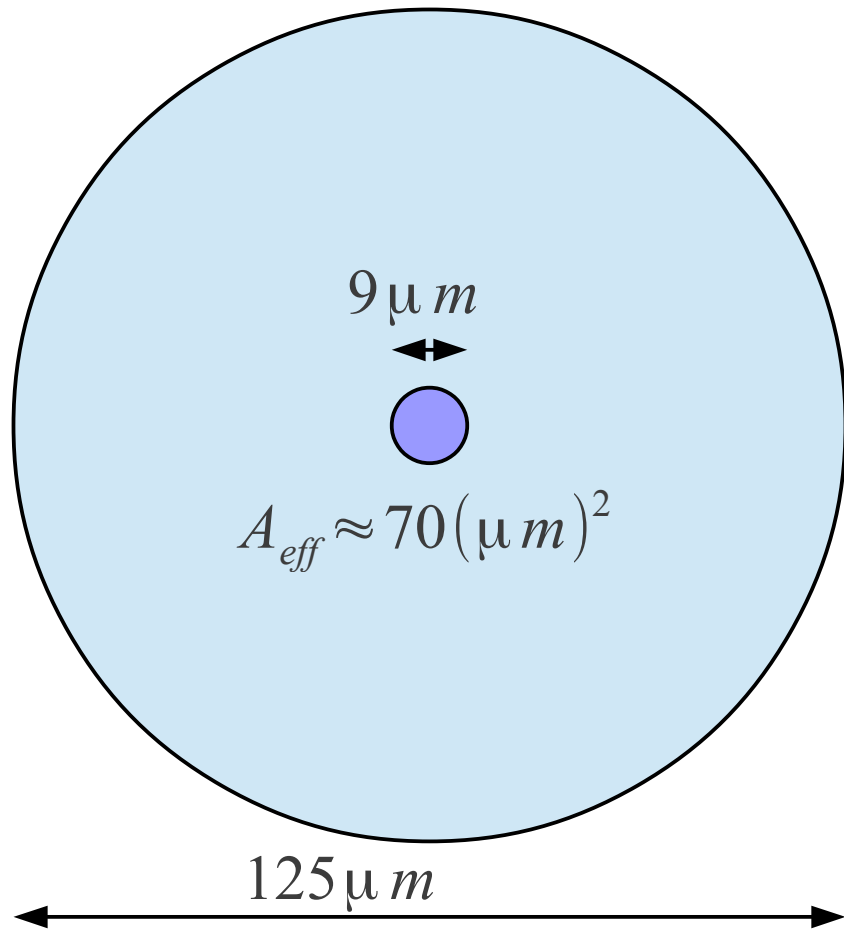


Optične komunikacije

Predavanje 7:

Nelinearne lastnosti svetlobnega vlakna



$SiO_2 + GeO_2$ G.652

$P \approx 100 mW$

$$S = \frac{P}{A_{eff}} \approx \frac{100 mW}{70 \mu m^2} \approx 1.4 \cdot 10^9 W / m^2 = 1.4 GW / m^2 = 140 kW / cm^2$$

$$S = \frac{|E|^2}{2Z} = \frac{|E|^2 n_1}{2Z_0} \quad n_1 \approx 1.5$$

$$Z_0 \approx 377 \Omega$$

$$P \approx 100 mW$$

$$|E| \approx \sqrt{\frac{2Z_0 S}{n_1}} \approx 860 kV / m = 8.6 kV / cm$$

$P \approx 1 mW \rightarrow$ nelinearni pojavi!

$P \approx 10 mW \rightarrow$ zažig vtičnic!

$P \approx 100 mW \rightarrow$ max P na vtičnici!

$P \approx 1 W \rightarrow$ max P v vlaknu!

$P \approx 10 W \rightarrow$ taljenje jedra vlakna!

