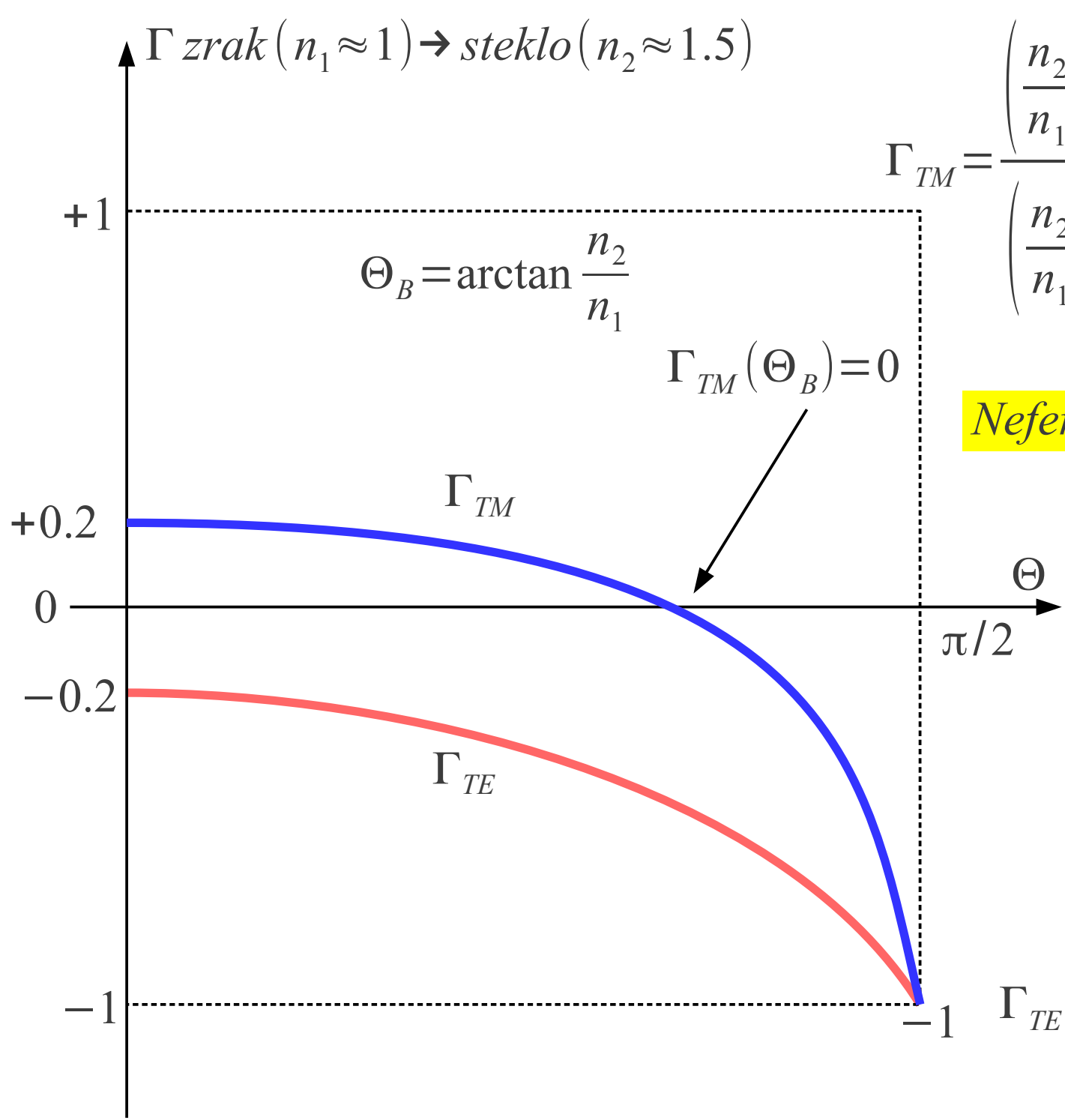


Optične komunikacije

Predavanje 3:

Popolni odboj v dielektričnem valovodu

Γ zrak ($n_1 \approx 1$) \rightarrow steklo ($n_2 \approx 1.5$)



$$\Theta_B = \arctan \frac{n_2}{n_1}$$

$$\Gamma_{TM}(\Theta_B) = 0$$

$$\Gamma_{TM} = \frac{\left(\frac{n_2}{n_1}\right)^2 \cos \Theta - \sqrt{\left(\frac{n_2}{n_1}\right)^2 - \sin^2 \Theta}}{\left(\frac{n_2}{n_1}\right)^2 \cos \Theta + \sqrt{\left(\frac{n_2}{n_1}\right)^2 - \sin^2 \Theta}}$$

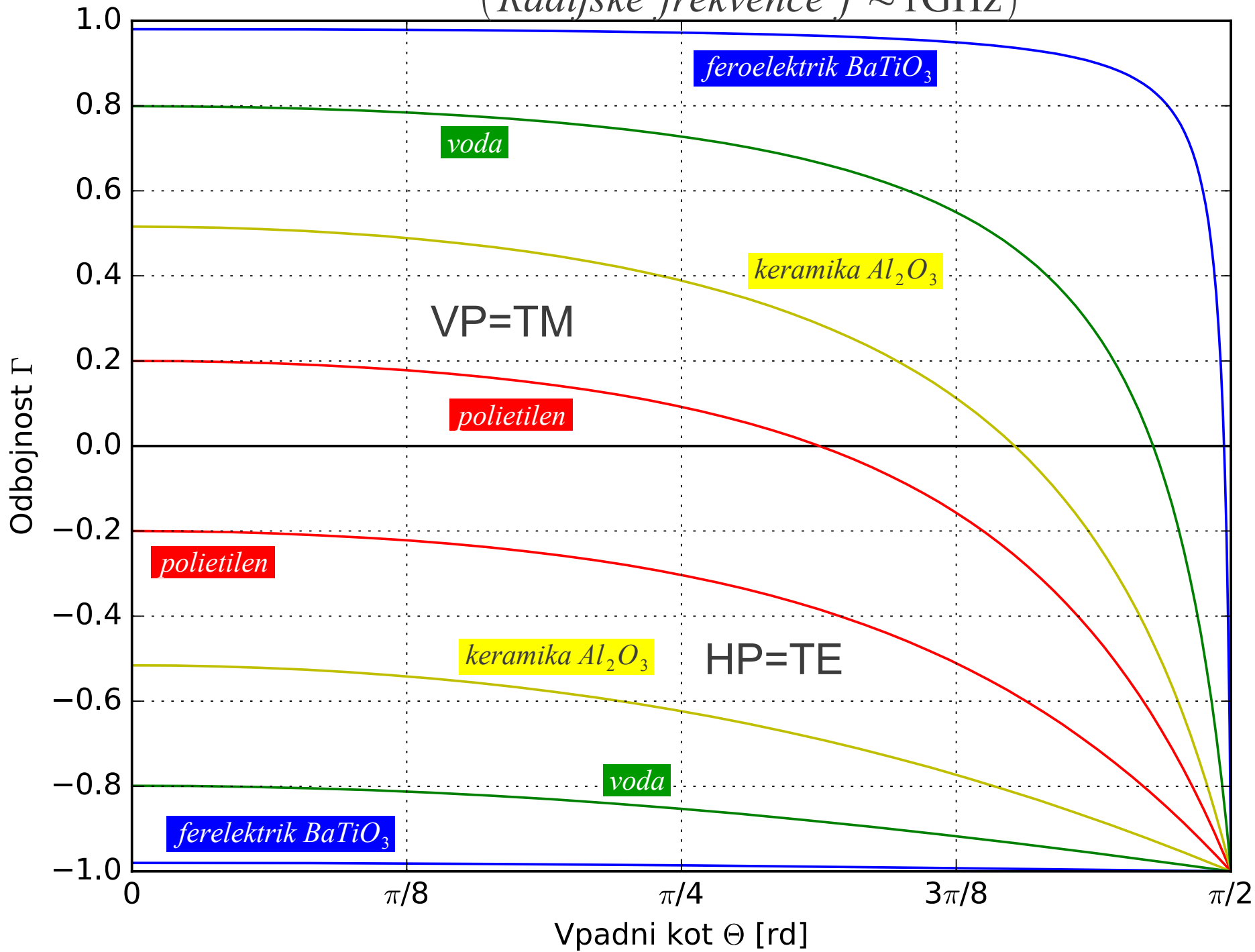
Neferomagnetiki $\mu_{r1} = \mu_{r2} = 1$