$$n = n_0 + n_1 \cdot E + n_2 \cdot E^2 + n_3 \cdot E^3 + \dots$$

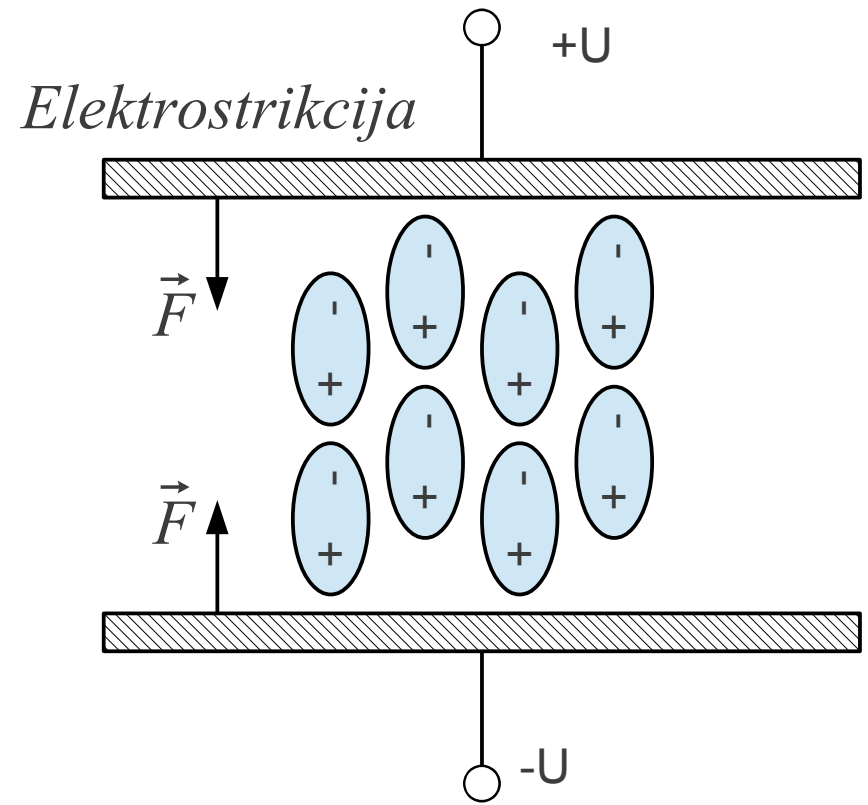
$n_1 \equiv$ Pockelsov pojav

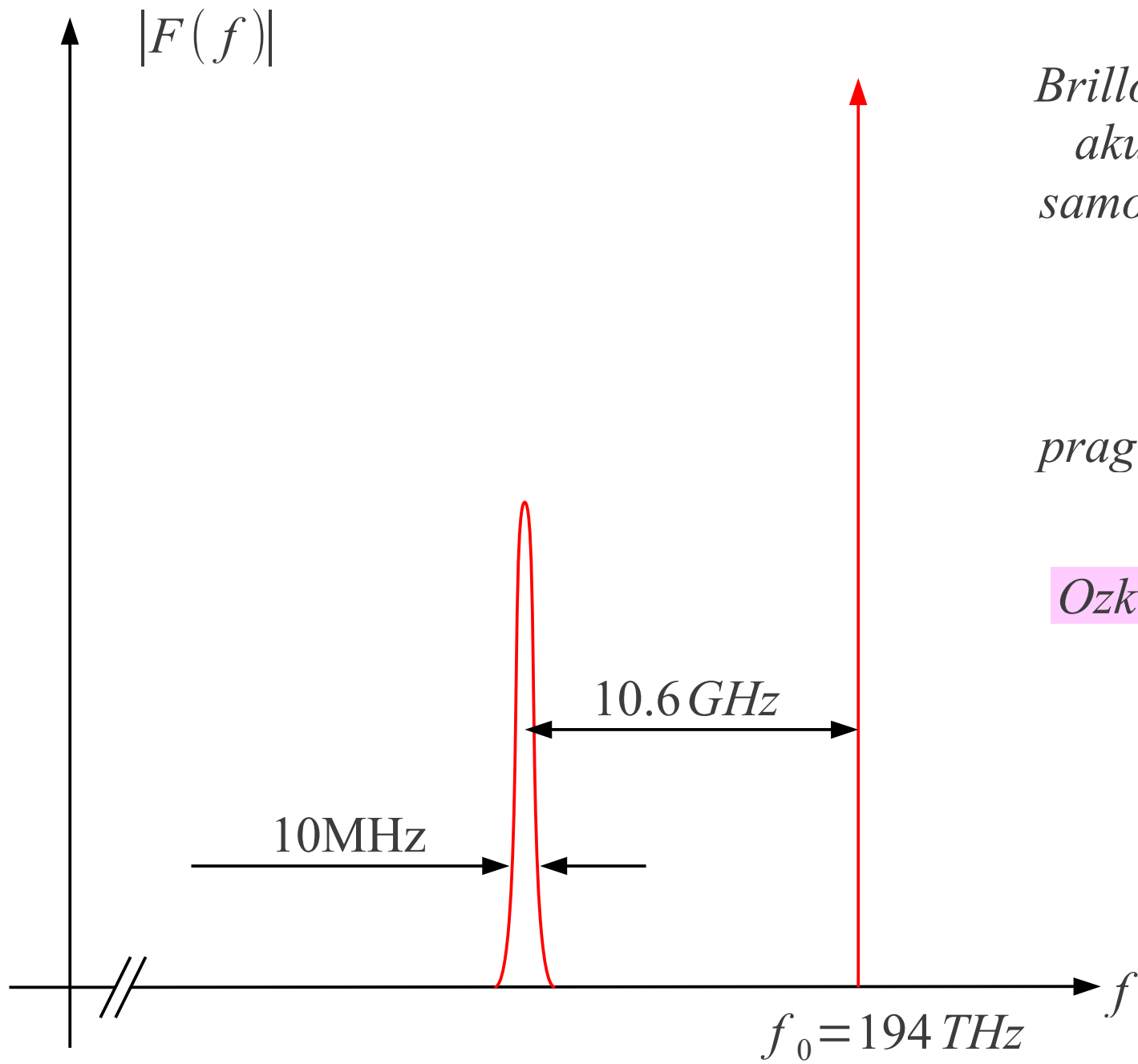
$n_2 \equiv$ Kerrov pojav

$$E^2 \rightarrow S$$

$$n = n_0 + n_2 \cdot S \quad n_0 \approx 1.46$$

$$SiO_2 + GeO_2 \rightarrow n_2 \approx 2.5 \cdot 10^{-20} m^2/W \dots 3.2 \cdot 10^{-20} m^2/W$$