$$n_1 = \sqrt{\epsilon_{r1}} \approx \sqrt{1} = 1$$

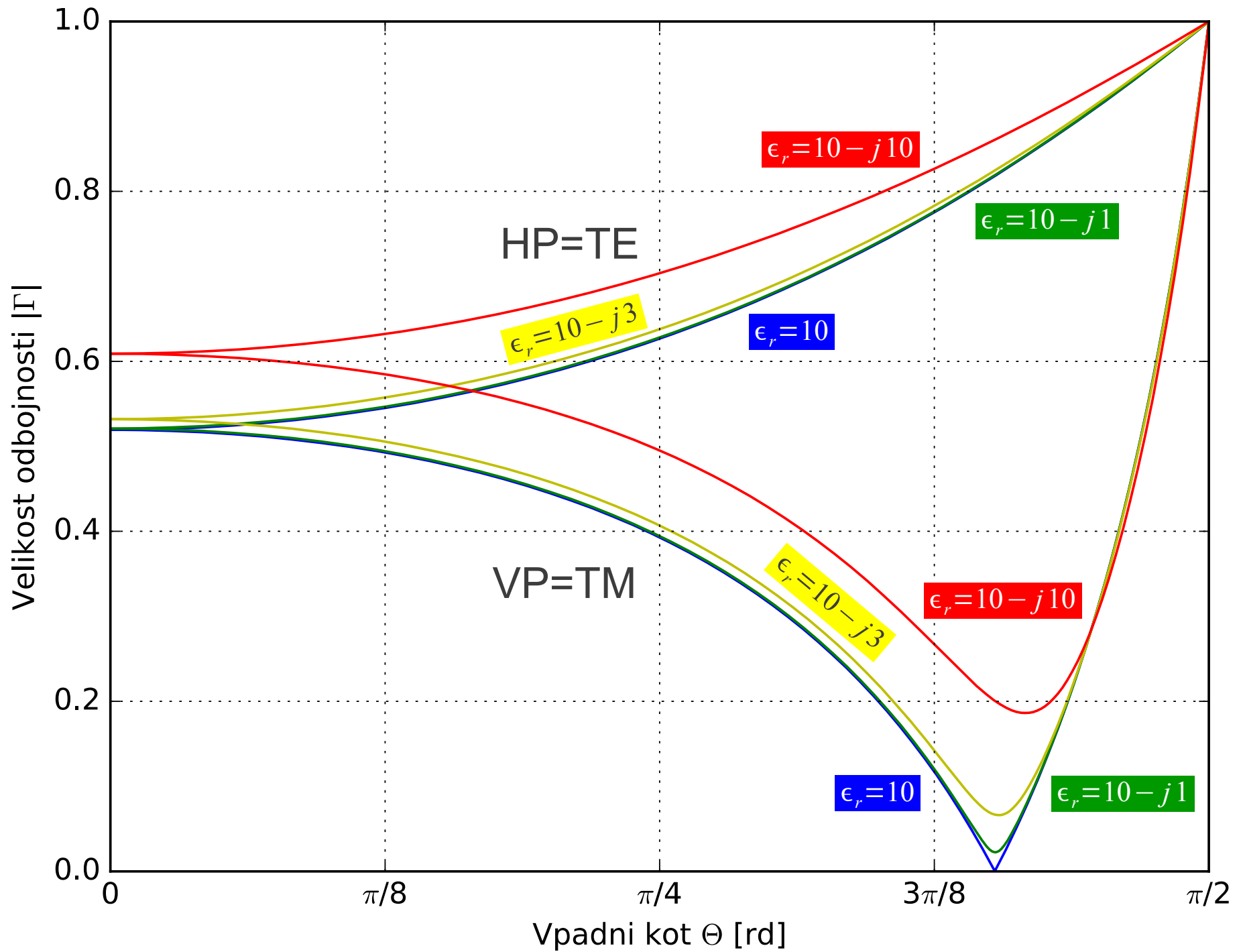
$$n_2 = \sqrt{\epsilon_{r2}} \approx \sqrt{2.25} = 1.5$$

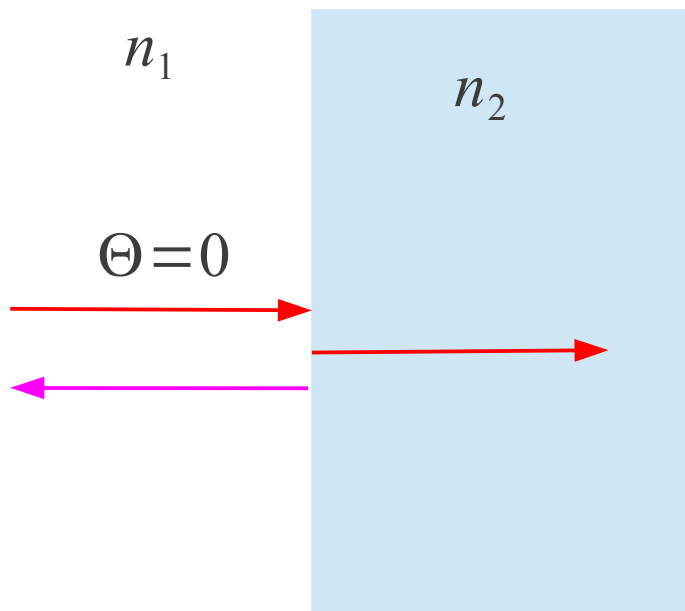
$$\Gamma_{TE} = \frac{\cos \Theta - \sqrt{\left(\frac{n_2}{n_1}\right)^2 - \sin^2 \Theta}}{\cos \Theta + \sqrt{\left(\frac{n_2}{n_1}\right)^2 - \sin^2 \Theta}}$$

Dielektrik $\epsilon_r = 2.25$ (*polietilen*), 9.8 (Al_2O_3), 80 (*voda*), 10000 ($BaTiO_3$)
 (Radijske frekvence $f \approx 1$ GHz)



Zrak ($\epsilon_r \approx 1$) \rightarrow Dielektrik z izgubami $\epsilon_r = 10, 10-j1, 10-j3, 10-j10$



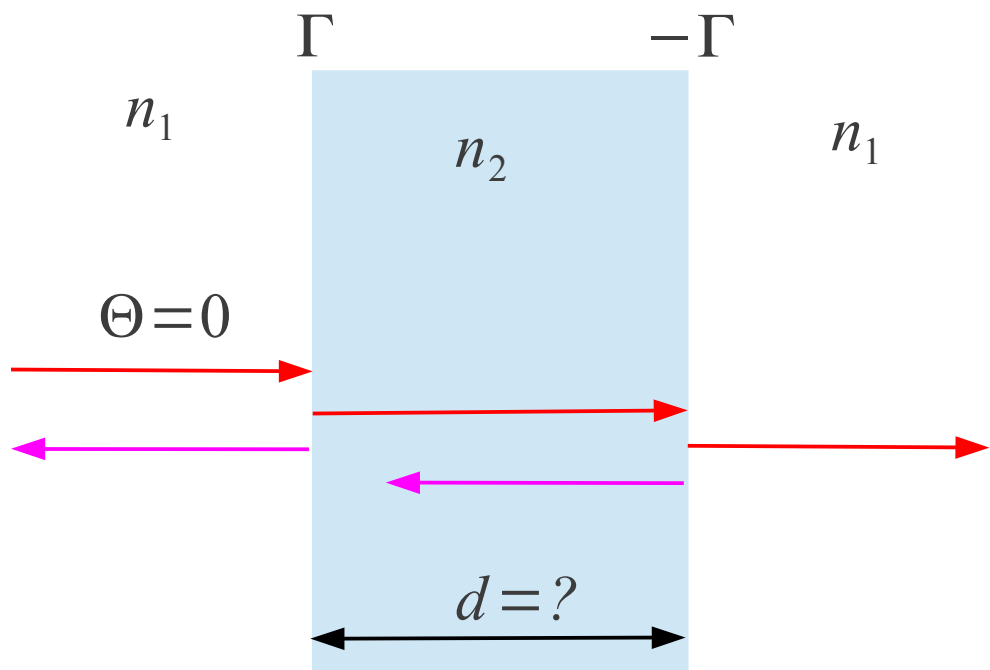
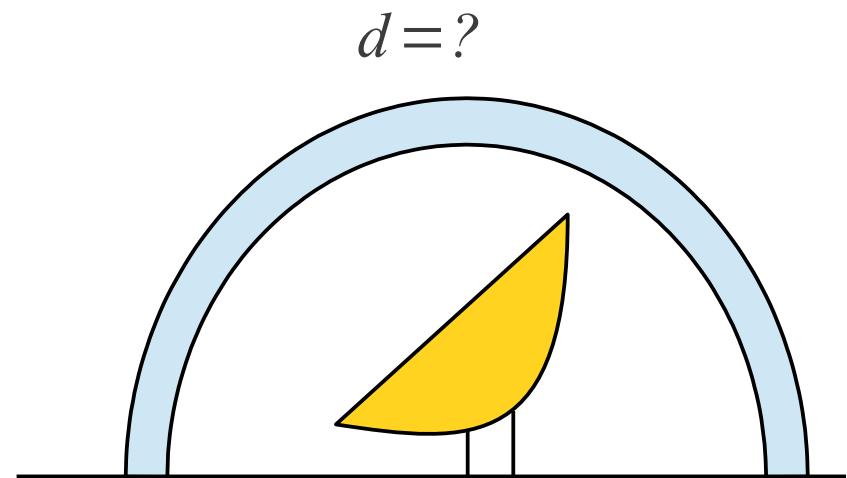