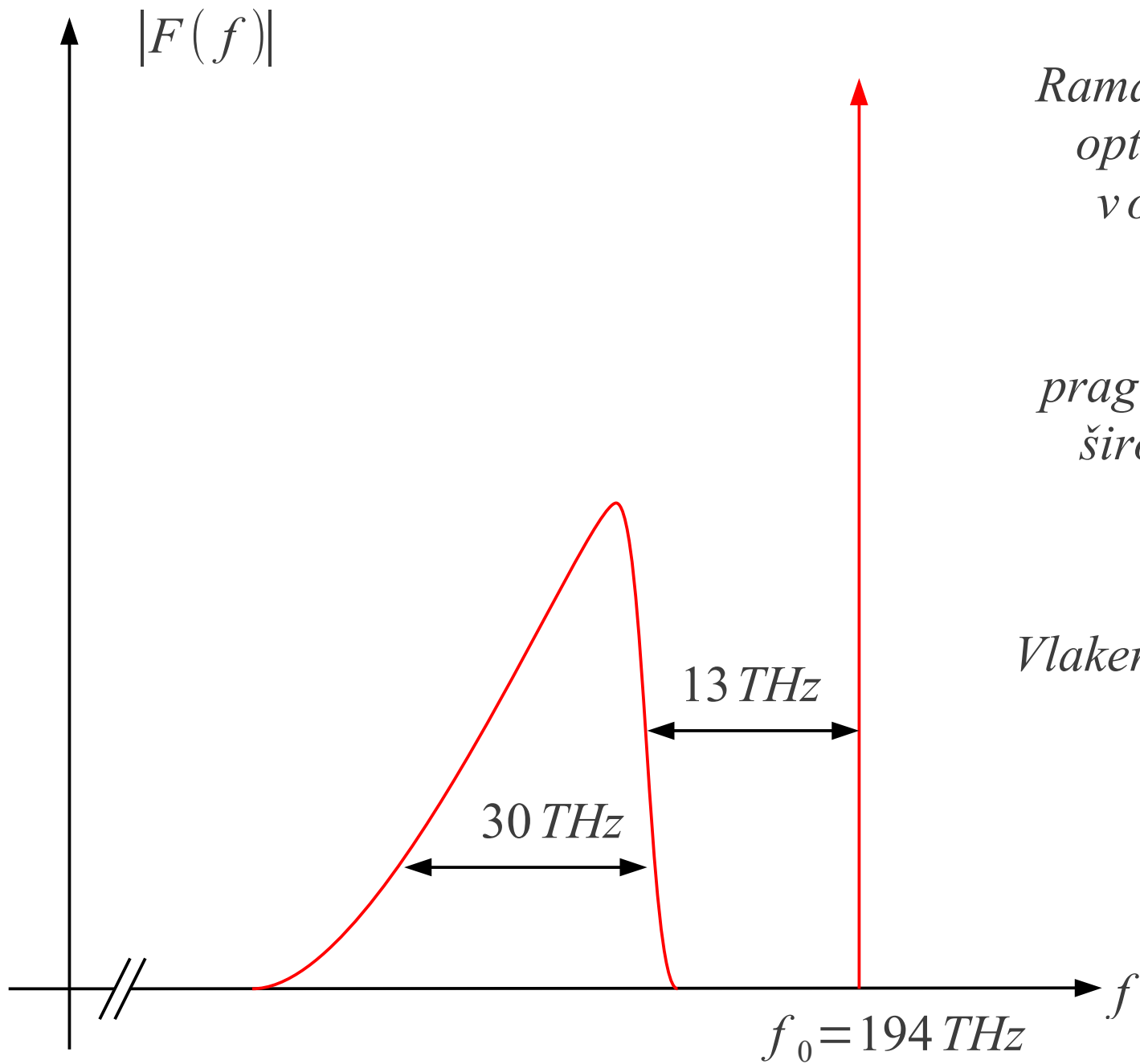




*Brillouinovo sipanje
akustični fononi
samo v smeri nazaj !*