$$\Gamma_{TE} = \frac{n_1 - n_2}{n_1 + n_2} = -\Gamma_{TM}$$

$$\Gamma = \left| \frac{n_1 - n_2}{n_1 + n_2} \right|$$

$$P_O = P_V |\Gamma|^2$$

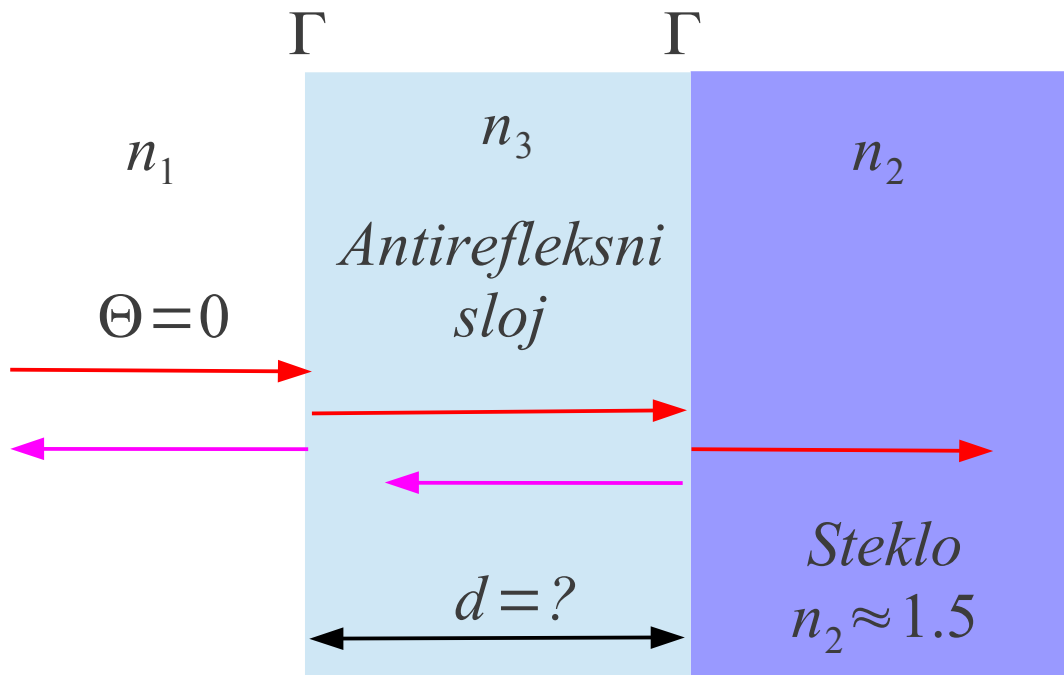
*Prozoren pokrov
za anteno*



$$\phi = 2 d k_2 = m 2 \pi$$

$$2 d = m \lambda_2 \quad k_2 = \frac{2 \pi}{\lambda_2}$$

$$\lambda_2 = \frac{\lambda_0}{n_2} = \frac{\lambda_0}{\sqrt{\epsilon_r}}$$



Zrak $n_1 \approx 1$

Steklo $n_2 \approx 1.5$

Antirefleksni sloj

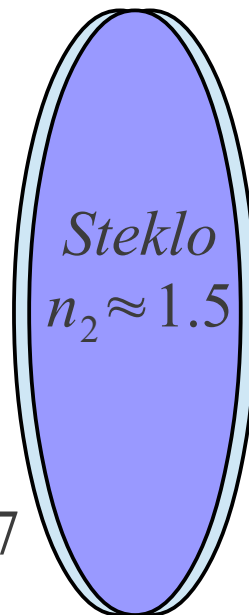
$$n_3 = \sqrt{n_1 n_2}$$

$$\phi = 2 d k_2 = \pi + m 2 \pi$$

$$2 d = \lambda_3 / 2 + m \lambda_3$$

$$d = \lambda_3 / 4 + m \lambda_3 / 2$$

$$d = \lambda_3 / 4$$



MgF₂
 $n_3 \approx 1.37$

MgF₂
 $n_3 \approx 1.37$

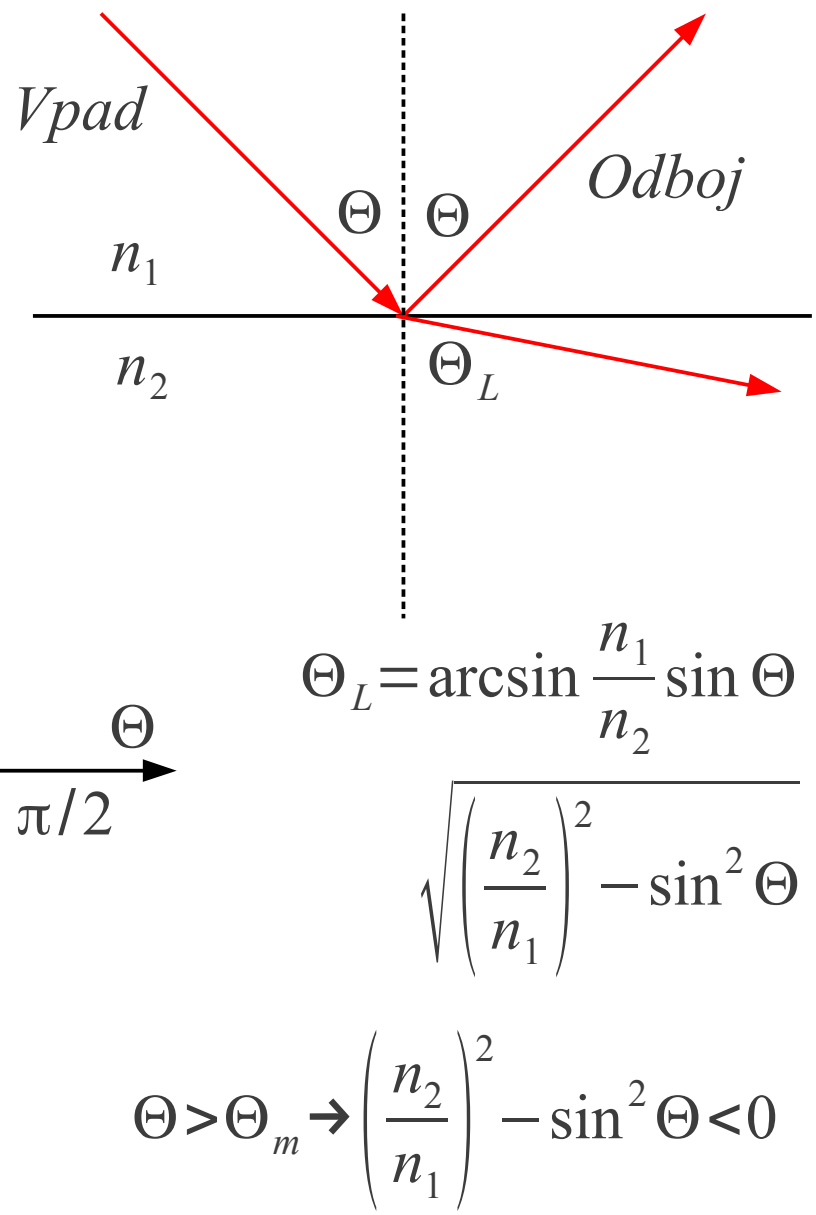
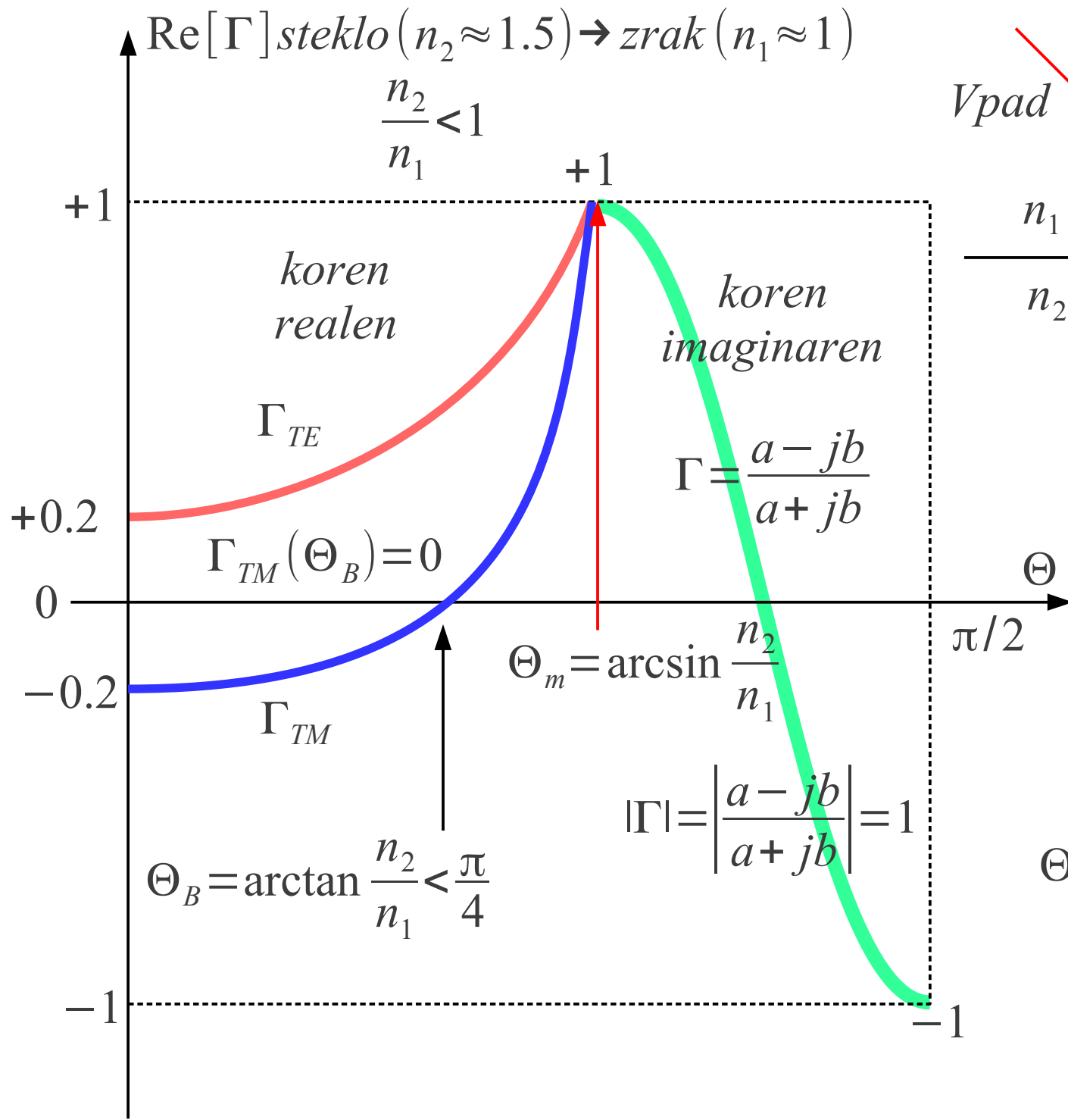
$$\sqrt{1.5} \approx 1.23$$

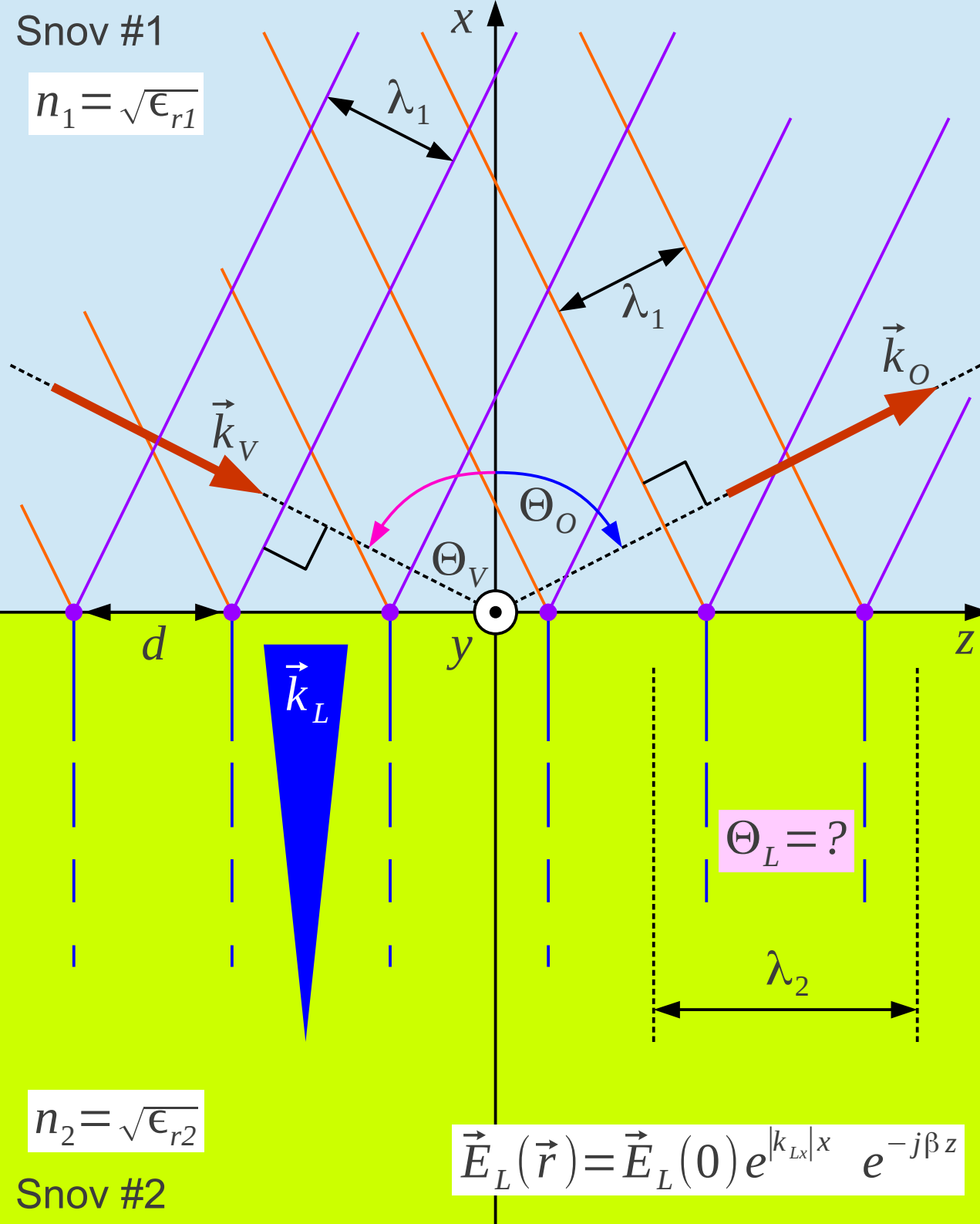
MgF₂ $n_3 \approx 1.37$

$\lambda_0 \approx 0.5 \mu m \equiv$ vidna svetloba

$\lambda_3 \approx 0.4 \mu m$

$d = \lambda_3 / 4 \approx 0.1 \mu m$





Snov #1

$$n_1 = \sqrt{\epsilon_{r1}}$$

$$n_2 = \sqrt{\epsilon_{r2}}$$

Snov #2

$$\vec{E}_L(\vec{r}) = \vec{E}_L(0) e^{|k_{Lx}|x} e^{-j\beta z}$$

Primer $n_2 < n_1$ velik $\sin \Theta_V$
 $\lambda_2 > d > \lambda_1$

$$\sin \Theta_L = \frac{n_1}{n_2} \sin \Theta_V > 1$$

Lomljeni žarek ne obstaja ?

$$\vec{S} = \frac{1}{2} \vec{E} \times \vec{H}^* \equiv \text{Poynting} \left[\frac{W}{m^2} \right]$$

$$k_{Vx}^2 + \beta^2 = k_{Ox}^2 + \beta^2 = k_1^2 = n_1^2 k_0^2$$

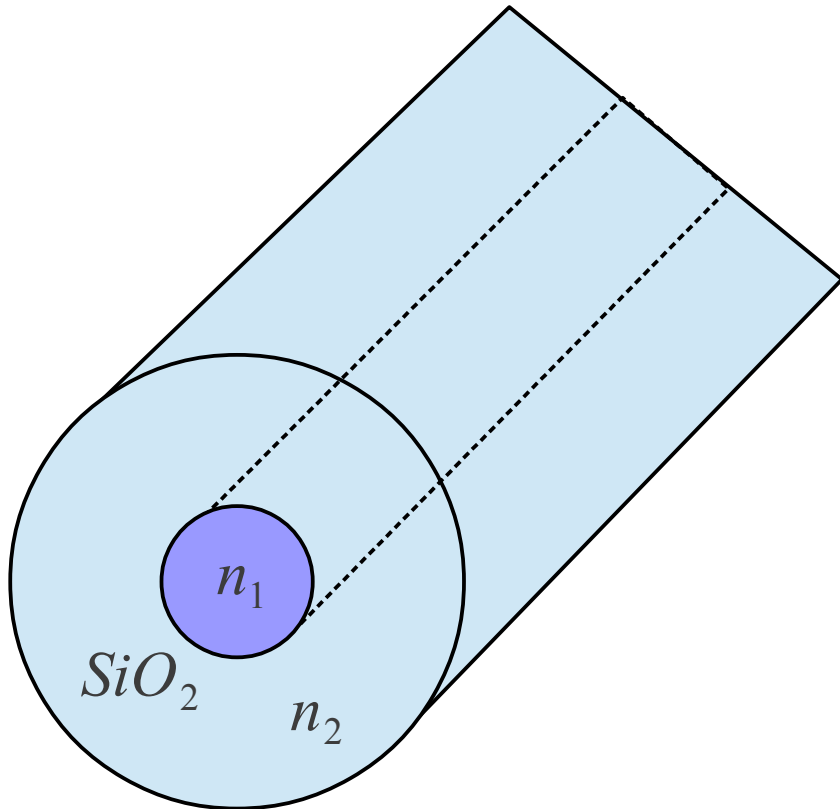
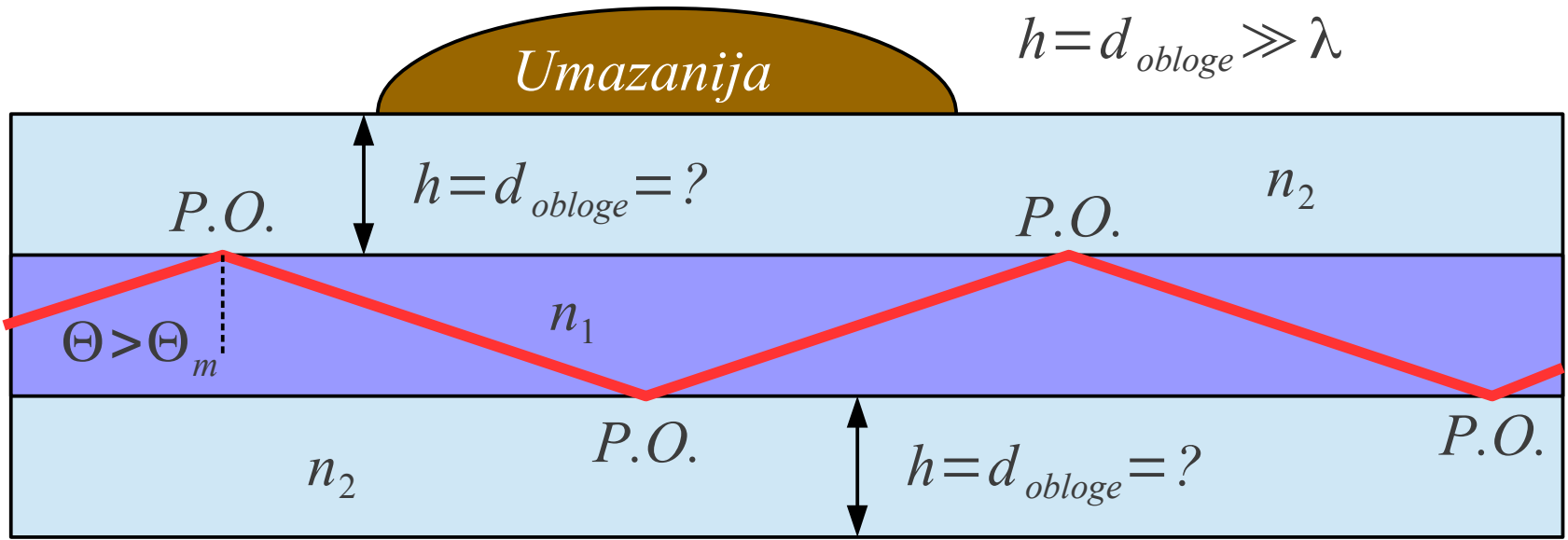
$$k_{Lx}^2 + \beta^2 = k_2^2 = n_2^2 k_0^2$$