prag laserja $P \approx 1\text{ mW}$

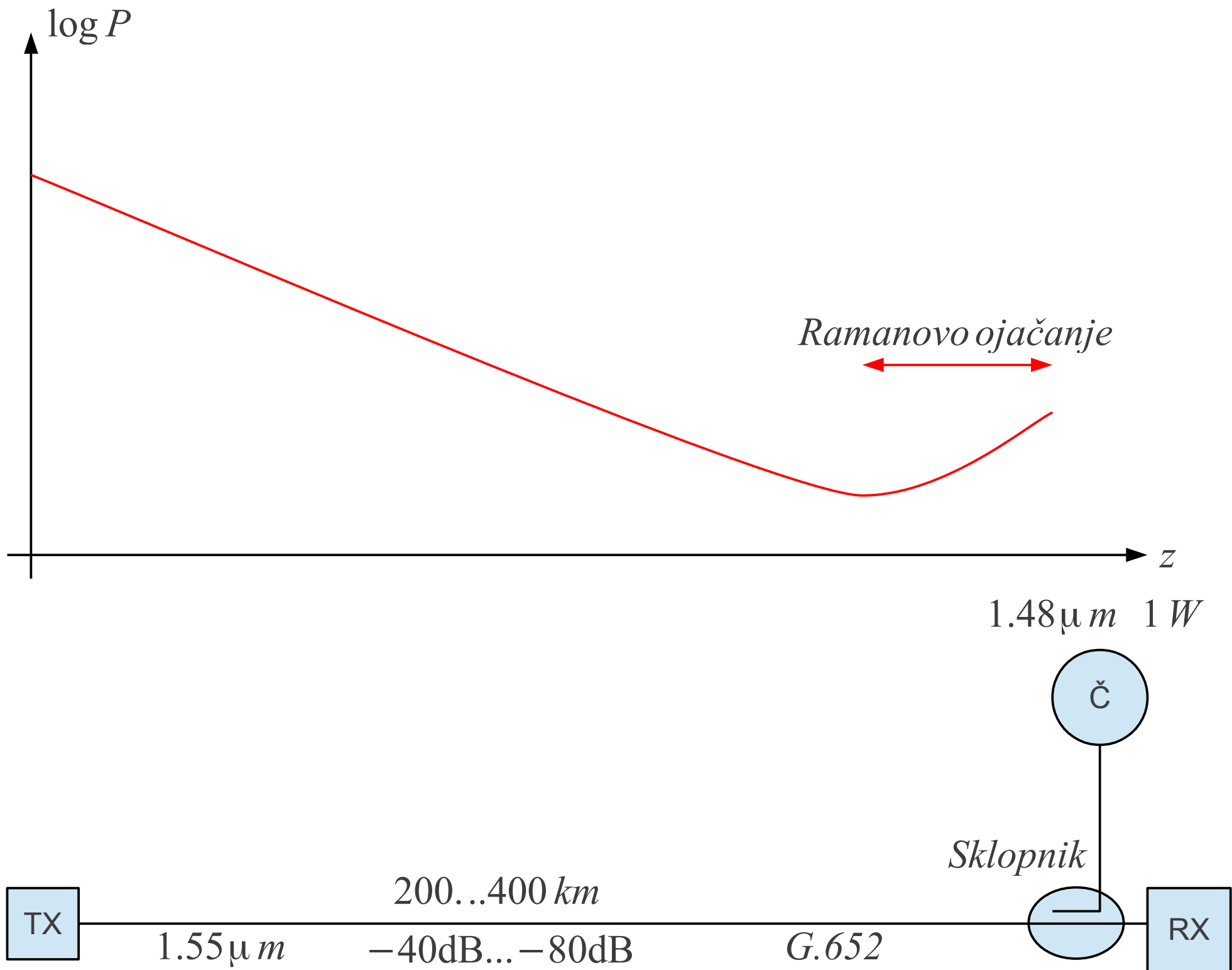
Ozkopasovni pojav !