$$k_{Lx}^2 = n_2^2 k_0^2 - \beta^2 = (n_2^2 - n_1^2 \sin^2 \Theta_V) k_0^2 < 0$$

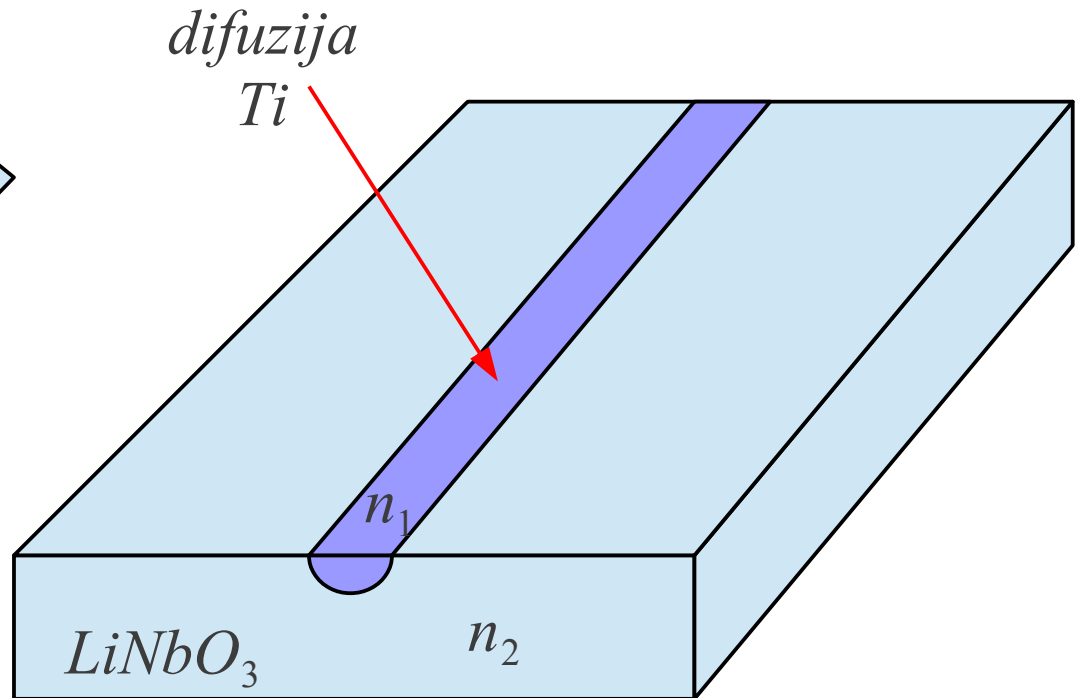
$$k_{Lx} = j \sqrt{\beta^2 - k_2^2} = j |k_{Lx}|$$

$$\vec{k}_L = \vec{1}_x (j |k_{Lx}|) + \vec{1}_z \beta$$

$$\text{Re}[-\vec{1}_x \cdot \vec{S}_2] = 0$$



Vlakno krožnega prereza



Planarni dielektrični valovod

Vpad + odboj

$$-k_{Vx} = k_{Ox} = \sqrt{n_1^2 k_0^2 - \beta^2}$$

$$\vec{E}_1(\vec{r}) = \vec{E}_V(0) e^{+jk_{1x}x} e^{-j\beta z} + \vec{E}_O(0) e^{-jk_{1x}x} e^{-j\beta z}$$

$$n_2 < n_1 < n_3$$

$$\lambda_2 > d > \lambda_1 > \lambda_3$$

$$\sin \Theta_T > 1$$

Tuneliranje

$$\pm |k_{Tx}| = \pm \sqrt{\beta^2 - n_2^2 k_0^2}$$

$$\vec{E}_2(\vec{r}) = \vec{E}_{T+}(0) e^{+|k_{Tx}|x} e^{-j\beta z} + \vec{E}_{T-}(0) e^{-|k_{Tx}|x} e^{-j\beta z}$$

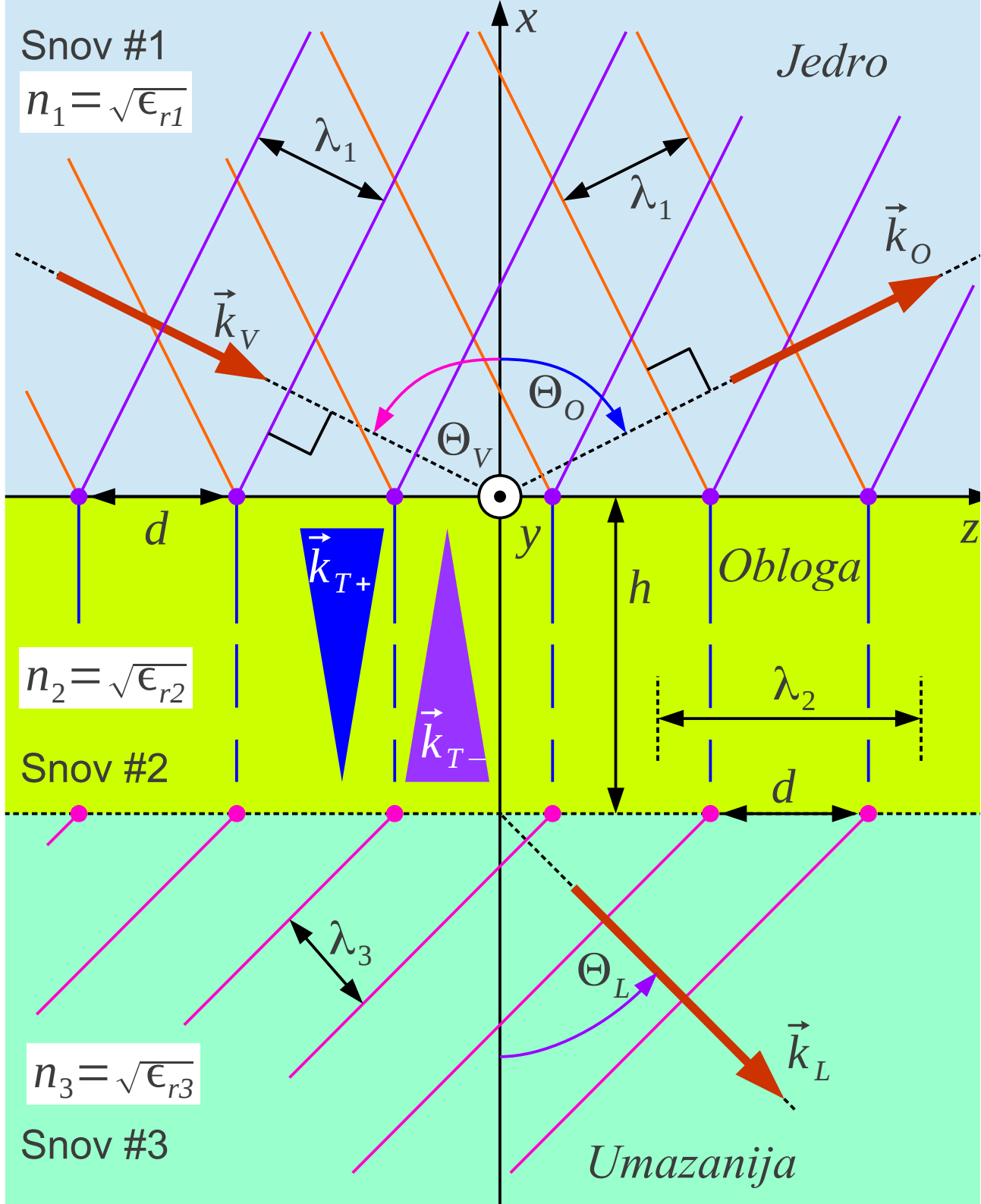
$$\text{Re}[\vec{E}_{T+} \cdot \vec{E}_{T-}^*] = 0$$

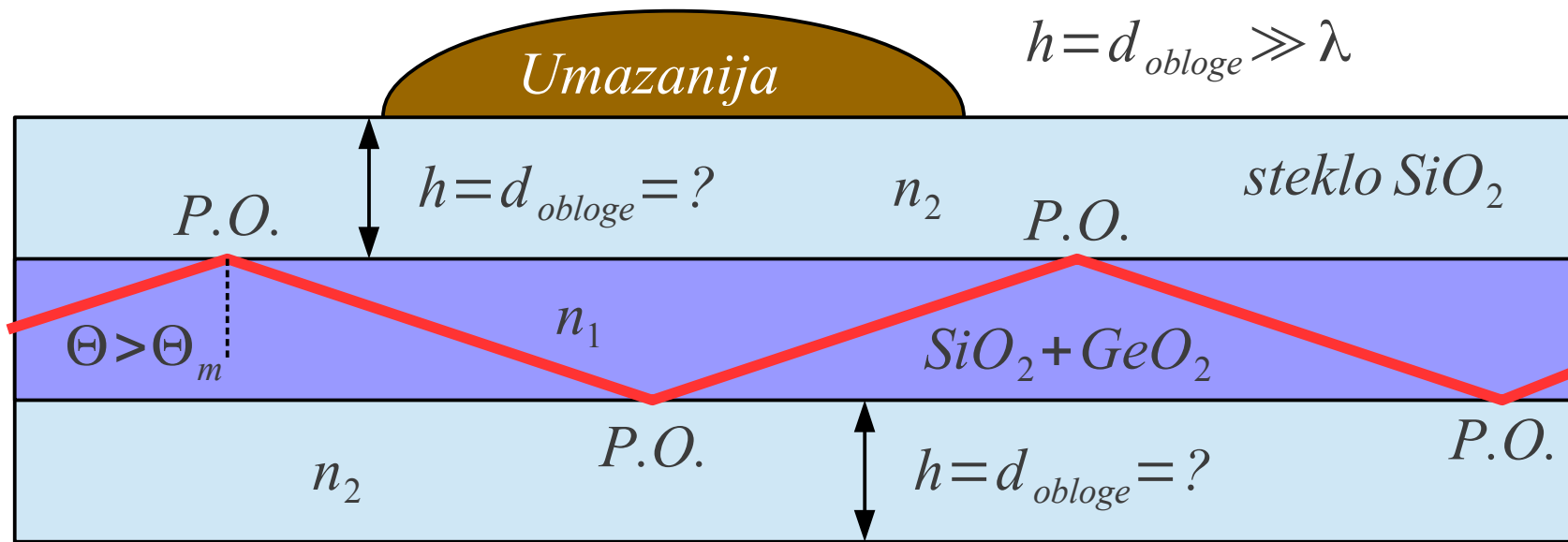
$$\text{Re}[-\vec{1}_x \cdot \vec{S}_2] \neq 0$$

Lom

$$k_{Lx} = -k_{3x} = -\sqrt{n_3^2 k_0^2 - \beta^2}$$

$$\vec{E}_3(\vec{r}) = \vec{E}_L(0) e^{+jk_{3x}x} e^{-j\beta z}$$





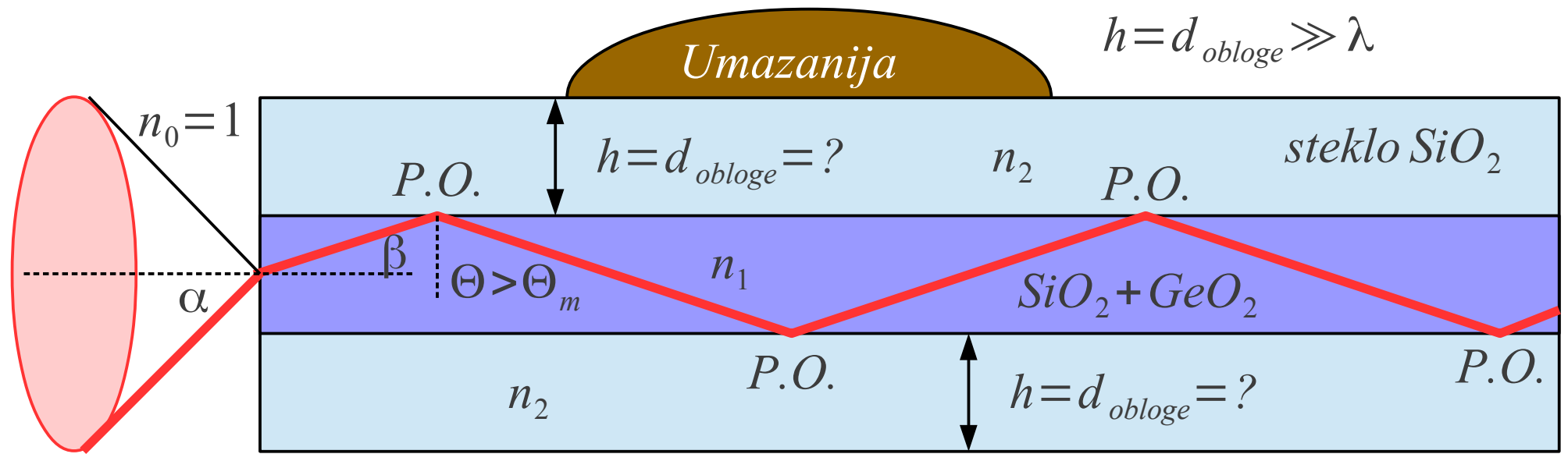
$$n_2 \approx 1.463$$

$$n_1 \approx 1.473$$

$$\Delta \approx 0.007 \rightarrow \text{tehnologija} = ?$$

Majhna razlika $n \rightarrow$ šibkolomno vlakno (valovod)

$$\Delta = \frac{n_1 - n_2}{n_1} \approx \frac{n_1 - n_2}{n} \equiv \text{relativna razlika lomnih količnikov}$$