*Ramanovo sipanje
optični fononi
v obe smeri!*

*prag laserja $P \approx 100 \text{ mW}$
širokopasoven pojav*

*Vlakenski optični ojačevalnik
 $P_{\text{črpalke}} \approx 1 \text{ W}$*



Lastna fazna modulacija

$$n = n_0 + n_2 \cdot S$$

$$\phi = -k \cdot l = -n \cdot k_0 \cdot l = \frac{-n \cdot 2\pi}{\lambda_0} \cdot l$$

$$P \approx 100 \text{ mW}$$

$$\Delta\phi = -\Delta n \cdot \frac{2\pi}{\lambda_0} \cdot l = n_2 \cdot S \cdot \frac{2\pi}{\lambda_0} \cdot l = \frac{2\pi \cdot n_2 \cdot P}{A_{\text{eff}} \cdot \lambda_0} \cdot l \approx 0.15 \text{ rd}$$

$$A_{\text{eff}} \approx 70 (\mu\text{m})^2$$

$$n_2 \approx 2.5 \cdot 10^{-20} \text{ m}^2 / \text{W}$$

$$l = 1 \text{ km}$$

linearni D + nelinearni n → Solitonski prenos! (1995)

Soliton ≡ skrbno izbrana obilka impulza

Lastna fazna modulacija z upoštevanjem slabljenja vlakna !

$$a \approx 0.2 \text{ dB/km} \qquad P(z) = P(0) \cdot 10^{-\frac{a \cdot z}{10}} = P(0) \cdot e^{-\frac{a \ln 10}{10} \cdot z}$$

$$\Delta \phi = \frac{-2 \pi \cdot n_2}{A_{\text{eff}} \cdot \lambda_0} \cdot \int_0^l P(z) dz = \frac{-2 \pi \cdot n_2 \cdot P(0)}{A_{\text{eff}} \cdot \lambda_0} \cdot \int_0^l e^{-\frac{a \ln 10}{10} \cdot z} dz$$

$$l_{\text{eff}} = \int_0^l e^{-\frac{a \ln 10}{10} \cdot z} dz \approx \int_0^{\infty} e^{-\frac{a \ln 10}{10} \cdot z} dz = \frac{10}{a \ln 10} = 21.7 \text{ km}$$

$$\Delta \phi = \frac{-2 \pi \cdot n_2 \cdot P(0)}{A_{\text{eff}} \cdot \lambda_0} \cdot l_{\text{eff}} \approx -2.83 \text{ rd}$$

$$P \approx 100 \text{ mW}$$

$$A_{\text{eff}} \approx 70 (\mu\text{m})^2$$

$$n_2 \approx 2.5 \cdot 10^{-20} \text{ m}^2/\text{W}$$

$$l > 50 \text{ km}$$

Dvotonsko krmiljenje

$$E = A_1 \cos \omega_1 t + A_2 \cos \omega_2 t \quad \dots (\text{zanemarim polarizacijo!})$$

$$\Delta \omega = \omega_1 - \omega_2 \ll \omega_1, \omega_2 \rightarrow \text{utripanje!}$$

$$p(t) = \alpha |E|^2 = \alpha |A_1 \cos \omega_1 t + A_2 \cos \omega_2 t|^2$$

$$p(t) = \alpha |A_1^2 \cos^2 \omega_1 t + A_2^2 \cos^2 \omega_2 t + 2 A_1 A_2 \cos \omega_1 t \cos \omega_2 t|^2$$