$$n_2 \approx 1.463$$

$$n_1 \approx 1.473$$

$$\Delta \approx 0.007$$

$$\beta + \Theta = \pi/2$$

$$\sin \alpha = \frac{n_1}{n_0} \sin \beta = n_1 \cos \Theta$$

$$\cos \Theta_m = \sqrt{1 - \sin^2 \Theta_m} = \sqrt{1 - \left(\frac{n_2}{n_1}\right)^2}$$

$$\text{Numerična apertura} \equiv NA = \sin \alpha_m = n_1 \cos \Theta_m$$

Šibkolomni valovod

$$\text{Numerična apertura} \equiv NA = \sqrt{n_1^2 - n_2^2}$$

$$1 \gg NA = \sin \alpha \approx \alpha$$

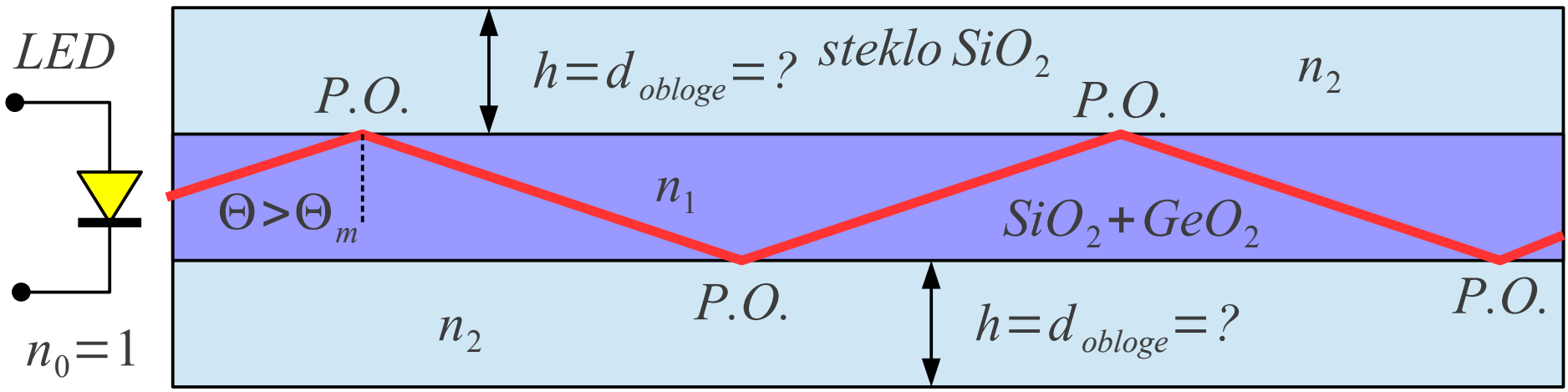
$$NA = \sqrt{n_1^2 - n_2^2} = \sqrt{(n_1 + n_2)(n_1 - n_2)}$$

$$n_1 + n_2 \approx 2n_1$$

$$n_1 - n_2 = \Delta n_1$$

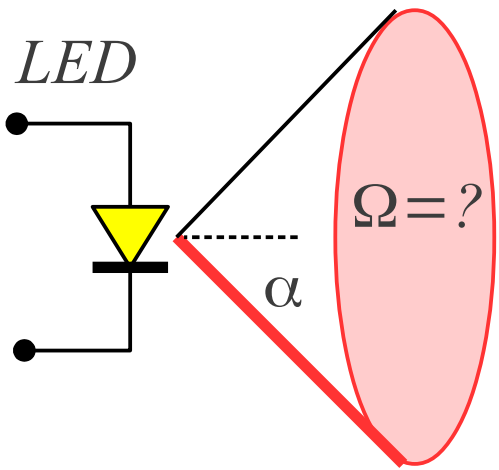
$$NA \approx \sqrt{2n_1 \Delta n_1} = n_1 \sqrt{2\Delta}$$

$$\Delta \approx \frac{1}{2} \left(\frac{NA}{n_1} \right)^2$$



Sklopni izkoristek $\equiv \eta = \frac{\Omega}{4\pi} = \frac{1 - \cos \alpha}{2} = \frac{1 - \sqrt{1 - NA^2}}{2} \approx \frac{NA^2}{4}$

$\cos \alpha = \sqrt{1 - NA^2} \approx 1 - \frac{NA^2}{2}$

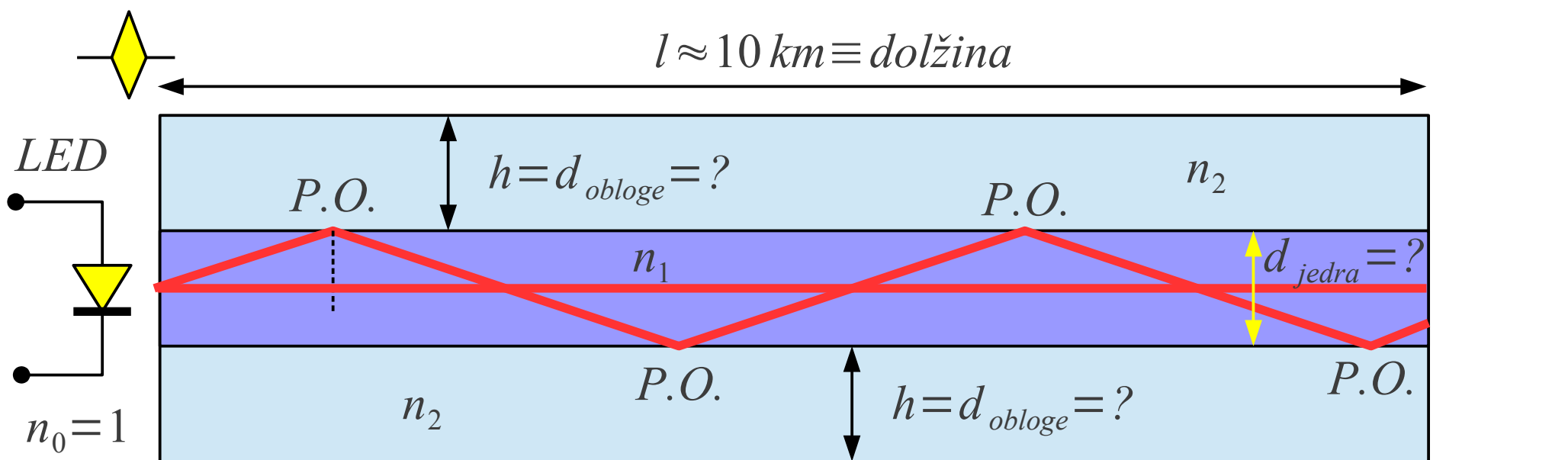


$h = r(1 - \cos \alpha)$

$\Omega = \frac{A}{r^2} = \frac{2\pi r h}{r^2} = 2\pi(1 - \cos \alpha)$

Zgled $NA \approx 0.2$

$\eta \approx \frac{0.2^2}{4} = 0.01$



Raven žarek $t_1 = \frac{l n_1}{c_0}$

$$l' = \frac{l}{\sin \Theta_m} = l \frac{n_1}{n_2}$$

$$\Delta t = t_2 - t_1$$

Cikcak $t_2 = \frac{l' n_1}{c_0} = t_1 \frac{n_1}{n_2}$

$$n_1 \approx 1.5$$

$$\Delta t < \frac{T_{\text{bit}}}{3}$$

$$\Delta \approx 0.009$$

$$\Delta t \approx 0.45 \mu s$$

$$\Delta t = \frac{l n_1}{c_0} \left(\frac{n_1}{n_2} - 1 \right) = \frac{l n_1^2}{c_0 n_2} \Delta \approx \frac{l n_1}{c_0} \Delta$$

$$C [\text{bit/s}] \approx \frac{1}{3 \Delta t} \approx 740 \text{ kbit/s}$$