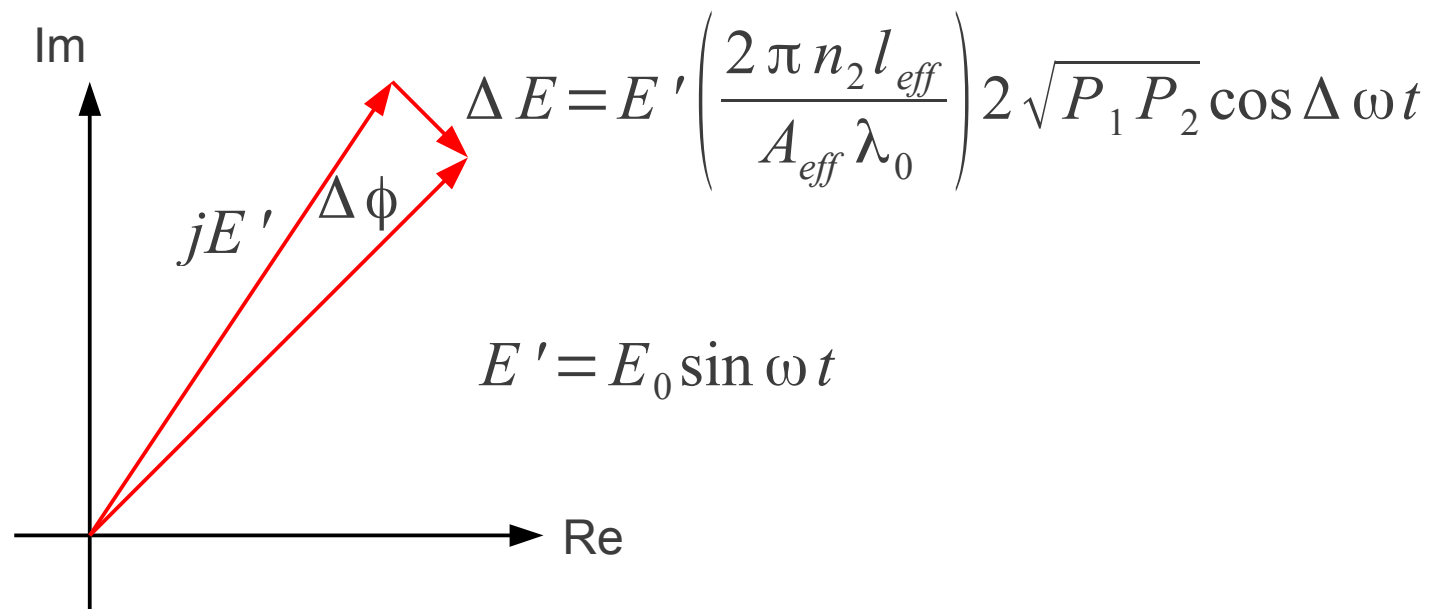
$$\cos x \cos y = \frac{1}{2} [\cos(x+y) + \cos(x-y)]$$

$$P = \langle p(t) \rangle = P_1 + P_2 + 2 \sqrt{P_1 P_2} \cos \Delta \omega t \quad \dots \text{samo počasni členi!}$$

Utripanje

$$\Delta \phi = \frac{-2 \pi \cdot n_2}{A_{eff} \cdot \lambda_0} \cdot l_{eff} \cdot 2 \sqrt{P_1 P_2} \cos \Delta \omega t \quad \dots \text{samo utripanje}$$

Križna fazna modulacija!



$$\Delta E = E_0 \left(\frac{2 \pi n_2 l_{eff}}{A_{eff} \lambda_0} \right) 2 \sqrt{P_1 P_2} \cos \Delta \omega t \sin \omega t$$

$$\cos x \sin y = \frac{1}{2} (\sin (y+x) + \sin (y-x))$$

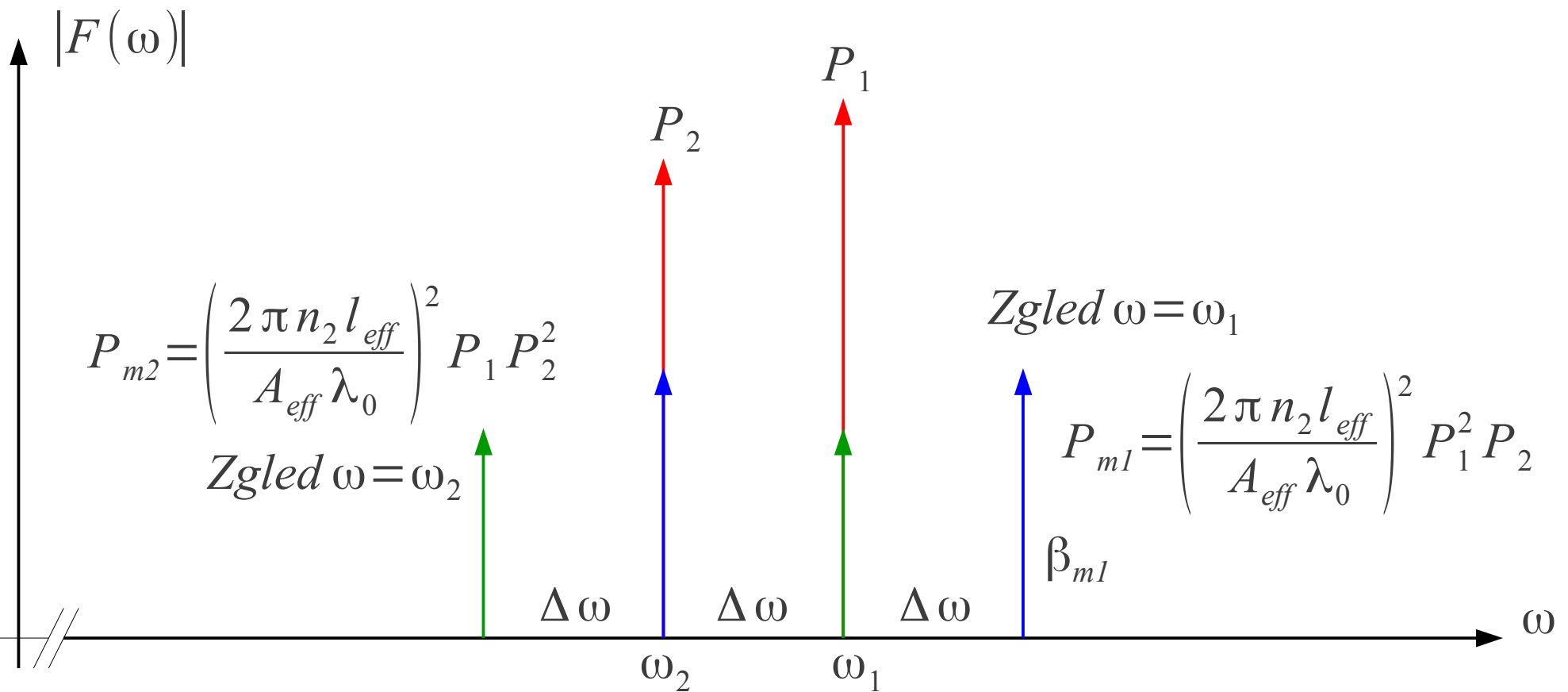
$$\Delta E = E_0 \left(\frac{2 \pi n_2 l_{eff}}{A_{eff} \lambda_0} \right) \sqrt{P_1 P_2} [\sin (\omega + \Delta \omega) t + \sin (\omega - \Delta \omega) t]$$

Dve novi frekvenci ≡ mešanje!

$$P(\omega + \Delta\omega) = P(\omega - \Delta\omega) = P(\omega) \cdot \left(\frac{2\pi n_2 l_{eff}}{A_{eff} \lambda_0} \right)^2 P_1 P_2$$

Štirivalovno mešanje FWM (Four – Wave Mixing)

Elektroinženirji 50 let pred fiziki! Intermodulacijsko popačenje IMD

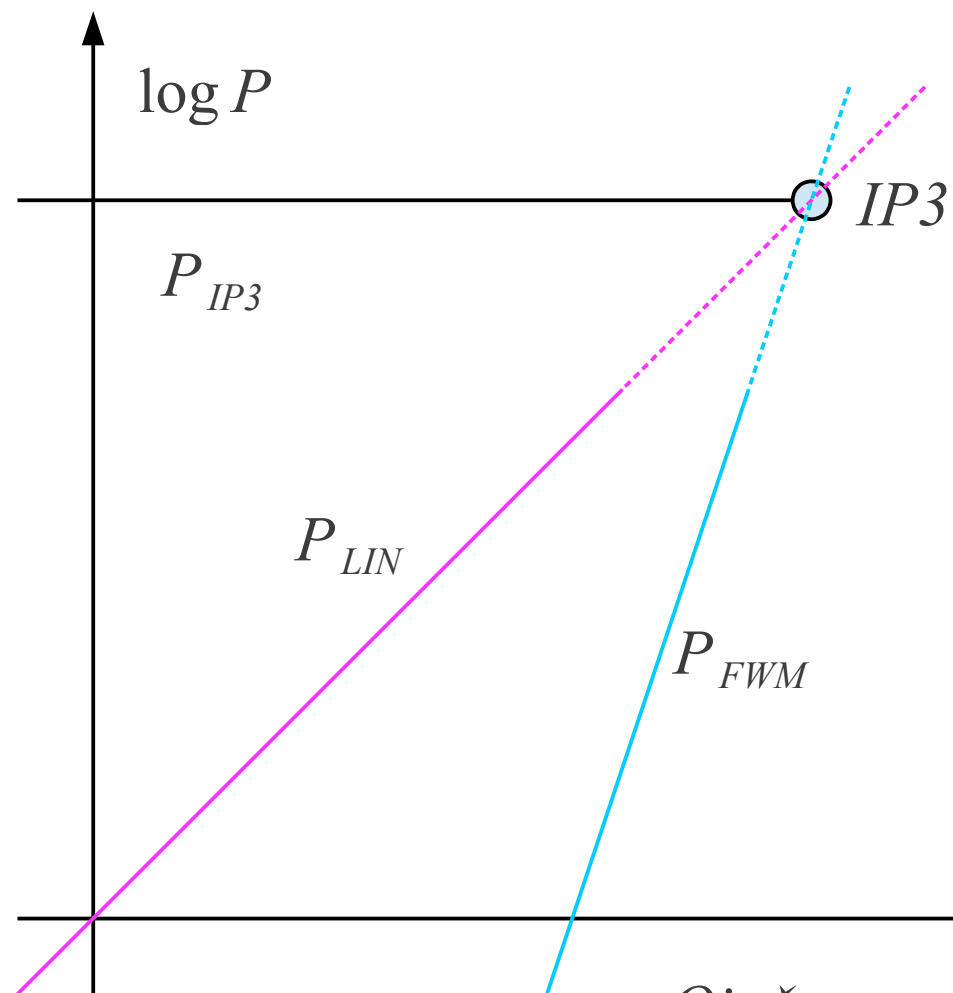


$$P_{m1} = \left(\frac{2\pi n_2 l_{eff}}{A_{eff} \lambda_0} \right)^2 P_1^2 P_2 = \frac{P_1^2 P_2}{P_{IP3}^2}$$

$$\left(\frac{2\pi n_2 l_{eff}}{A_{eff} \lambda_0} \right)^2 [W^{-2}]$$

$$P_{m2} = \left(\frac{2\pi n_2 l_{eff}}{A_{eff} \lambda_0} \right)^2 P_1 P_2^2 = \frac{P_1 P_2^2}{P_{IP3}^2}$$

$$P_{IP3} = \left(\frac{A_{eff} \lambda_0}{2\pi n_2 l_{eff}} \right) [W]$$



$$DSF G.653 \quad A_{eff} \approx 30 (\mu m)^2$$

$$n_2 \approx 2.5 \cdot 10^{-20} m^2/W$$

$$l_{eff} = 21.7 km$$

$$P_{IP3} = \left(\frac{A_{eff} \lambda_0}{2\pi n_2 l_{eff}} \right) = 14 mW$$

Ojačevana zveza $N \cdot l_{eff} !!!$

vlakno

porazdeljena nelinearnost → porazdeljeno mešanje

$$l_{eff} = \left| \int_0^l e^{-\frac{a \ln 10}{10} \cdot z} e^{-j \Delta \beta} dz \right| \approx \frac{1}{\sqrt{\left(\frac{a \ln 10}{10}\right)^2 + (\Delta \beta)^2}}$$

$$\Delta \omega = 2 \pi \cdot 100 \text{ GHz}$$

$$l_{eff} \approx \frac{1}{\Delta \beta} \approx 0.4 \text{ km}$$

$$\text{Fazna neuskklajenost} \equiv \Delta \beta = \beta_2 + \beta_{ml} - 2 \beta_1 \approx \frac{d^2 \beta}{d \omega^2} \cdot (\Delta \omega)^2 \approx -2.51 \text{ rd/km}$$

$$t_g = \frac{l}{v_g} = l \frac{d \beta}{d \omega}$$

$$\text{NZDSF G.655 } D \approx 5 \text{ ps/(nm.km)}$$

$$\frac{d t_g}{d \omega} = l \frac{d^2 \beta}{d \omega^2} = \frac{d t_g}{d \lambda_0} \cdot \frac{d \lambda_0}{d \omega} = D \cdot l \cdot \frac{-\lambda_0^2}{2 \pi c_0}$$

$$\frac{d^2 \beta}{d \omega^2} = D \cdot \frac{-\lambda_0^2}{2 \pi c_0}$$

$$\Delta \omega = 2 \pi \cdot 100 \text{ GHz}$$

WDM ≈ 100 kanalov po 100 GHz

$$l_{\text{eff}} \approx \frac{1}{\Delta \beta} \approx 0.4 \text{ km}$$

NZDSF G.655 $D \approx 5 \text{ ps}/(\text{nm} \cdot \text{km})$

$$A_{\text{eff}} \approx 80 (\mu\text{m})^2$$

$$P_{\text{IP3}} = \left(\frac{A_{\text{eff}} \lambda_0}{2 \pi n_2 l_{\text{eff}}} \right) = 2 \text{ W}$$

$$P_{\text{ml}} = \left(\frac{2 \pi n_2 l_{\text{eff}}}{A_{\text{eff}} \lambda_0} \right)^2 P_1^2 P_2 = \frac{P_1^2 P_2}{P_{\text{IP3}}^2} \approx 2 \text{ nW}$$

$$P_1 = P_2 = 2 \text{ mW}$$

Ojačevana zveza $N \cdot l_{\text{eff}} = 40 \text{ km}$ $N = 100$

$$P_{\text{IP3}} \approx 20 \text{ mW} \rightarrow P_{\text{ml}} \approx 0.02 \text{ mW}$$

vlakno LEAF
Large Effective Area Fiber

